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## Musical Style Modification as an Optimization Problem

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# Content

1. Introduction and Overview
2. Data corpus
3. Local search within neighborhood
4. Objective functions
5. Results

# Introduction and Overview

## Motivation

- Origin of project

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- Origin of project
- Musical style modification



# Introduction and Overview

## Motivation

- Origin of project
- Musical style modification
- Applications



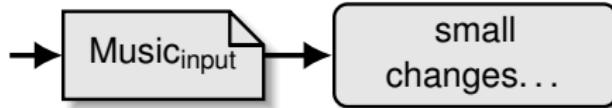
# Introduction and Overview

## Overview of modification procedure



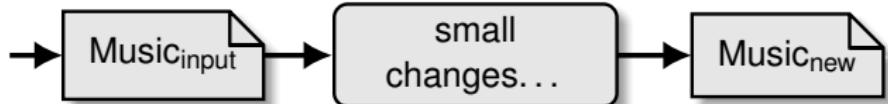
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## Overview of modification procedure



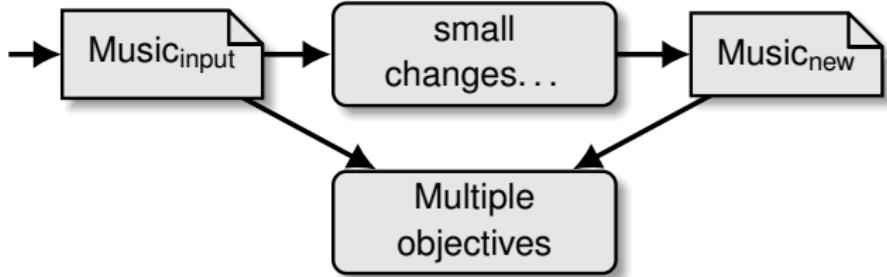
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## Overview of modification procedure



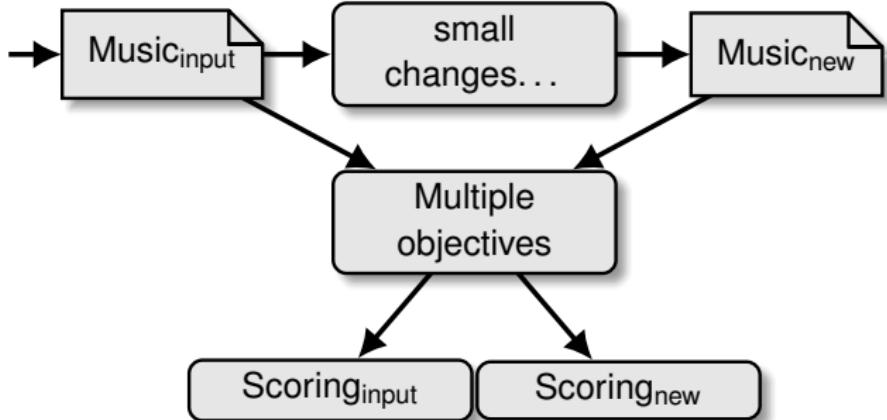
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## Overview of modification procedure



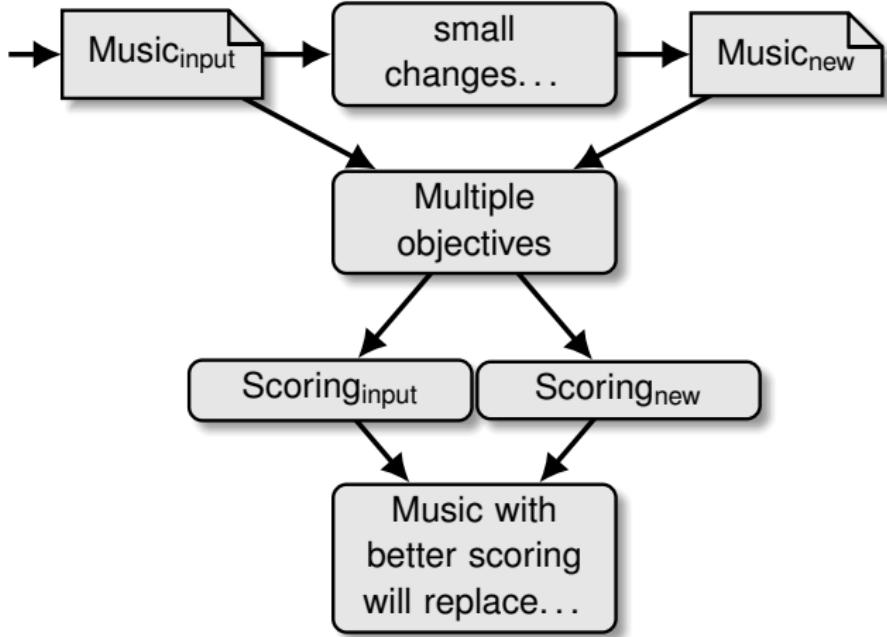
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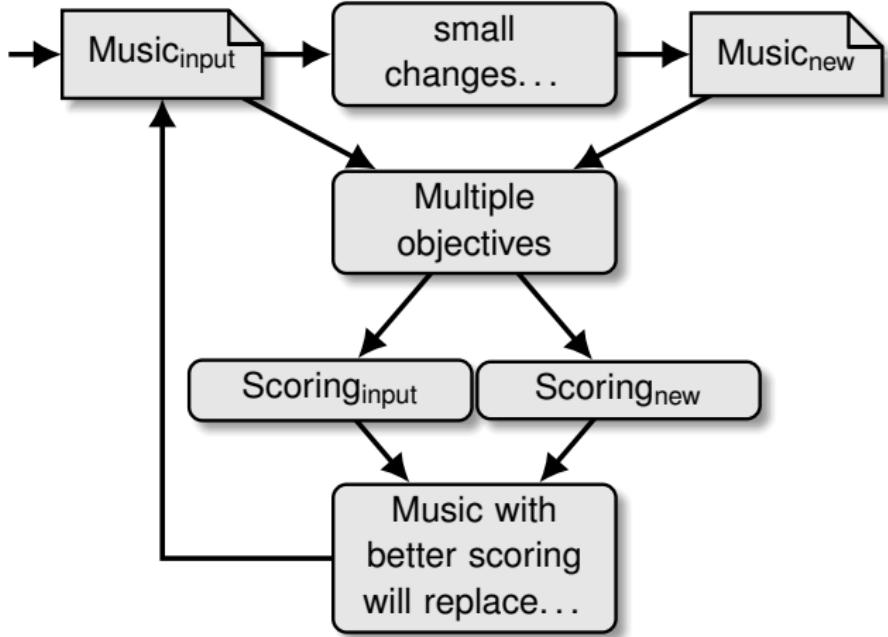
# Introduction and Overview

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# Introduction and Overview

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# Content

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5. Results

# Data corpus

## Pieces

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Jaco Pastorius [Malone, 2002]

Victor Wooten [Wooten, 2003]

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# Data corpus

## Pieces

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### Jaco Pastorius [Malone, 2002]

P. Metheny: *Bright Size Life*  
C. Parker: *Donna Lee*  
J. Pastorius: *Havona*  
W. Shorter: *Port Of Entry*  
J. Pastorius: *Punk Jazz*  
J. Pastorius: *Slang*  
H. Mancini: *The Days of Wine and Roses*  
J. Pastorius: *(Used To Be A) Cha Cha*

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### Victor Wooten [Wooten, 2003]

V. Wooten: *A Show of Hands*  
B. Fleck, V. Wooten and H. Levy: *Blu-Bop*  
R. Noble: *Cherokee (Indian Love Song)*  
V. Wooten: *Classical Thumb*  
J. Lennon and P. McCartney: *Norwegian Wood (This Bird Has Flown)*  
V. Wooten: *Sex in a Pan*  
B. Fleck: *Sinister Minister*  
V. Wooten and B. Fleck: *Stomping Grounds*

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# Data corpus

## Pieces

Jaco Pastorius [Malone, 2002]	Victor Wooten [Wooten, 2003]
P. Metheny: <i>Bright Size Life</i>	V. Wooten: <i>A Show of Hands</i>
C. Parker: <i>Donna Lee</i>	B. Fleck, V. Wooten and H. Levy: <i>Blu-Bop</i>
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J. Pastorius: <i>Punk Jazz</i>	J. Lennon and P. McCartney: <i>Norwegian Wood (This Bird Has Flown)</i>
J. Pastorius: <i>Slang</i>	V. Wooten: <i>Sex in a Pan</i>
H. Mancini: <i>The Days of Wine and Roses</i>	B. Fleck: <i>Sinister Minister</i>
J. Pastorius: <i>(Used To Be A) Cha Cha</i>	V. Wooten and B. Fleck: <i>Stomping Grounds</i>
2227.5 quarter length total	3642.75 quarter length total

# Data corpus

## Pieces – Examples

Jaco Pastorius [Malone, 2002]

Victor Wooten [Wooten, 2003]

### *Donna Lee*

$\text{♩} = 218$

A♭ F<sup>7</sup>  
B♭<sup>7</sup> B♭ m<sup>7</sup>  
E♭<sup>7</sup> A♭ E♭ m<sup>7</sup> D<sup>7</sup>  
D♭ D♭ m<sup>7</sup> A♭  
F<sup>7</sup> B♭<sup>7</sup>

Audio from J. Pastorius: *Jaco Pastorius*, Epic 1976.

# Data corpus

## Pieces – Examples

Jaco Pastorius [Malone, 2002]

Victor Wooten [Wooten, 2003]

### *Donna Lee*

Sheet music for Jaco Pastorius' "Donna Lee". The tempo is  $\text{♩} = 218$ . The key signature is A♭ major (three flats). The music consists of two staves. The top staff starts with a rest, followed by a series of eighth-note patterns. The bottom staff begins at measure 3 with a B♭7 chord. Measures 6 and 9 show E♭7 and D♭ chords respectively. Measures 12 and 15 feature F7 and B♭7 chords. The music is highly rhythmic, with many sixteenth-note patterns and grace notes.

Audio from J. Pastorius: *Jaco Pastorius*, Epic 1976.

### *Classical Thumb*

Sheet music for Victor Wooten's "Classical Thumb". The tempo is  $\text{♩} = 132$ . The key signature is N.C. (no key signature). The music is composed of a single bass line. It features eighth-note patterns and includes measures 3, 5, and 7. The bass line is characterized by its rhythmic precision and technical skill, demonstrating a classical approach to thumb-style bass playing.

Audio from V. Wooten: *A Show of Hands*, Compass 1996.

# Content

1. Introduction and Overview
2. Data corpus
3. Local search within neighborhood
4. Objective functions
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# Local search within neighborhood

Note events:  $N = (n_1, n_2, \dots, n_I)$  where  $n_i = (p_i, d_i)$

## Local search within neighborhood

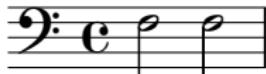
Note events:  $N = (n_1, n_2, \dots, n_I)$  where  $n_i = (p_i, d_i)$

Chord events:  $C = (c_1, c_2, \dots, c_J)$  where  $c_j = (s_j, d_j)$

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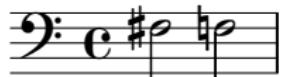
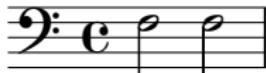
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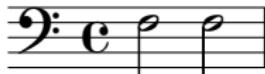


- Changing the pitch  $p_i$

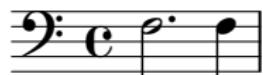
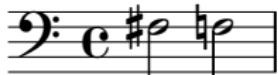
## Local search within neighborhood

Note events:  $N = (n_1, n_2, \dots, n_I)$  where  $n_i = (p_i, d_i)$

Chord events:  $C = (c_1, c_2, \dots, c_J)$  where  $c_j = (s_j, d_j)$



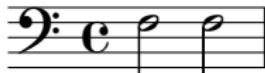
- Changing the pitch  $p_i$
- Changing the duration of two notes  $d_{i_1}$  and  $d_{i_2}$



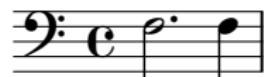
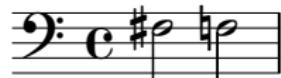
## Local search within neighborhood

Note events:  $N = (n_1, n_2, \dots, n_I)$  where  $n_i = (p_i, d_i)$

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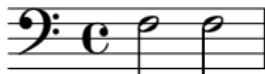
- Changing the pitch  $p_i$
- Changing the duration of two notes  $d_{i_1}$  and  $d_{i_2}$
- Dividing  $n_i$  into multiple notes



## Local search within neighborhood

Note events:  $N = (n_1, n_2, \dots, n_I)$  where  $n_i = (p_i, d_i)$

Chord events:  $C = (c_1, c_2, \dots, c_J)$  where  $c_j = (s_j, d_j)$



- Changing the pitch  $p_i$
- Changing the duration of two notes  $d_{i_1}$  and  $d_{i_2}$
- Dividing  $n_i$  into multiple notes
- Joining  $n_i$  and  $n_{i+1}$  into single note



# Content

1. Introduction and Overview
2. Data corpus
3. Local search within neighborhood
- 4. Objective functions**
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# Objective functions

## Feature classification

- Windowing (overlapping segments of 2–12 quarter lengths)

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- Windowing (overlapping segments of 2–12 quarter lengths)
- 324 of music21's feature extractors [Cuthbert et al., 2011] as well as 86 customly designed ones

# Objective functions

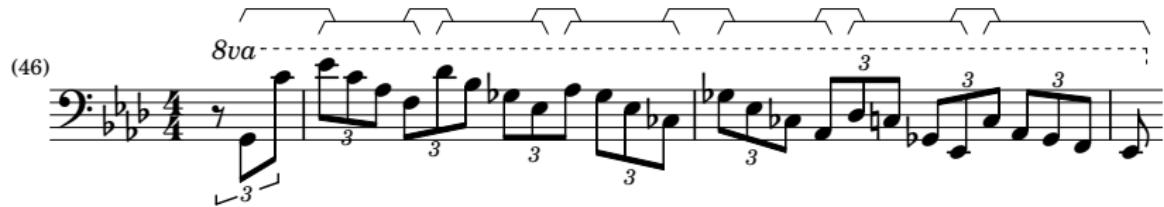
## Feature classification

- Windowing (overlapping segments of 2–12 quarter lengths)
- 324 of music21's feature extractors [Cuthbert et al., 2011] as well as 86 customly designed ones
- Gradient Tree Boosting [Hastie et al., 2009], outputting probability

# Objective functions

## Feature classification

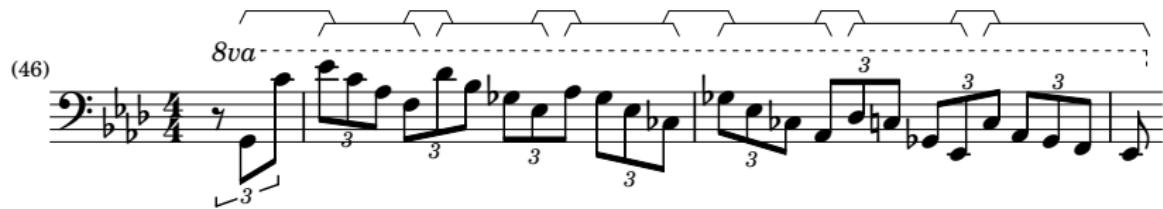
Example of customly designed features:



# Objective functions

## Feature classification

Example of customly designed features:

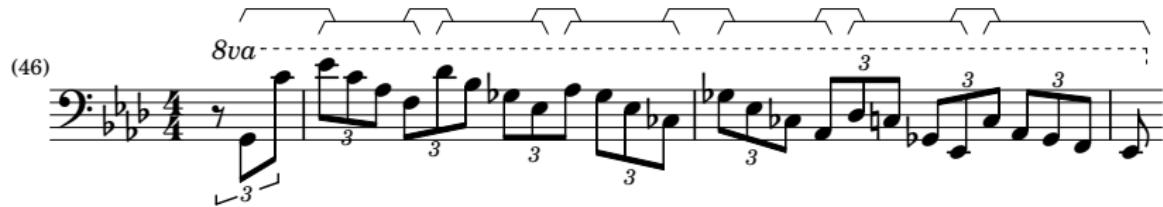


$$f_{\text{Jaco}} = \frac{f_{\text{Len}}}{b} \bmod 1 \text{ where } \frac{a}{b} = f_{\text{Dur}}, \\ \gcd(a, b) = 1$$

# Objective functions

## Feature classification

Example of customly designed features:



$$f_{\text{Jaco}} = \frac{f_{\text{Len}}}{b} \bmod 1 \text{ where } \frac{a}{b} = f_{\text{Dur}}, \\ \gcd(a, b) = 1$$

$f_{\text{Len}} = 4$  and  $f_{\text{Dur}} = 1/3$ , so  $f_{\text{Jaco}} = 4/3 \bmod 1 = 1/3$

# Objective functions

## Markov probability

- Separate Markov chains for durations and pitches

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- Linear interpolation smoothing

# Objective functions

## Markov probability

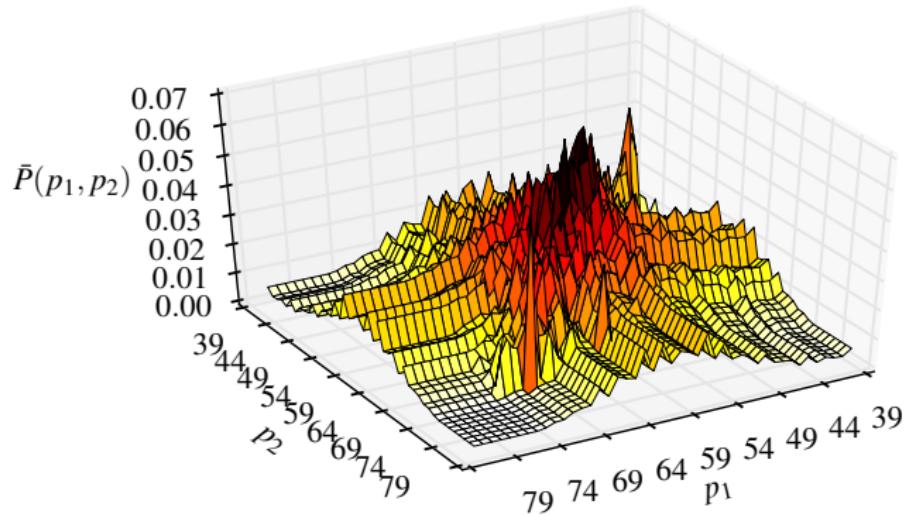
- Separate Markov chains for durations and pitches
- Separate Markov chains per chord symbol type
- Linear interpolation smoothing
- Additive smoothing

## Objective functions

Ratio of example/counter-example Markov probability

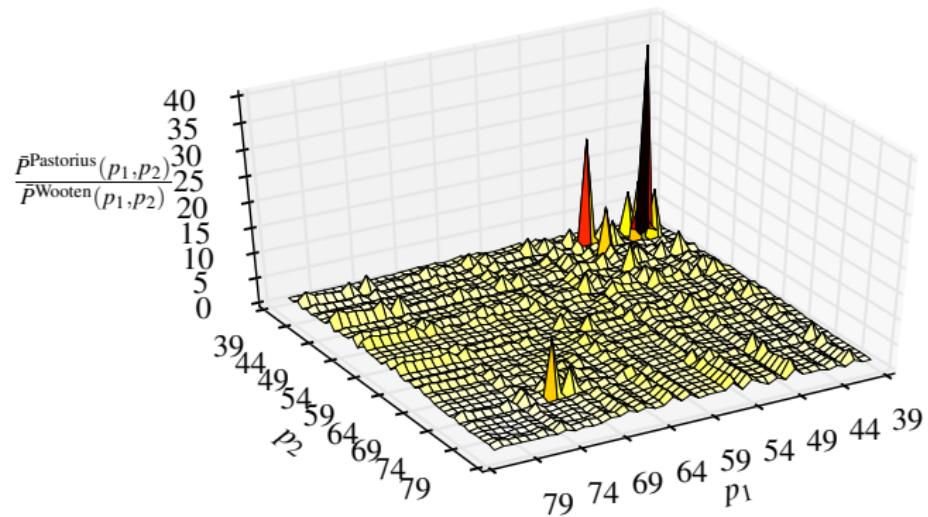
## Objective functions

Ratio of example/counter-example Markov probability



## Objective functions

Ratio of example/counter-example Markov probability



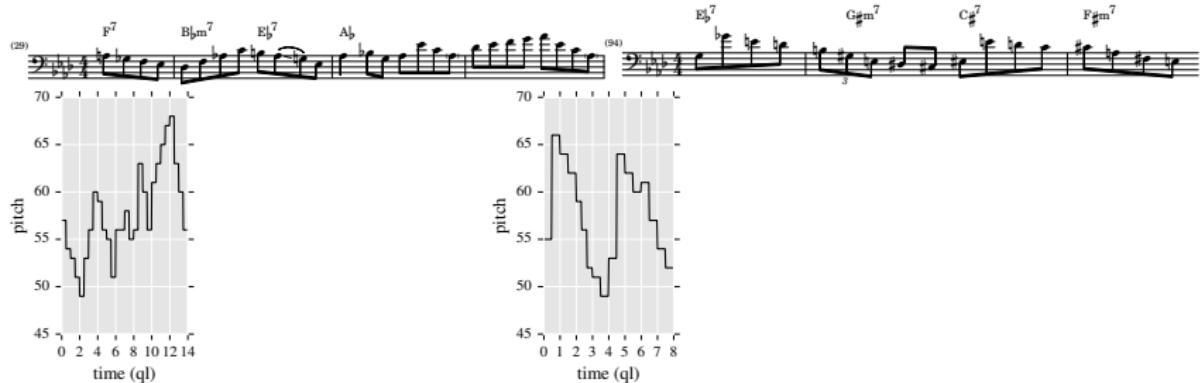
# Objective functions

## Time correlations for chord-repetitions



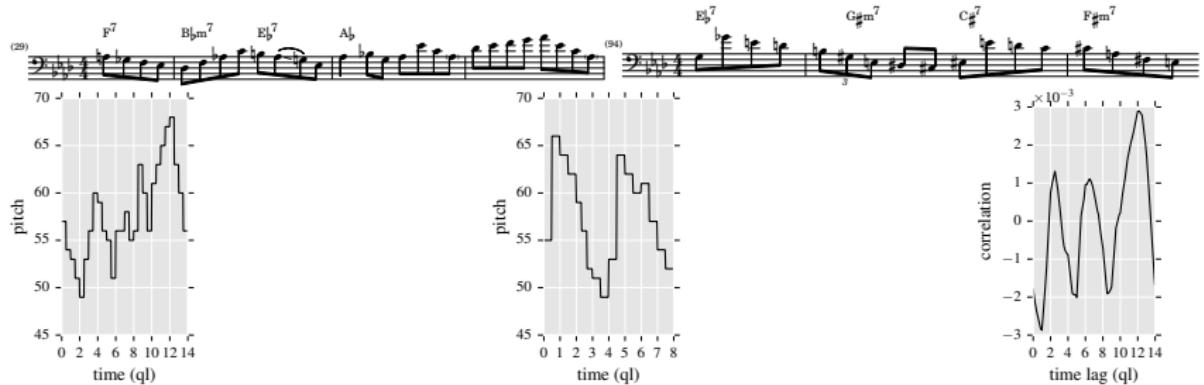
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## Time correlations for chord-repetitions



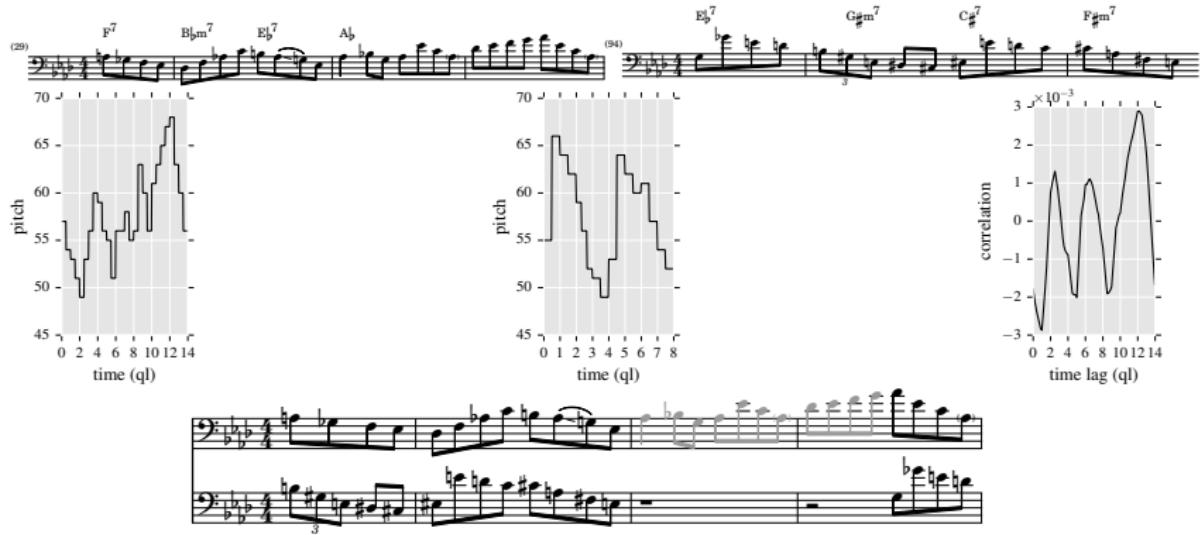
# Objective functions

## Time correlations for chord-repetitions



# Objective functions

## Time correlations for chord-repetitions



# Content

1. Introduction and Overview
2. Data corpus
3. Local search within neighborhood
4. Objective functions
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# Results

## Problem of evaluation

# Results

## Example

### Original

A musical score for a double bass in 3/4 time. The key signature is one flat. The score consists of three staves of music. The first staff starts with a pickup followed by measures 1 through 5. Measure 1 has a bass note followed by eighth-note pairs. Measures 2-5 show a repeating pattern of eighth-note pairs. The second staff starts at measure 6 with eighth-note pairs, followed by measures 7-11 which show a repeating pattern. The third staff starts at measure 12 with eighth-note pairs, followed by measures 13-15 which show a repeating pattern. Chords are labeled above the staff: N.C. F, F<sup>7</sup>, B♭, F, C, C<sup>7</sup>, F, F<sup>7</sup>, B♭, F, C<sup>7</sup>, F.

### iteration 0 (0 accepted changes, target style Pastorius)

A musical score for a double bass in 3/4 time, identical in structure to the original score. It consists of three staves of music. The first staff starts with a pickup followed by measures 1 through 5. The second staff starts at measure 6 with eighth-note pairs, followed by measures 7-11. The third staff starts at measure 12 with eighth-note pairs, followed by measures 13-15. Chords are labeled above the staff: N.C. F, F<sup>7</sup>, B♭, F, C, C<sup>7</sup>, F, F<sup>7</sup>, B♭, F, C<sup>7</sup>, F.

# Results

## Example

Original

Original musical score for bassoon in 3/4 time. The score consists of three staves of music. The first staff starts at measure 1 with a pickup followed by measures 2-4. Measure 2 has a label "N.C." above it. Measures 3 and 4 have labels "F" and "F<sup>7</sup>" above them respectively. Measures 5-7 have labels "B♭" and "F" above them respectively. Measures 8-10 have labels "C" and "C<sup>7</sup>" above them respectively. Measures 11-13 have labels "F" and "F<sup>7</sup>" above them respectively. Measures 14-16 have labels "B♭" and "F" above them respectively. Measures 17-19 have labels "C" and "C<sup>7</sup>" above them respectively. Measures 20-22 have labels "F" and "F<sup>7</sup>" above them respectively. Measures 23-25 have labels "B♭" and "F" above them respectively. Measures 26-28 have labels "C" and "C<sup>7</sup>" above them respectively. Measures 29-31 have labels "F" and "F<sup>7</sup>" above them respectively.

iteration 140

(5 accepted changes, target style Pastorius)

Musical score after iteration 140, showing 5 accepted changes in the target style of Pastorius. The score follows the same structure as the original, with measures 1-3 being a pickup. Measures 4-6 show changes: measure 4 has a sharp sign above the first note; measure 5 has a label "F" above it; measure 6 has a label "F<sup>7</sup>" above it. Measures 7-9 show changes: measure 7 has a label "B♭" above it; measure 8 has a label "F" above it; measure 9 has a label "F<sup>7</sup>" above it. Measures 10-12 show changes: measure 10 has a label "C" above it; measure 11 has a label "C<sup>7</sup>" above it; measure 12 has a label "F" above it. Measures 13-15 show changes: measure 13 has a label "F" above it; measure 14 has a label "F<sup>7</sup>" above it; measure 15 has a label "B♭" above it. Measures 16-18 show changes: measure 16 has a label "C" above it; measure 17 has a label "C<sup>7</sup>" above it; measure 18 has a label "F" above it. Measures 19-21 show changes: measure 19 has a label "F" above it; measure 20 has a label "F<sup>7</sup>" above it; measure 21 has a label "B♭" above it. Measures 22-24 show changes: measure 22 has a label "C" above it; measure 23 has a label "C<sup>7</sup>" above it; measure 24 has a label "F" above it. Measures 25-27 show changes: measure 25 has a label "F" above it; measure 26 has a label "F<sup>7</sup>" above it; measure 27 has a label "B♭" above it.

# Results

## Example

Original

Original musical score for bassoon in 3/4 time. The score consists of three staves of music. The first staff starts at measure 1 with a pickup followed by measures 2-4. Measures 2 and 3 have a key signature of one sharp (F#). Measure 4 has a key signature of one flat (Bb). The second staff starts at measure 5 with a key signature of one flat (Bb). Measures 5-7 have a key signature of one sharp (C#). Measures 8-10 have a key signature of one flat (Bb). The third staff starts at measure 11 with a key signature of one flat (Bb). Measures 11-13 have a key signature of one sharp (C#).

N.C. F      F<sup>7</sup>      B<sub>b</sub>      F

6      C      C<sup>7</sup>      F      F<sup>7</sup>

12      B<sub>b</sub>      F      C<sup>7</sup>      F

iteration 644  
(10 accepted changes, target style Pastorius)

Iterated musical score for bassoon in 3/4 time, labeled "iteration 644 (10 accepted changes, target style Pastorius)". The score follows the same structure as the original, but with changes in harmonic progression and rhythm. The first staff now starts with a key signature of one flat (Bb) for measures 2-4. The second staff starts with a key signature of one sharp (C#) for measures 5-7. The third staff starts with a key signature of one sharp (C#) for measures 11-13.

N.C. F      F<sup>7</sup>      B<sub>b</sub>      F

6      C      C<sup>7</sup>      F      F<sup>7</sup>

12      B<sub>b</sub>      F      C<sup>7</sup>      F

# Results

## Example

Original

Original musical score for bassoon in 3/4 time. The score consists of three staves of music. The first staff starts at measure 1 with a pickup followed by measures 2-4. Measures 2 and 4 have a key signature of one sharp (F#). Measure 3 has a key signature of one flat (Bb). Measures 5-7 have a key signature of one flat (Bb). Measures 8-10 have a key signature of one sharp (F#). Measures 11-13 have a key signature of one flat (Bb). Measures 14-15 have a key signature of one sharp (F#).

iteration 2058  
(14 accepted changes, target style Pastorius)

Generated musical score for iteration 2058, target style Pastorius. The score consists of three staves of music. The first staff starts at measure 1 with a pickup followed by measures 2-4. Measures 2 and 4 have a key signature of one sharp (F#). Measure 3 has a key signature of one flat (Bb). Measures 5-7 have a key signature of one flat (Bb). Measures 8-10 have a key signature of one sharp (F#). Measures 11-13 have a key signature of one flat (Bb). Measures 14-15 have a key signature of one sharp (F#).

# Results

## Example

Original

Original musical score for iteration 1776. The score consists of three staves of music for a bassoon. The first staff starts at measure 1 with a pickup followed by measures 2-4. The second staff starts at measure 5 with a pickup followed by measures 6-8. The third staff starts at measure 9 with a pickup followed by measures 10-12. Chords indicated are N.C., F, F<sup>7</sup>, B♭, F, C, C<sup>7</sup>, F, F<sup>7</sup>, B♭, F, C<sup>7</sup>, F.

iteration 1776  
(24 accepted changes, target style Wooten)

Iteration 1776 musical score. The score consists of three staves of music for a bassoon. The first staff starts at measure 1 with a pickup followed by measures 2-4. The second staff starts at measure 5 with a pickup followed by measures 6-8. The third staff starts at measure 9 with a pickup followed by measures 10-12. Chords indicated are N.C., F, F<sup>7</sup>, B♭, F, C, C<sup>7</sup>, F, F<sup>7</sup>, B♭, F, C<sup>7</sup>, F.

# Results

## Recap

- Method for musical style modification

# Results

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- Method for musical style modification
- Local optimization is great for this task

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## Recap

- Method for musical style modification
- Local optimization is great for this task
- Hard to evaluate

# References

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