

Ringvorlesung WS 2021/22
Aktuelle Perspektiven der Digital Humanities

Neue Wege für die Musikforschung mittels Digitaler Signalverarbeitung (Teil I)

Meinard Müller, Christof Weiß

International Audio Laboratories Erlangen
meinard.mueller@audiolabs-erlangen.de, christof.weiss@audiolabs-erlangen.de



Meinard Müller



- Mathematics (Diplom/Master)
Computer Science (PhD)
Information Retrieval (Habilitation)



- Since 2012: Professor
Semantic Audio Processing



- President of the International Society for
Music Information Retrieval (MIR)



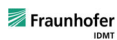
- IEEE Fellow for contributions to Music Signal
Processing



Christof Weiß

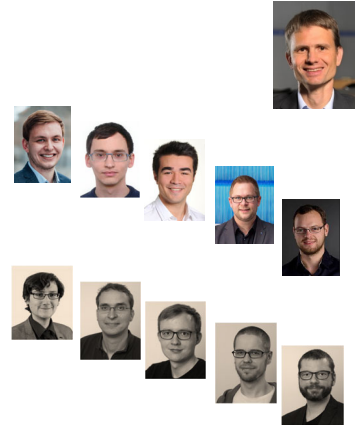


- Physics Diploma & Composition
- Ph. D. in Media Technology
- Postdoc in Music Processing & Composer
- 2018: KlarText Award for Science Communication
- 2021: Postdoc at Télécom ParisTech



Group Members

- Sebastian Rosenzweig
- Michael Krause
- Yigitcan Özer
- Peter Meier (external)
- Christof Weiß (Paris)



- Frank Zalkow
- Christian Dittmar
- Stefan Balke
- Jonathan Driedger
- Thomas Prätzlich
- ...

International Audio Laboratories Erlangen



- Fraunhofer Institute for
Integrated Circuits IIS
- Largest Fraunhofer
institute with
≈ 1000 members
- Applied research for
sensor, audio, and
media technology



- Friedrich-Alexander
Universität Erlangen-
Nürnberg (FAU)
- One of Germany's
largest universities with
≈ 40,000 students
- Large Technical Faculty

AudioLabs – FAU

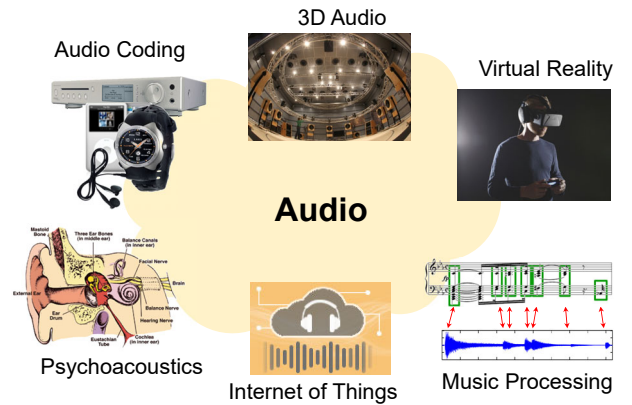
- Prof. Dr. Jürgen Herre
Audio Coding
- Prof. Dr. Bernd Edler
Audio Signal Analysis
- Prof. Dr. Meinard Müller
Semantic Audio Processing
- Prof. Dr. Emanuel Habets
Spatial Audio Signal Processing
- Prof. Dr. Nils Peters
Audio Signal Processing
- Dr. Stefan Turowski
Coordinator AudioLabs-FAU



International Audio Laboratories Erlangen



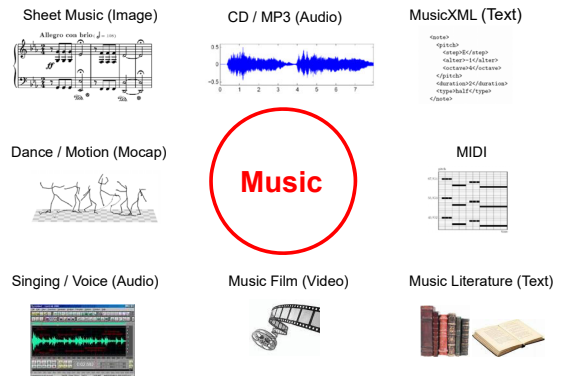
International Audio Laboratories Erlangen



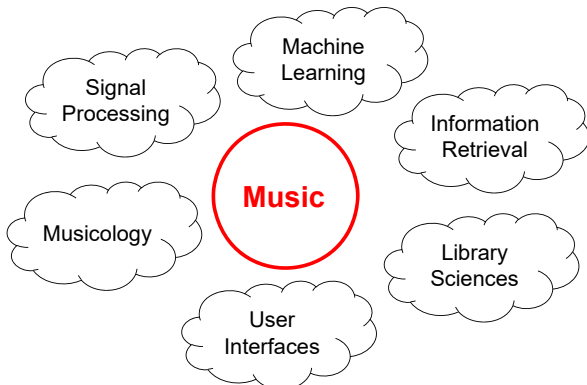
Music



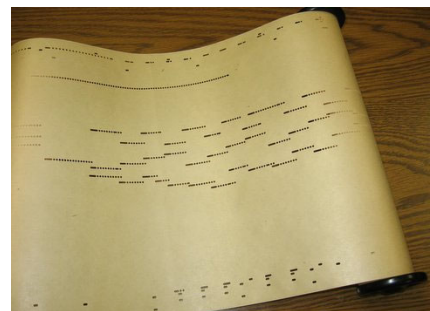
Music Information Retrieval (MIR)



Music Information Retrieval (MIR)



Piano Roll Representation



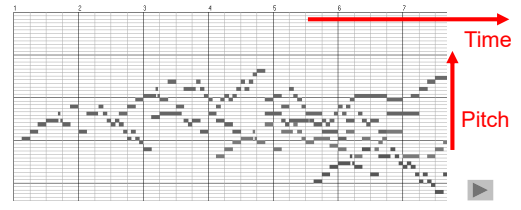
Player Piano (1900)



Piano Roll Representation (MIDI)



J.S. Bach, C-Major Fuge
(Well Tempered Piano, BWV 846)

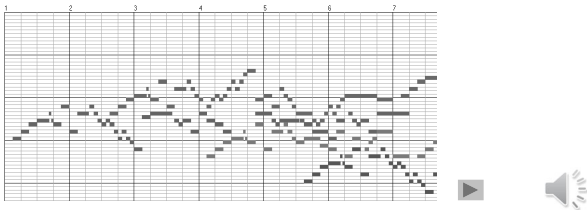


Piano Roll Representation (MIDI)



Query:

Goal: Find all occurrences of the query



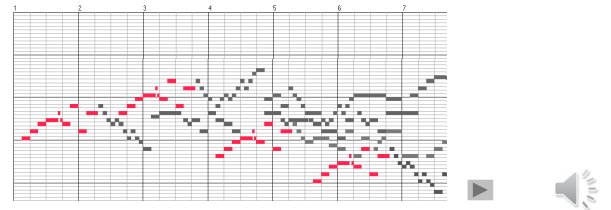
Piano Roll Representation (MIDI)



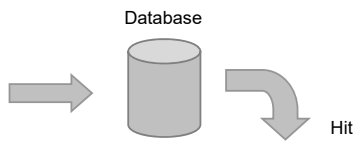
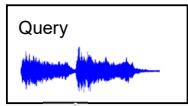
Query:

Goal: Find all occurrences of the query

Matches:



Music Retrieval



Audio-ID

Version-ID

Category-ID

Bernstein (1962)
Beethoven, Symphony No. 5

Beethoven, Symphony No. 5:
▪ Bernstein (1962)
▪ Karajan (1982)
▪ Gould (1992)

Beethoven, Symphony No. 9
Beethoven, Symphony No. 3
Haydn Symphony No. 94

Music Synchronization: Audio-Audio

Beethoven's Fifth

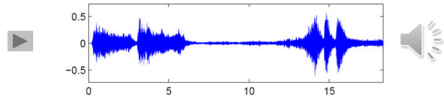


Music Synchronization: Audio-Audio

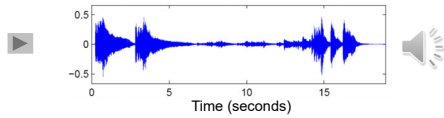
Beethoven's Fifth



Orchester (Karajan)



Piano (Scherbakov)

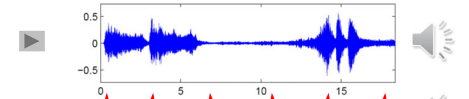


Music Synchronization: Audio-Audio

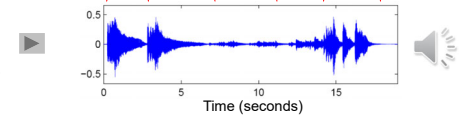
Beethoven's Fifth



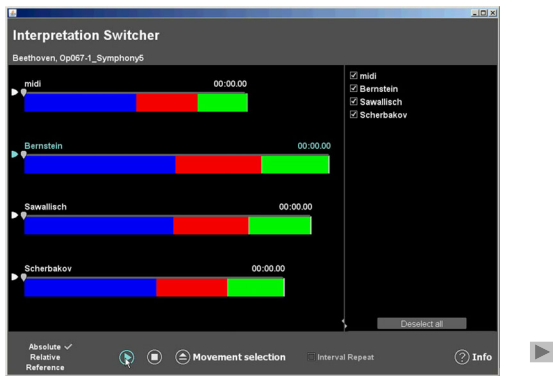
Orchester (Karajan)



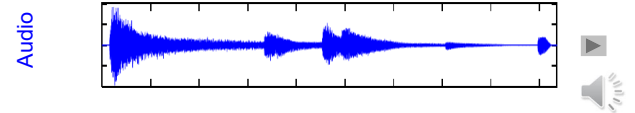
Piano (Scherbakov)



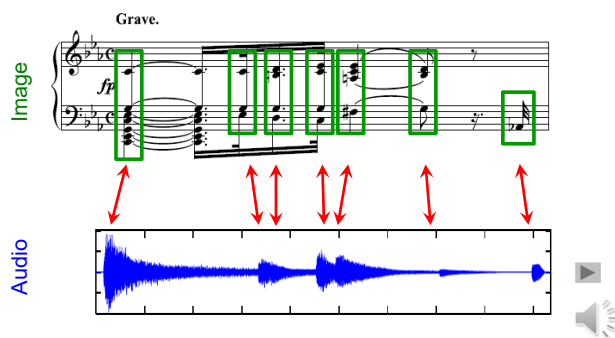
Application: Interpretation Switcher



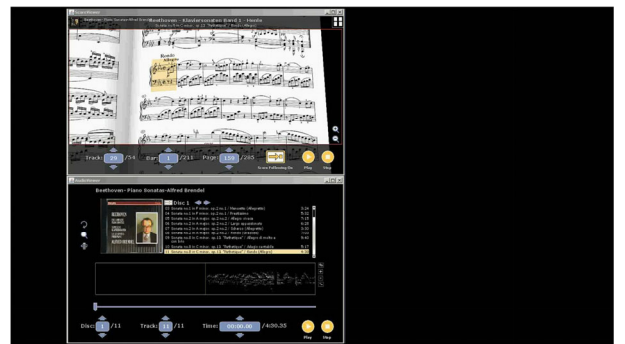
Music Synchronization: Image-Audio



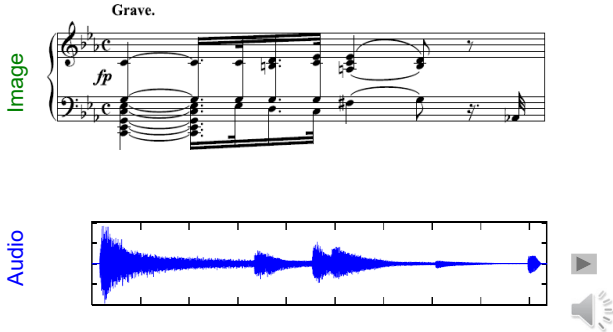
Music Synchronization: Image-Audio



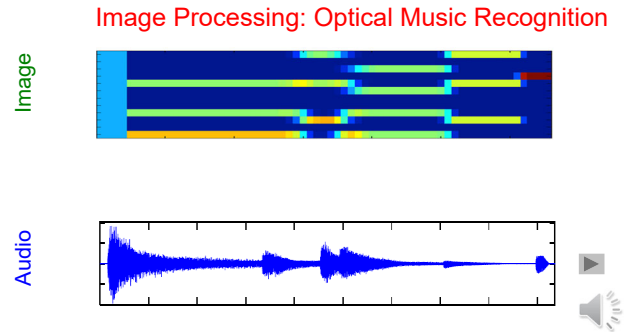
Application: Score Viewer



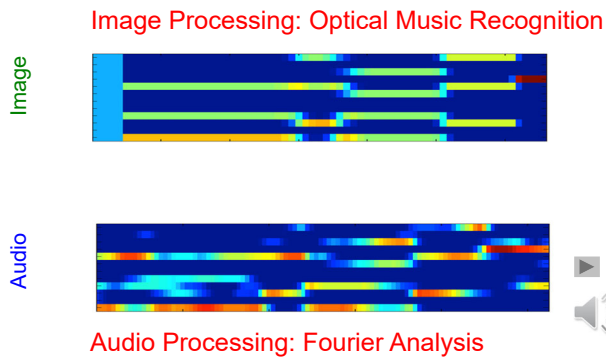
How to make the data comparable?



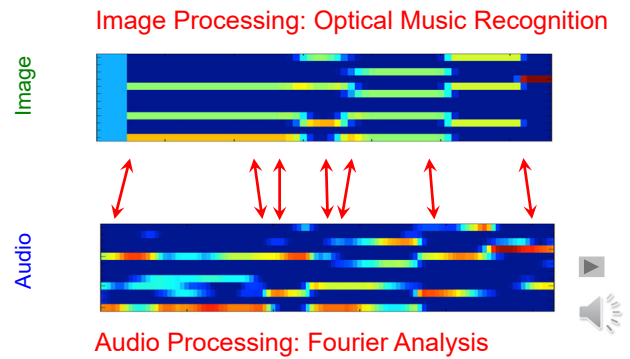
How to make the data comparable?



How to make the data comparable?

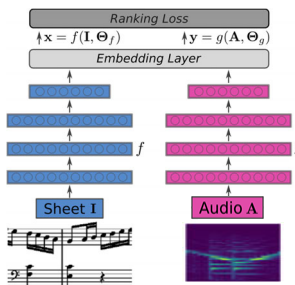


How to make the data comparable?



Music Synchronization: Image-Audio

Deep Learning Approach



- Cross-modal embedding
- Requires corresponding snippets of audio and sheet music for training
- Triplet Loss function $\max(0, d(x^a, y^b) - d(x^a, y^n) + \alpha)$
- Problem very hard
 - Performance variations
 - Layout variations

Cross-Modal Retrieval

Dorfer et al.: End-to-End Cross-Modality Retrieval with CCA Projections and Pairwise Ranking Loss. International Journal of Multimedia Information Retrieval, 2018.

Automatic Music Transcription

Task: Convert a music recording into sheet music

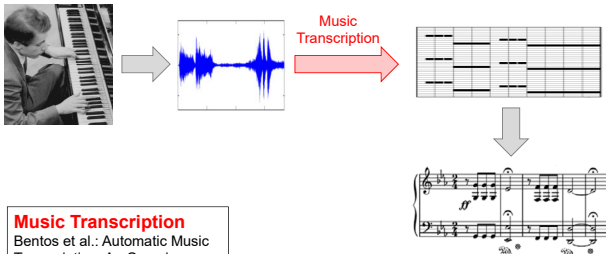


Music Transcription

Bentos et al.: Automatic Music Transcription: An Overview. IEEE Signal Processing Magazine 36(1), 2019.

Automatic Music Transcription

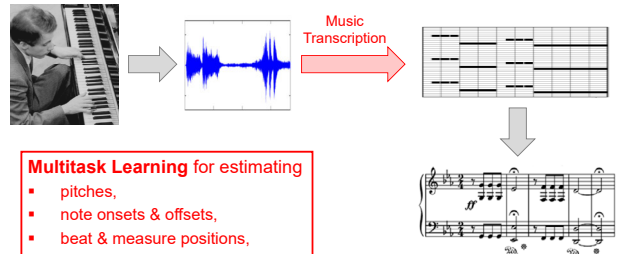
Task: Convert a music recording into sheet music
(or another symbolic music representation)



Music Transcription
Bentos et al.: Automatic Music Transcription: An Overview.
IEEE Signal Processing Magazine 36(1), 2019.

Automatic Music Transcription


Task: Convert a music recording into sheet music
(or another symbolic music representation)



Multitask Learning for estimating

- pitches,
- note onsets & offsets,
- beat & measure positions,
- musical voices & instrumentation,
- pedalling, dynamics, ...

Why is Music Processing Challenging?

Example: Chopin, Mazurka Op. 63 No. 3  

Mazurka.

Allegretto. F. CHOPIN. Op. 63, No. 3.

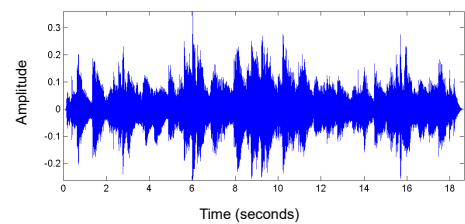
41.

The image shows a musical score for Chopin's Mazurka Op. 63 No. 3. It includes the tempo marking "Allegretto" and the composer's name "F. CHOPIN. Op. 63, No. 3." The score is written for piano and consists of two staves. The first staff is the right hand and the second is the left hand. The music is in 3/4 time and features a mix of eighth and sixteenth notes. There are dynamic markings like "p" and "ff" throughout the piece.

Why is Music Processing Challenging?

Example: Chopin, Mazurka Op. 63 No. 3

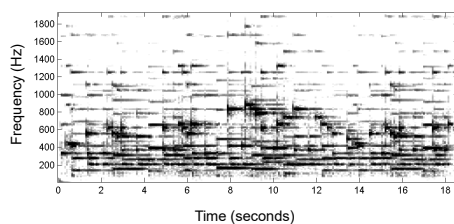
- Waveform



Why is Music Processing Challenging?

Example: Chopin, Mazurka Op. 63 No. 3

- Waveform / Spectrogram



Why is Music Processing Challenging?

Example: Chopin, Mazurka Op. 63 No. 3

- Waveform / Spectrogram

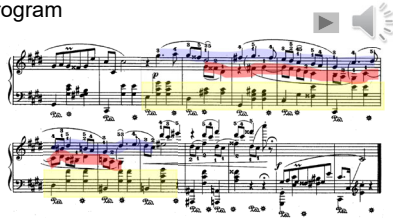
- Performance
 - Tempo
 - Dynamics
 - Note deviations
 - Sustain pedal

Why is Music Processing Challenging?

Example: Chopin, Mazurka Op. 63 No. 3

▪ Waveform / Spectrogram

- Performance
 - Tempo
 - Dynamics
 - Note deviations
 - Sustain pedal



▪ Polyphony

- Main Melody
- Additional melody line
- Accompaniment

Source Separation

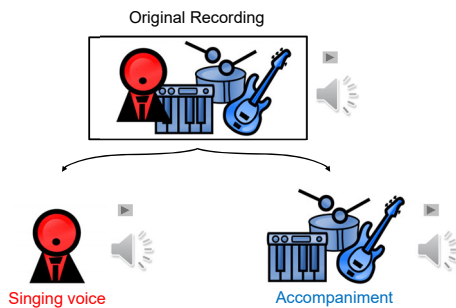
- Decomposition of audio stream into different sound sources
- Central task in digital signal processing
- “Cocktail party effect”
- Several input signals
- Sources are assumed to be statistically independent

Source Separation

- Decomposition of audio stream into different sound sources
- Central task in digital signal processing
- “Cocktail party effect”

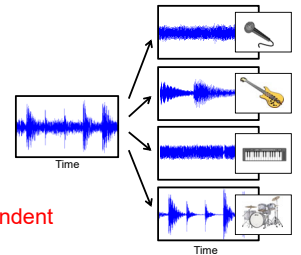


Singing Voice Extraction

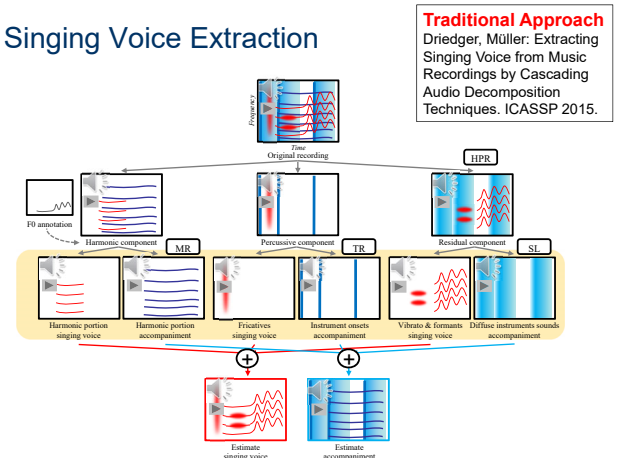


Source Separation (Music)

- Main melody, accompaniment, drum track
- Instrumental voices
- Individual note events
- Only mono or stereo
- Sources are often highly dependent

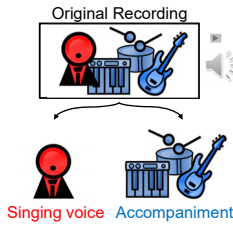


Singing Voice Extraction



Singing Voice Extraction

Deep learning has led to breakthrough



DL-Based Approach
Stöter, Ulich Luitkus, Mitsufuji: Open-Unmix – A Reference Implementation for Music Source Separation. JOSS 2019.

Reference voices:



Engineering approach:

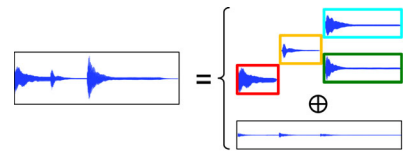
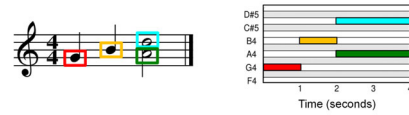


Deep learning approach:



Score-Informed Audio Decomposition

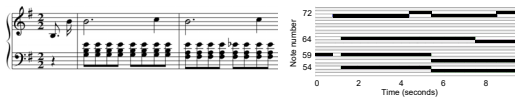
Exploit musical score to support decomposition process



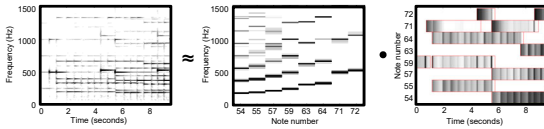
Prior Knowledge
Ewert, Pardo, Müller, Plumbley: Score-Informed Source Separation for Musical Audio Recordings. IEEE SPM, 2014.

Score-Informed Audio Decomposition

Exploit musical score to support decomposition process



NMF-based spectrogram decomposition

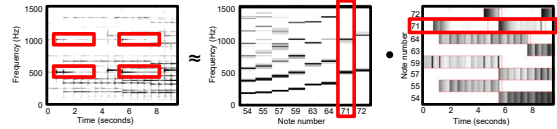


Score-Informed Audio Decomposition

Exploit musical score to support decomposition process

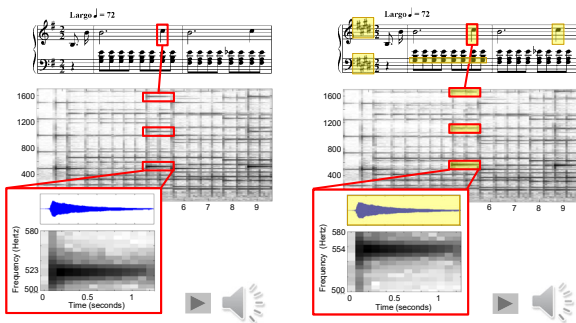


NMF-based spectrogram decomposition

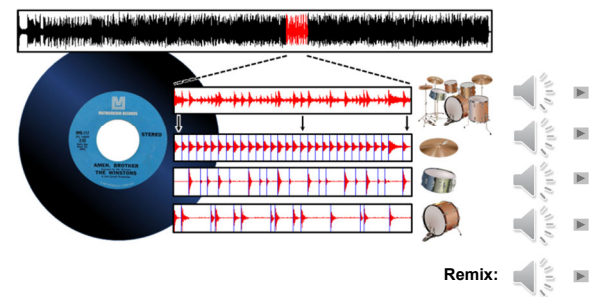


Score-Informed Audio Decomposition

Application: Audio editing



Informed Drum-Sound Decomposition



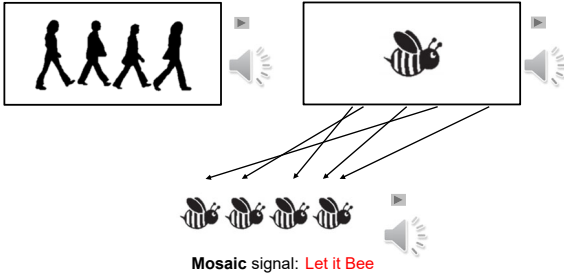
Literature: [Dittmar/Müller, IEEE/ACM-TASLP 2016]

Demo: <https://www.audiolabs-erlangen.de/resources/MIR/2016-IEEE-TASLP-DrumSeparation>

Audio Mosaicing

Target signal: Beatles-Let it be

Source signal: Bees



Literature: [Driedger/Müller, ISMIR 2015]

Demo: <https://www.audiolabs-erlangen.de/resources/MIR/2015-ISMIR-LettBee>

Motivic Similarity



Beethoven's Fifth (1st Mov.)



Beethoven's Fifth (3rd Mov.)



Beethoven's Appassionata



Motivic Similarity

Var. 4: Vivace



Motivic Similarity



S aut - ge - raff,

A und nie - mand ach - tet

T und nie - mand ach - tet drauf

B auf - ge - raff,

Computational Analysis of Traditional Georgian Vocal Music



- Partner: Prof. Frank Scherbaum
Potsdam University
- Duration: 2018 – 2022
- Objectives
 - Harmonic and melodic singing analysis
 - New sensors (larynx microphones)
 - Digital humanities

<https://www.audiolabs-erlangen.de/resources/MIR/2017-GeorgianMusic-Erkomaishvili>

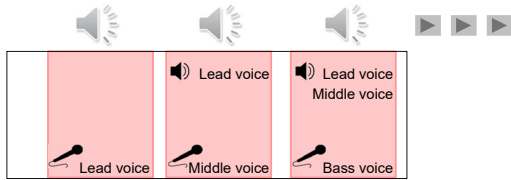
<https://www.audiolabs-erlangen.de/resources/MIR/2018-ISMIR-LBD-ThroatMics>

Traditional Georgian Vocal Music

Which scale? Harmonic/melodic intervals? Singer interaction?

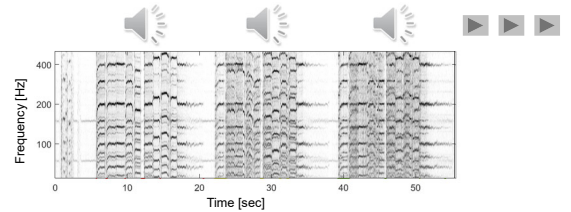


Traditional Georgian Vocal Music



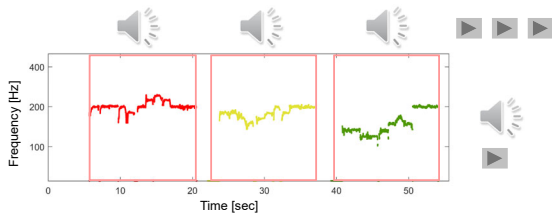
- Master chanter: Artem Erkomaishvili
- Recordings of 100 songs (1966)
- Example song: Da sulisatsa (#87)

Traditional Georgian Vocal Music



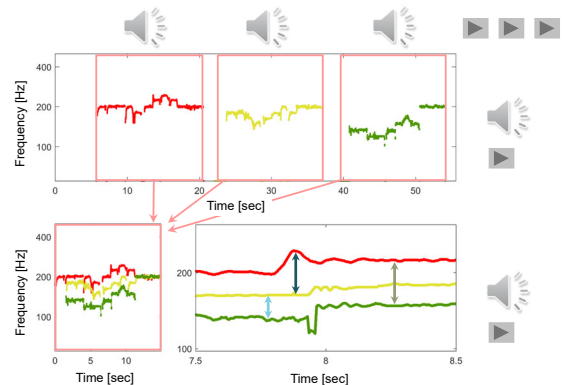
- Master chanter: Artem Erkomaishvili
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Traditional Georgian Vocal Music

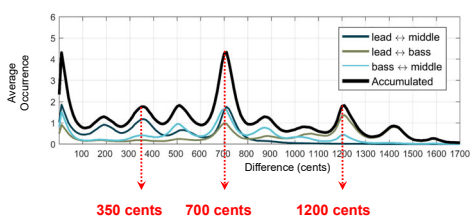


- Master chanter: Artem Erkomaishvili
- Recordings of 100 songs (1966)
- Example song: Da sulisatsa (#87)

Traditional Georgian Vocal Music



Traditional Georgian Vocal Music



- Peak at 350 cents (between minor and major third)
- **Non-western temperament**

Automated Methods and Tools for Analyzing and Structuring Choral Music



- Partner: Carus-Verlag
- Duration: 2018 – 2021
- Objectives
 - Navigation, visualization, sonification of musical structures
 - Practicability & applications (music education, musicology)
 - Web-based prototypes for interactive interfaces



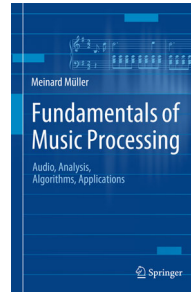
Computer-Assisted Analysis of Harmonic Structures



- Partner: Prof. Rainer Kleinertz
Saarland University
- Duration: 2014 – 2023
- Objectives
 - Computer-assisted harmonic structures
 - Beethoven's Piano Sonatas
 - Wagner's "Der Ring des Nibelungen"

Weiß, Kleinertz (Ringvorlesung, 10.01.2022):
Neue Wege für die Musikforschung mittels Digitaler Signalverarbeitung II

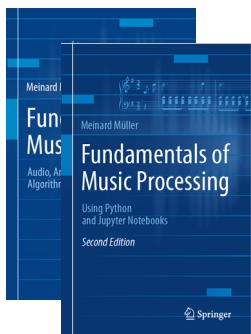
Fundamentals of Music Processing (FMP)



Meinard Müller
Fundamentals of Music Processing
Audio, Analysis, Algorithms, Applications
Springer, 2015

Accompanying website:
www.music-processing.de

Fundamentals of Music Processing (FMP)



Meinard Müller
Fundamentals of Music Processing
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Springer, 2015

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www.music-processing.de

2nd edition
Meinard Müller
Fundamentals of Music Processing
Using Python and Jupyter Notebooks
Springer, 2021

Fundamentals of Music Processing (FMP)

Chapter	Music Processing Scenario
1	Music Representations
2	Fourier Analysis of Signals
3	Music Synchronization
4	Music Structure Analysis
5	Chord Recognition
6	Tempo and Beat Tracking
7	Content-Based Audio Retrieval
8	Musically Informed Audio Decomposition

Meinard Müller
Fundamentals of Music Processing
Audio, Analysis, Algorithms, Applications
Springer, 2015

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www.music-processing.de

2nd edition
Meinard Müller
Fundamentals of Music Processing
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Springer, 2021

FMP Notebooks: Education & Research

FMP Notebooks
Python Notebooks for Fundamentals of Music Processing

The FMP notebooks offer a collection of educational material closely following the textbook [Fundamentals of Music Processing \(FMP\)](https://www.audiolabs-erlangen.de/FMP). This is the starting website, which is opened when calling <https://www.audiolabs-erlangen.de/FMP>. Besides giving an [overview](#), this website provides information on the license, the main contributors, and some links.

<https://www.audiolabs-erlangen.de/FMP>

FMP Notebooks

Part	Title	Notions, Techniques & Algorithms	HTML IPYNB
0	Basics	Basic information on Python, Jupyter notebooks, Anaconda package management system, Python environments, visualizations, and other topics	html ipynb
0	Overview	Overview of the notebooks (https://www.audiolabs-erlangen.de/FMP)	html ipynb
1	Music Representations	Music notation, MIDI, audio signal, waveform, pitch, loudness, timbre	html ipynb
2	Fourier Analysis of Signals	Discrete/analogue signal, sinusoid, exponential, Fourier transform, Fourier representation, DFT, FFT, STFT	html ipynb
3	Music Synchronization	Chrona feature, dynamic programming, dynamic time warping (DTW), alignment, user interface	html ipynb
4	Music Structure Analysis	Similarity matrix, repetition, threshold, homogeneity, novelty, evaluation, precision, recall, F-measure, visualization, scope plot	html ipynb
5	Chord Recognition	Harmony, music theory, chords, scales, templates, hidden Markov model (HMM), evaluation	html ipynb
6	Tempo and Beat Tracking	Onset, novelty, tempo, tempoogram, beat, periodicity, Fourier analysis, autocorrelation	html ipynb
7	Content-Based Audio Retrieval	Identification, fingerprint, indexing, inverted list, matching, version, cover, song	html ipynb
8	Musically Informed Audio Decomposition	Harmonic/percussive separation, signal reconstruction, instantaneous frequency, fundamental frequency (F0), trajectory, nonnegative matrix factorization (NMF)	html ipynb

FMP Notebooks

Structured in 10 parts

Part	Title	Notions, Techniques & Algorithms	HTML	IPYNB
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2	Fourier Analysis of Signals	Discrete/analog signal, sinusoid, exponential, Fourier transform, Fourier representation, DFT, FFT, STFT	html	ipynb
3	Music Synchronization	Chroma feature, dynamic programming, dynamic time warping (DTW), alignment, user interface	html	ipynb
4	Music Structure Analysis	Similarity matrix, repetition, thumbnail, homogeneity, novelty, evaluation, precision, recall, F-measure, visualization, scape plot	html	ipynb
5	Chord Recognition	Harmony, music theory, chords, scales, templates, hidden Markov model (HMM), evaluation	html	ipynb
6	Tempo and Beat Tracking	Onset, novelty, tempo, tempoogram, beat, periodicity, Fourier analysis, autocorrelation	html	ipynb
7	Content-Based Audio Retrieval	Identification, fingerprint, indexing, inverted list, matching, version, cover song	html	ipynb
8	Musically Informed Audio Decomposition	Harmonic/percussive separation, signal reconstruction, instantaneous frequency, fundamental frequency (F0), trajectory, nonnegative matrix factorization (NMF)	html	ipynb

FMP Notebooks

Structured in 10 parts

- Part B: Basic introductions to
 - Jupyter notebook framework
 - Python programming
 - Other technical concepts underlying these notebooks

Part	Title	Notions, Techniques & Algorithms	HTML	IPYNB
B	Basics	Basic information on Python, Jupyter notebooks, Anaconda package management system, Python environments, visualizations, and other topics	html	ipynb
0	Overview	Overview of the notebooks (https://www.audiolabs-erlangen.de/FMP/)	html	ipynb
1	Music Representations	Music notation, MIDI, audio signal, waveform, pitch, loudness, timbre	html	ipynb
2	Fourier Analysis of Signals	Discrete/analog signal, sinusoid, exponential, Fourier transform, Fourier representation, DFT, FFT, STFT	html	ipynb
3	Music Synchronization	Chroma feature, dynamic programming, dynamic time warping (DTW), alignment, user interface	html	ipynb
4	Music Structure Analysis	Similarity matrix, repetition, thumbnail, homogeneity, novelty, evaluation, precision, recall, F-measure, visualization, scape plot	html	ipynb
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FMP Notebooks

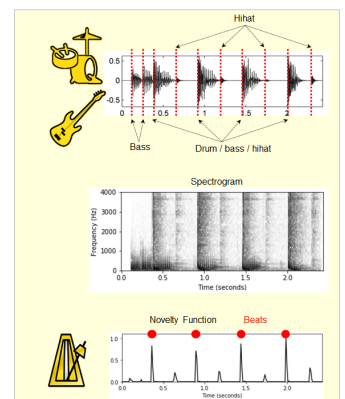
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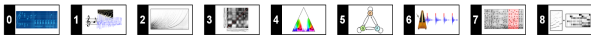
Part 6: Tempo and Beat Tracking

- When listening to a piece of music, we as humans are often able to tap along with the musical beat
- Automated beat tracking: Simulate this cognitive process by a computer



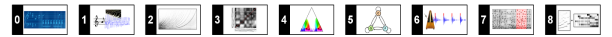
FMP Notebooks
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Basics + 8 Chapters

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Basics + 8 Chapters

Tempo and Beat Tracking

Tempo and Beat Tracking

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Tempo and Beat Tracking

Definition

We assume that we are given a discrete-time novelty function $\Delta : \mathbb{Z} \rightarrow \mathbb{1}$ indicate note onset candidates. The idea of Fourier analysis is to detect to in novelty curve by comparing it with windowed sinusoids. A high correlation of Δ with a windowed sinusoid indicates a periodicity of the novelty curve (given a suitable phase). This correlation (along with the phase) can be extracted by the short-time Fourier transform. To this end, we fix a window function $w : \mathbb{Z} \rightarrow \mathbb{R}$ of length centered at $n = 0$ (e.g., a sampled Hann window). Then, for a frequency parameter $\omega \in \mathbb{R}_{\geq 0}$ and time parameter $n \in \mathbb{Z}$, the complex Fourier coefficient is defined by

$$\mathcal{F}(n, \omega) := \sum_{m \in \mathbb{Z}} \Delta(m) w(m - n) \exp(-2\pi i \omega m).$$

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Explanations

Theory

Mathematics

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Tempo and Beat Tracking

6

Example: Shostakovich

In the following example, we consider an excerpt of a recording of Dimitri Shostakovich's Suite for Variety Orchestra No. 1. The score version of the excerpt.

We start with a [spectral-based novelty function](#) resampled to F_s^A . Furthermore, we use a window size corresponding to 5 seconds (1

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Tempo and Beat Tracking

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Annotations

Music Examples

Audio

Links

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Tempo and Beat Tracking

6

```
In [2]: def compute_sinusoid_optimal(c, tempo, n, Fs, H)
        """Compute windowed sinusoid with optimal F
        Notebook: C6/C6S2_TempogramFourier.ipynb

        Args:
            c: Coefficient of tempogram (c=X(k,n))
            tempo: Tempo parameter corresponding to
            _coef_BPM(k)
            n: Frame parameter of c
            Fs: Sampling rate
            N: Window length
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Python Code

Algorithms

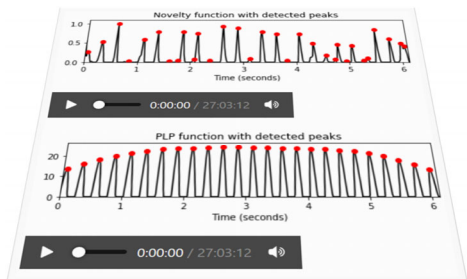
Functions

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Tempo and Beat Tracking

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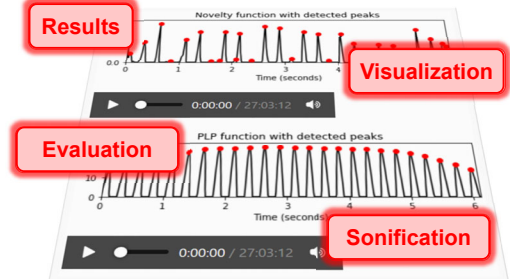


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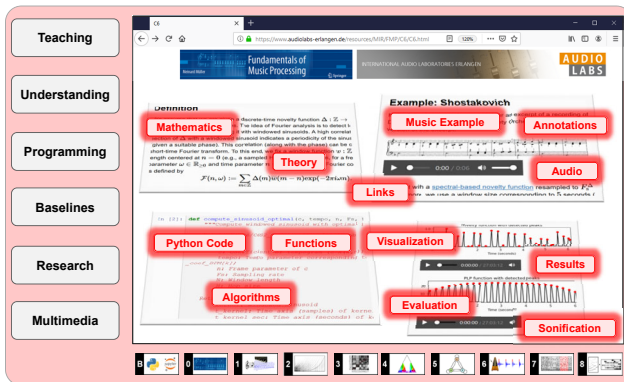
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Tempo and Beat Tracking

6



FMP Notebooks



References

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- Meinard Müller and Frank Zalkow: libfmp: A Python Package for Fundamentals of Music Processing. Journal of Open Source Software (JOSS), 6(63): 1–5, 2021. <https://joss.theoj.org/papers/10.21105/joss.03326>
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- Meinard Müller and Frank Zalkow: FMP Notebooks: Educational Material for Teaching and Learning Fundamentals of Music Processing. Proc. International Society for Music Information Retrieval Conference (ISMIR): 573–580, 2019. https://zenodo.org/record/3527872#_YOHEQgzaUK
- Meinard Müller, Brian McFee, and Katherine Kinnaird: Interactive Learning of Signal Processing Through Music: Making Fourier Analysis Concrete for Students. IEEE Signal Processing Magazine, 38(3): 73–84, 2021. <https://ieeexplore.ieee.org/document/9418542>

Resources (Group Meinard Müller)

- FMP Notebooks: <https://www.audiolabs-erlangen.de/FMP>
- libfmp: <https://github.com/meinardmueller/libfmp>
- synctoolbox: <https://github.com/meinardmueller/synctoolbox>
- libtsm: <https://github.com/meinardmueller/libtsm>
- Preparation Course Python (PCP) Notebooks: <https://www.audiolabs-erlangen.de/resources/MIR/PCP/PCP.html>
<https://github.com/meinardmueller/PCP>

Resources

- librosa: <https://librosa.org/>
- madmom: <https://github.com/CPJKU/madmom>
- Essentia Python tutorial: https://essentia.upf.edu/essentia_python_tutorial.html
- mirdata: <https://github.com/mir-dataset-loaders/mirdata>
- open-unmix: <https://github.com/sigsep/open-unmix-pytorch>
- Open Source Tools & Data for Music Source Separation: <https://source-separation.github.io/tutorial/landing.html>

