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Lecture  
**Music Processing**

# Chord Recognition

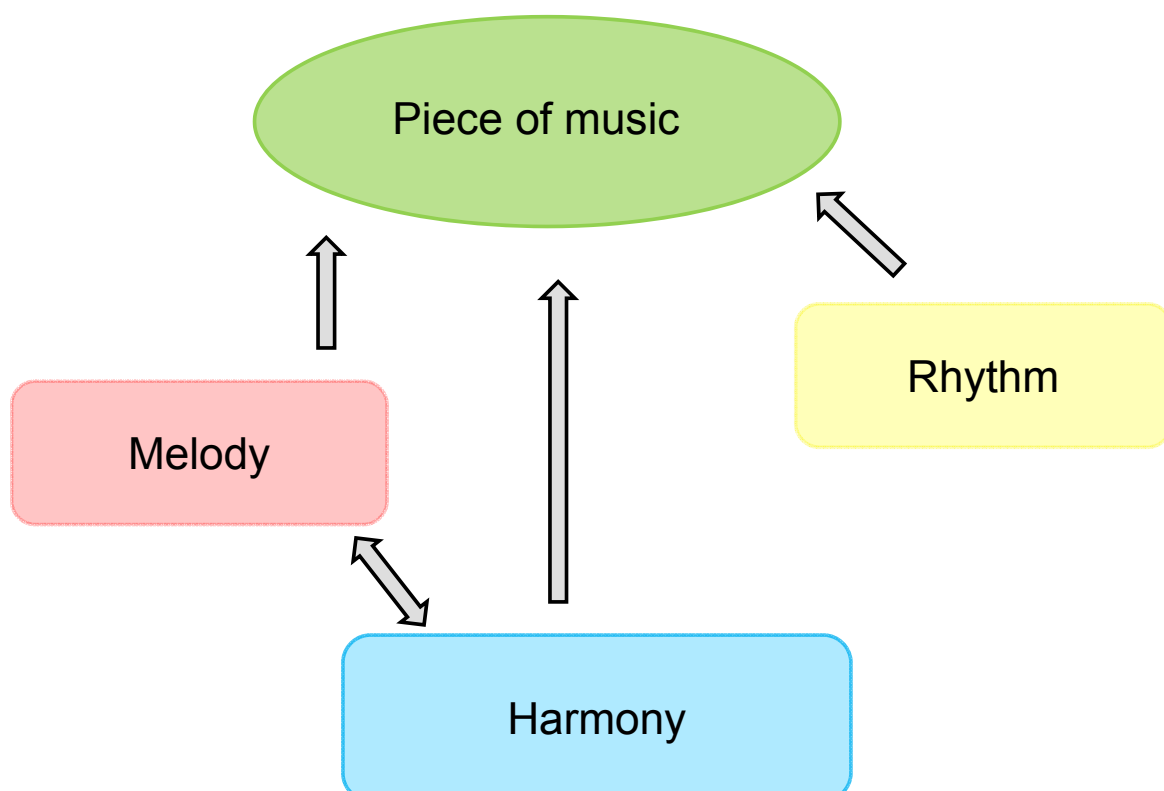
**Meinard Müller**

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meinard.mueller@audiolabs-erlangen.de

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## Aspects of Music



# Harmony: The Basis of Music

## Pachelbel's Canon



Andantino Moderato

Johann Pachelbel  
George Winston

Piano

## Coversong *Die Eine (Die Firma)*



# Musical Chords

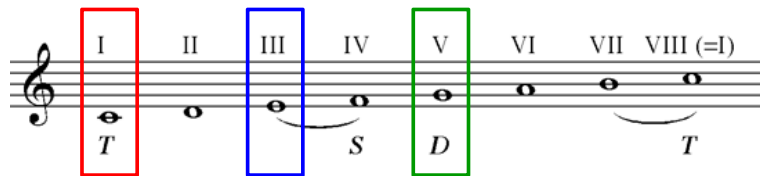
- Combination of three or more tones which sound simultaneously
- Chord classes
  - Triads including major, minor, diminished, augmented chords
  - Many other more complex chords such as seventh chords
- Here: focus on major and minor triads

# Musical Chords

The C **major** chord



Derived from the C **major** scale



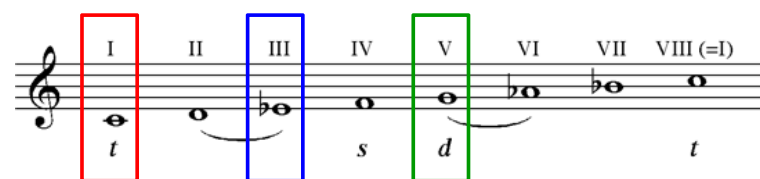
- C ---- the **root**
- E ---- the (**major**) **third**
- G ---- the **fifth**

# Musical Chords

The C **minor** chord



Derived from the C **minor** scale



- C ---- the **root**
- E<sub>b</sub> ---- the (**minor**) **third**
- G ---- the **fifth**

# Musical Chords

Structure of the 24 major/minor chords



	0	1	2	3	4	5	6	7	8	9	10	11
	C	C#	D	D#	E	F	F#	G	G#	A	A#	B
C major	✓				✓			✓				
C minor	✓			✓				✓				



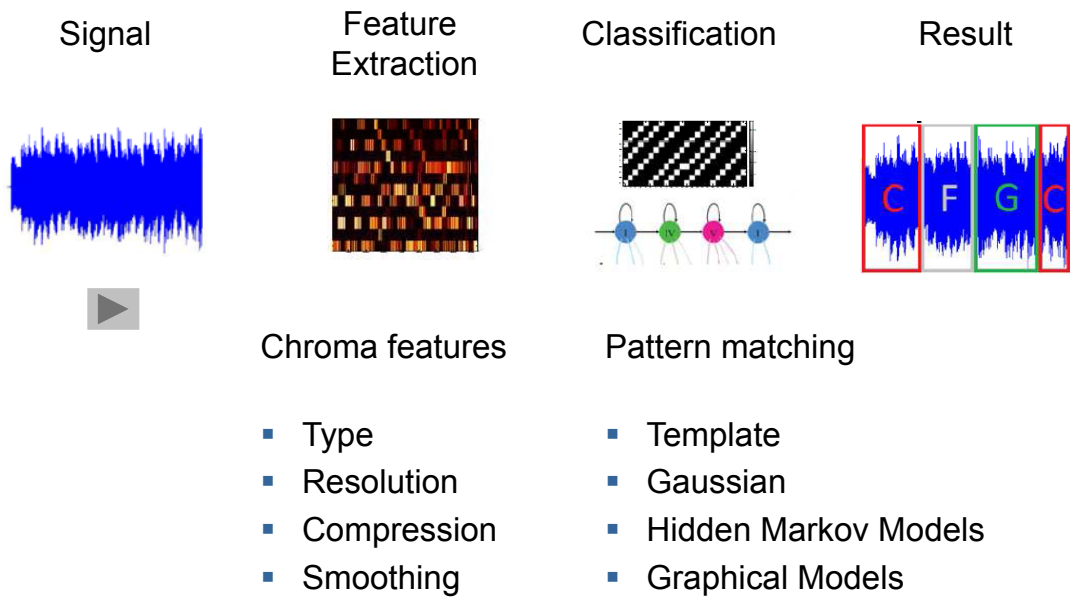
## Chord Recognition

- Development of automatic methods for the harmonic analysis of audio data
- Applications in the field of music information retrieval:
  - music segmentation
  - cover song identification
  - audio matching
  - music structure analysis
  - ...

# Chord Recognition



# Chord Recognition



# Chord Recognition

**Given:** Audio file



**Output:** Segmentation and chord labeling

Johann Pachelbel  
George Winston

Andantino Moderato

Chord labels: C G A:min E:min F C F G C G A:min E:min F C F G C G A:min E:min F C F G

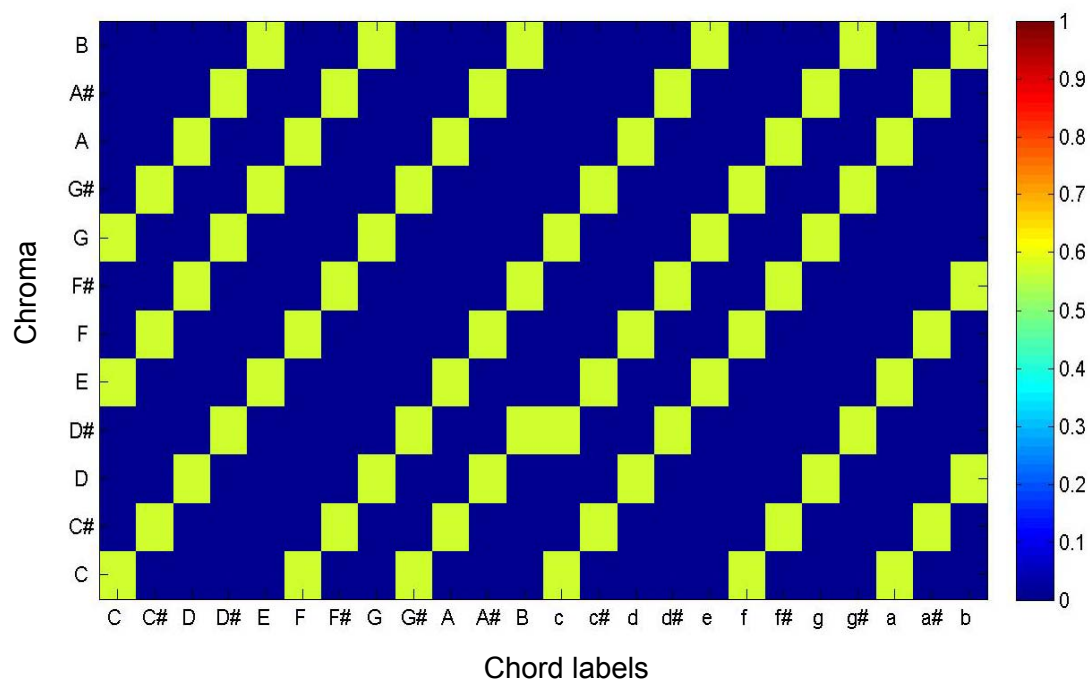
# Baseline Method for Chord Recognition

Chord templates 24 major/minor chords

	C major	C# major	D major	D# major	.....	C minor	C# minor	.....
B	0	0	0	0	.....	0	0	.....
A#	0	0	0	1	.....	0	0	.....
A	0	0	1	0	.....	0	0	.....
G#	0	1	0	0	.....	0	1	.....
G	1	0	0	1	.....	1	0	.....
F#	0	0	1	0	.....	0	0	.....
F	0	1	0	0	.....	0	0	.....
E	1	0	0	0	.....	0	1	.....
D#	0	0	0	1	.....	1	0	.....
D	0	0	1	0	.....	0	0	.....
C#	0	1	0	0	.....	0	1	.....
C	1	0	0	0	.....	1	0	.....

# Baseline Method for Chord Recognition

Chord templates 24 major/minor chords



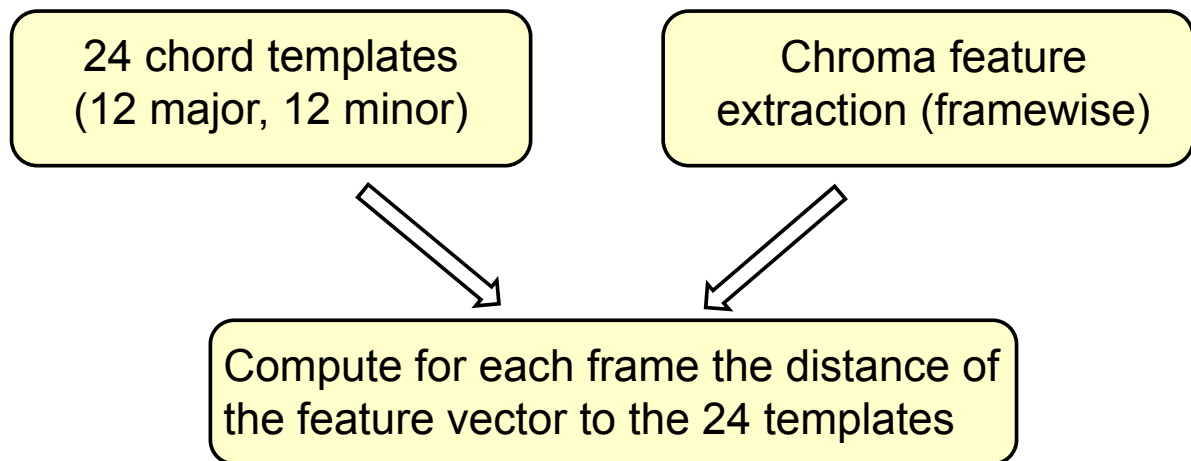
# Baseline Method for Chord Recognition

24 chord templates  
(12 major, 12 minor)

Chroma feature  
extraction (framewise)

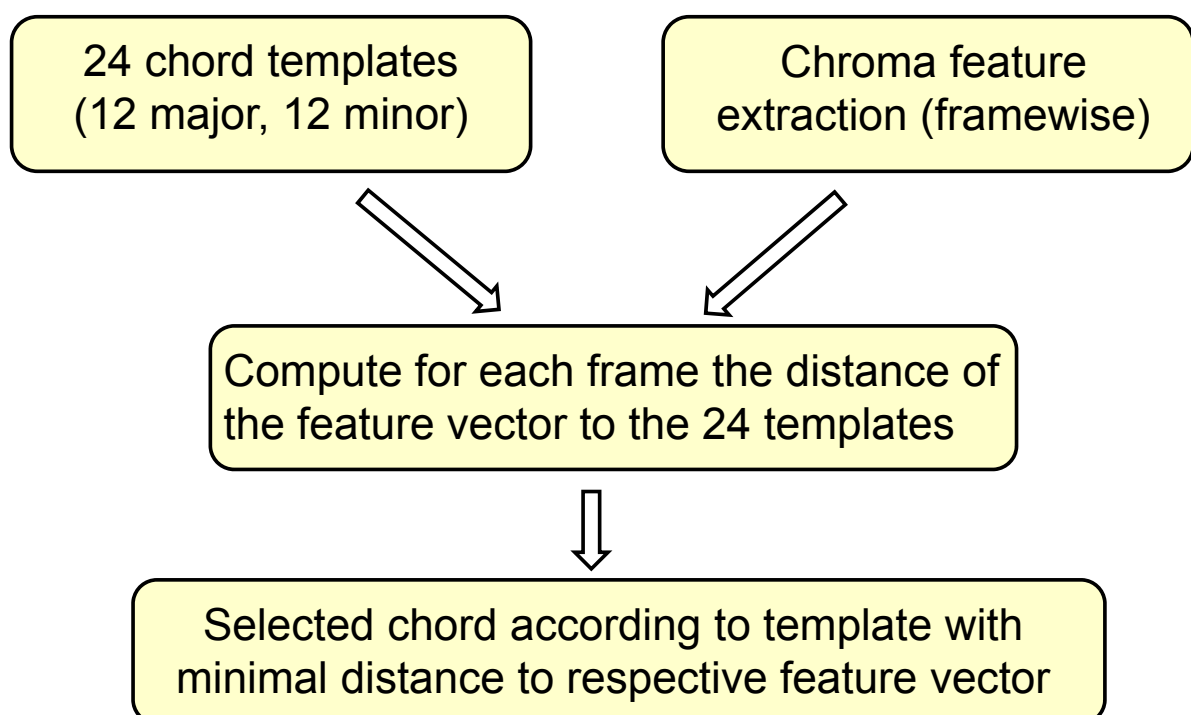
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## Baseline Method for Chord Recognition



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## Baseline Method for Chord Recognition

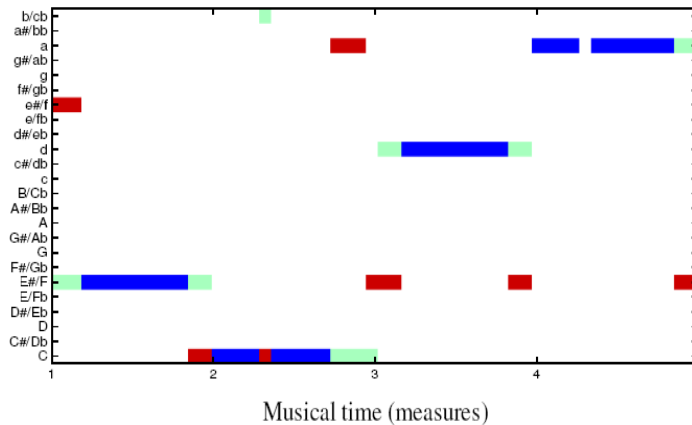




# Problems in Chord Recognition

**Problem: Transitions between subsequent chord**

Example: Chopin Mazurka Op. 68 No.3



- Correct
- False positive
- False negative

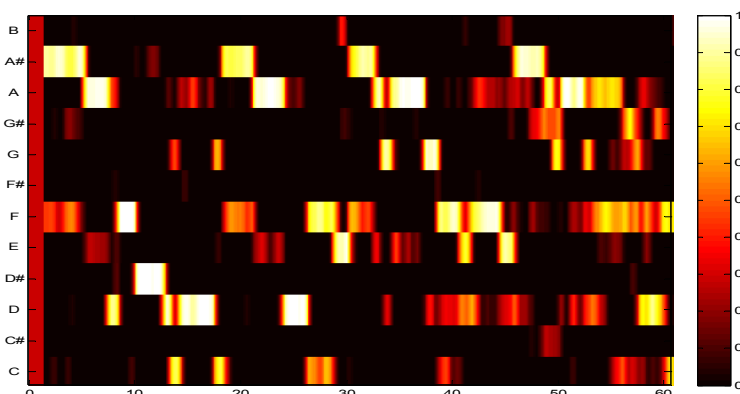
# Problems in Chord Recognition

**Problem: Monophonic musical passages**

Example: Excerpt of Wagner's Meistersinger



## Chromagram



## Problems in Chord Recognition

**Problem: Frame-wise chord analysis may not be meaningful**

Example: Bach: Prelude C major, BWV 846

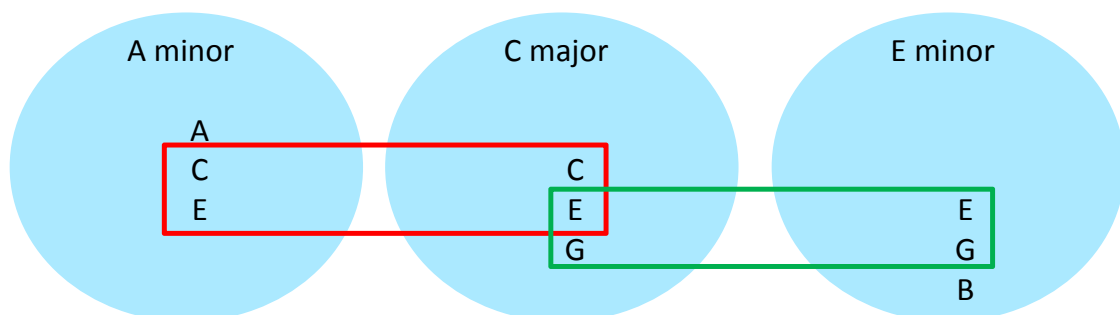


Problem: Broken chords

→ Measure-wise chord analysis necessary

## Problems in Chord Recognition

**Problem: Ambiguity of chords**



# Problems in Chord Recognition

**Problem: Reduction to the 24 major/minor chords makes the recognition of more complex chords difficult/impossible!**

Example: Prelude C major, BWV 846, mm.19-25



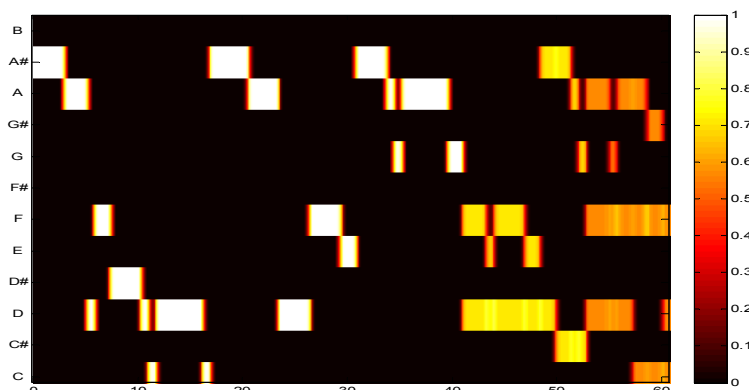
# Problems in Chord Recognition

**Problem: Tuning problems**

Example: Excerpt of Wagner's Meistersinger



Chromagram (from MIDI)



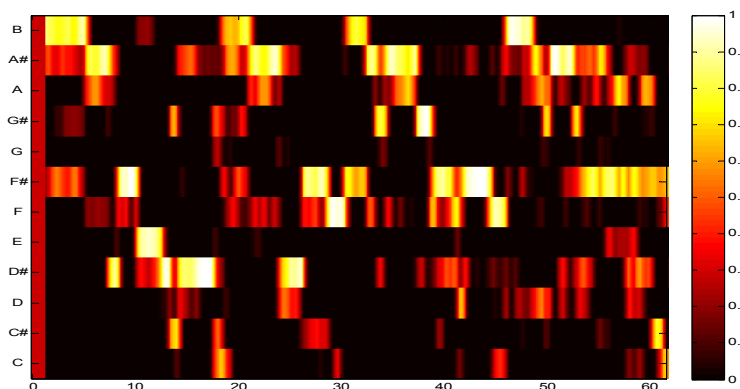
# Problems in Chord Recognition

**Problem: Tuning problems**

Example: Excerpt of Wagner's Meistersinger



Chromagram (from MIDI)



**Problem:**  
Audio is tuned more than half a semi-tone upwards

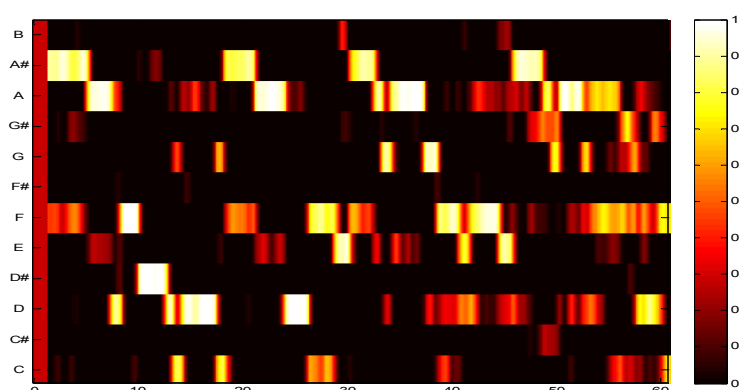
# Problems in Chord Recognition

**Problem: Tuning problems**

Example: Excerpt of Wagner's Meistersinger



Chromagram (from MIDI)



**Problem:**  
Audio is tuned more than half a semi-tone upwards

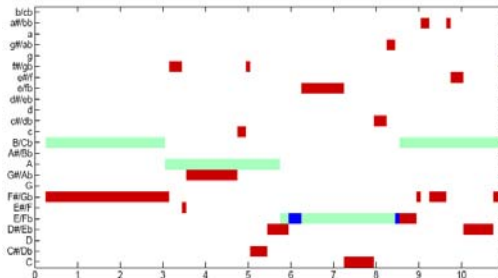
**Solution:**  
Adjust frequency binning when computing pitch features.




# Problems in Chord Recognition

## Problem: Tuning problems

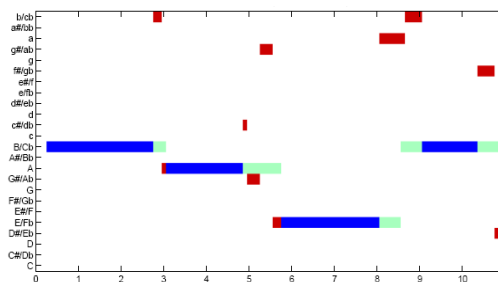
Example: The Beatles "Lovely Rita" 

Without tuning

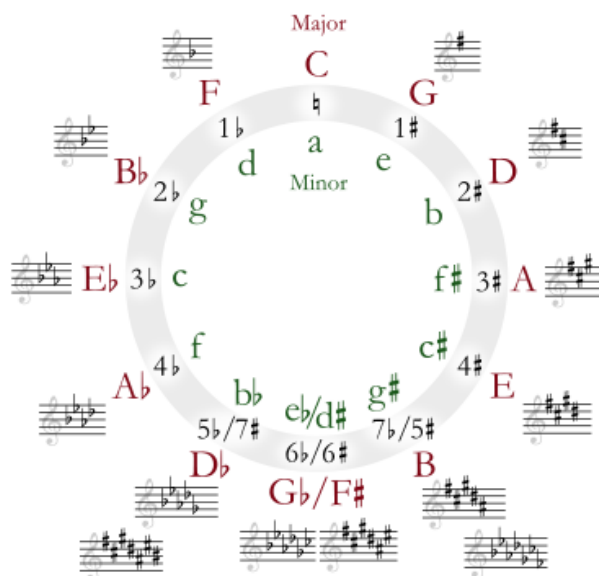


-  Correct
-  False positive
-  False negative

With tuning

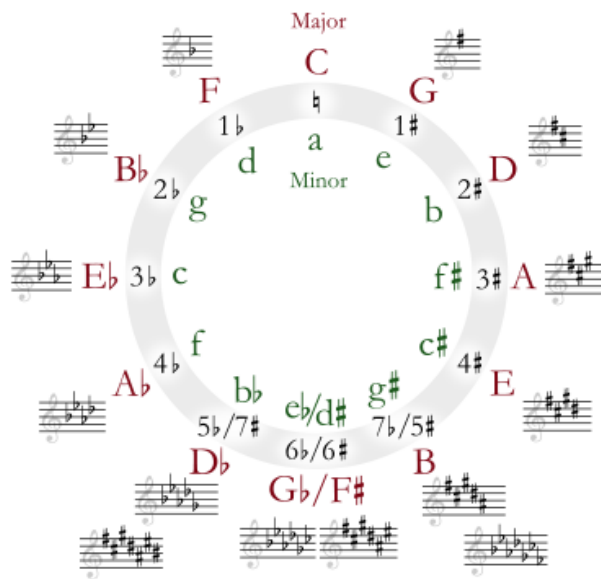


# Key Relations: Circle of Fifths



From [http://en.wikipedia.org/wiki/Circle\\_of\\_fifths](http://en.wikipedia.org/wiki/Circle_of_fifths)

# Key Relations: Circle of Fifths



Observation:

For tonality reasons, some chord progressions are more likely than others.

Idea:

Usage of Hidden Markov Models (HMMs) to model chord dependencies

From [http://en.wikipedia.org/wiki/Circle\\_of\\_fifths](http://en.wikipedia.org/wiki/Circle_of_fifths)

# Markov Models

Description of certain stochastic processes



Andrei Markov  
(Wikipedia)

# Markov Models

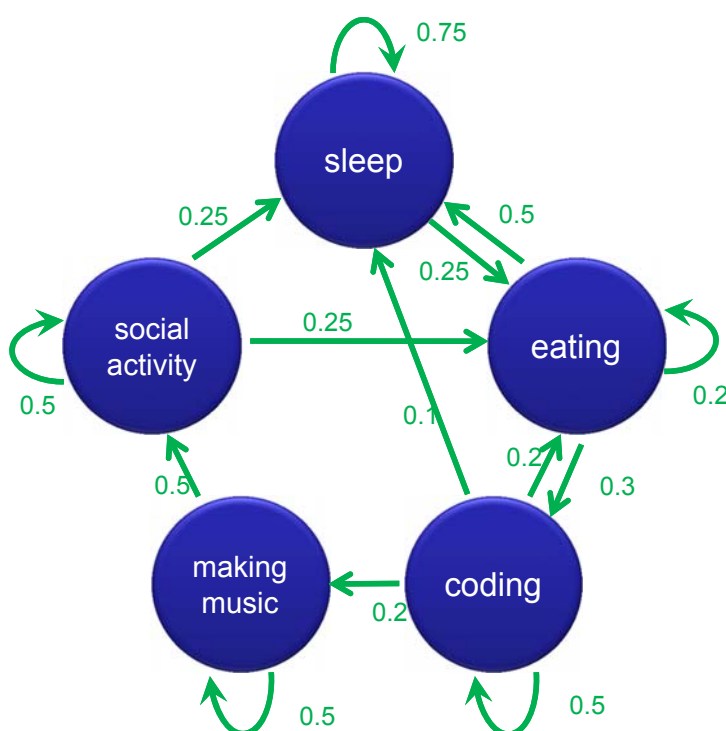
Description of certain stochastic processes



Andrei Markov  
(Wikipedia)

- Processes over discrete time
- Sequence of random variables  $X_1, X_2, \dots$
- Process has to follow Markov property:
  - no “memory”, only current state “known”
  - “future” depends only on “present”, not on “past”
  - $P(X_{n+1} = x \mid X_n = y) = P(X_{n+1} = x \mid X_n = y, X_{n-1} = y_2, \dots)$

# Hidden Markov Models



$$G = (S, E, P)$$

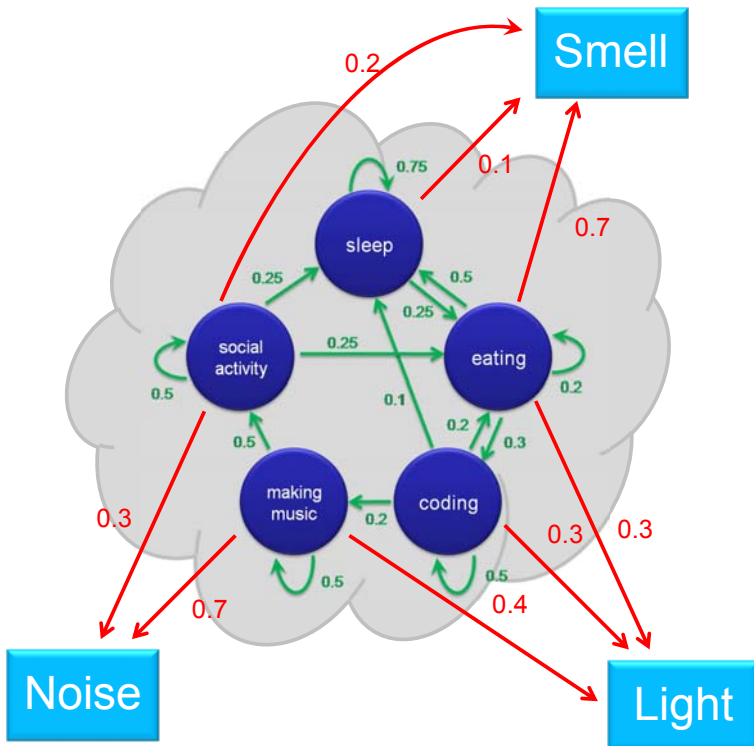
S: States

E: Transitions

P: Transition probabilities

Note: For each state, the sum of outgoing transition probabilities is equal to one.

# Hidden Markov Models



$$G = (S, P, V, B)$$

S: States

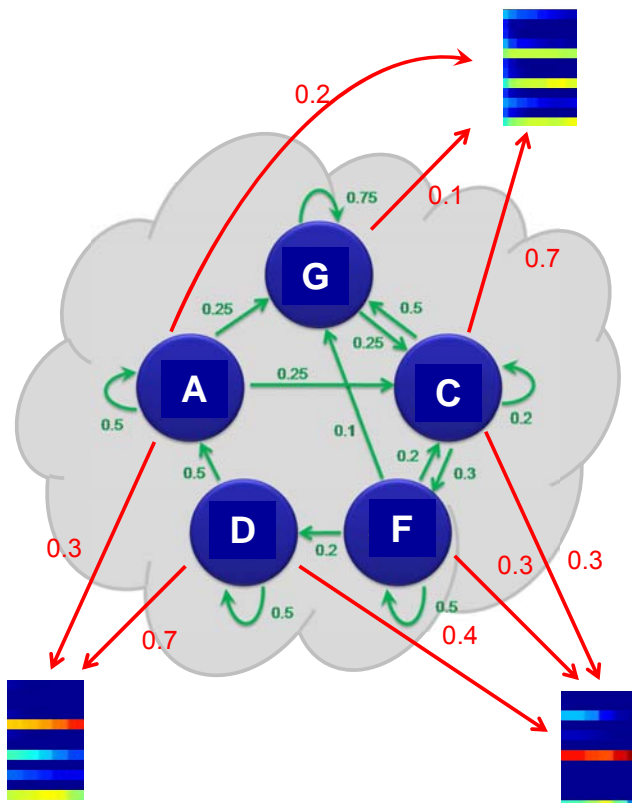
P: Transition probabilities

V: Observations

B: Emission probabilities

[Radu Curticapean]

# Hidden Markov Models



$$G = (S, P, V, B)$$

S: States

P: Transition probabilities

V: Observations

B: Emission probabilities



# Hidden Markov Models

$$G = (S, P, V, B)$$

24 major/minor chords

S: States

Probabilities for having a transition from one chord to another chord

P: Transition probabilities

Chroma vectors

V: Observations

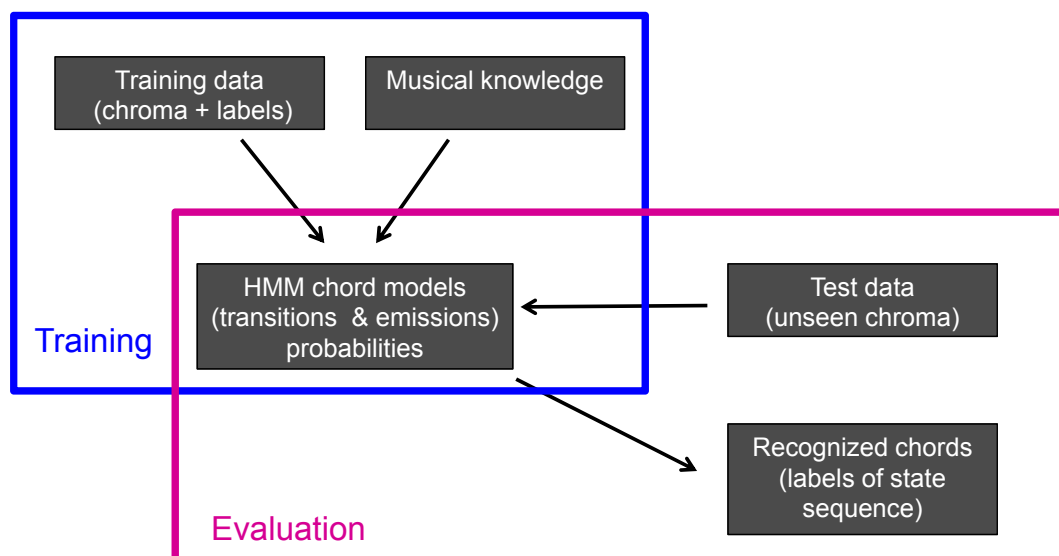
Probability for a chord model to produce a chroma distribution

B: Emission probabilities

# Hidden Markov Models

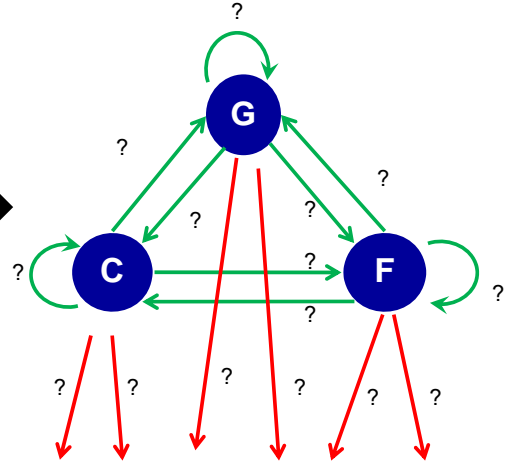
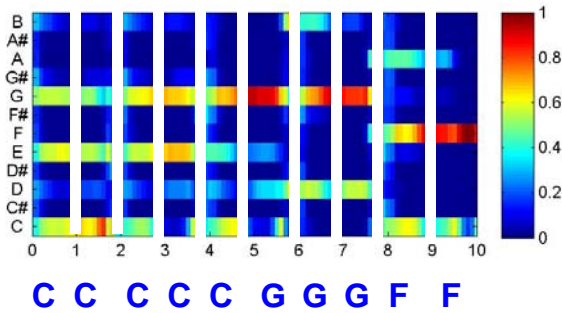
Two computational problems

1. **Training:** learn model parameters (Baum-Welch Algorithm)
2. **Evaluation:** find optimal state sequence (Viterbi Algorithm)



# Hidden Markov Models

## Training



Input:

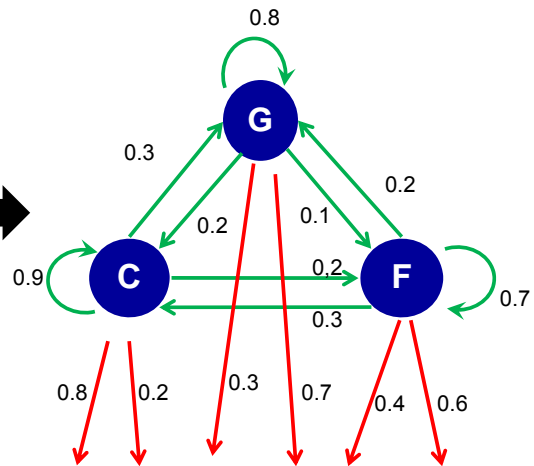
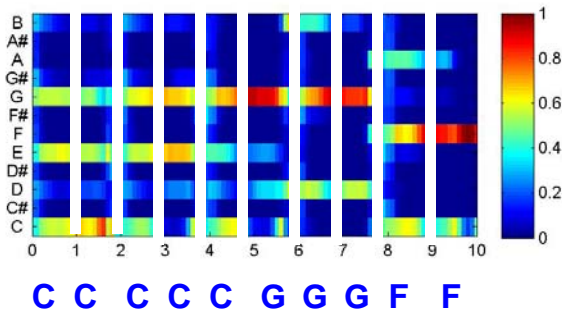
Sequence of features (observations)  
Corresponding ground truth chord labels

Output:

Emission probabilities  
Transition probabilities

# Hidden Markov Models

## Training



Input:

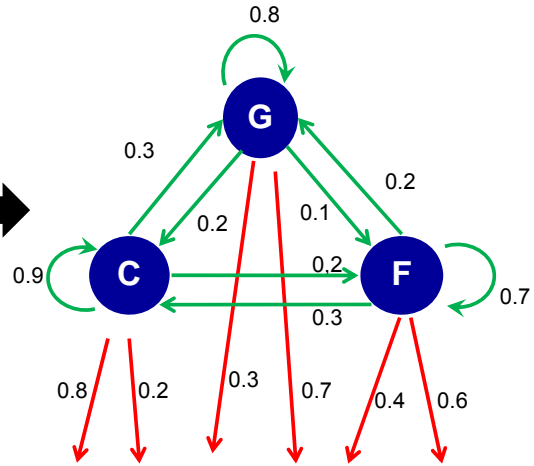
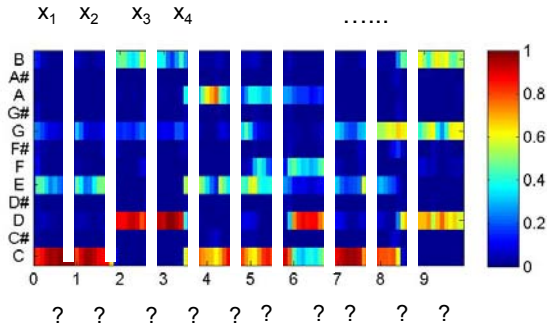
Sequence of features (observations)  
Corresponding ground truth chord labels

Output:

Emission probabilities  
Transition probabilities

# Hidden Markov Models

## Evaluation



Input:

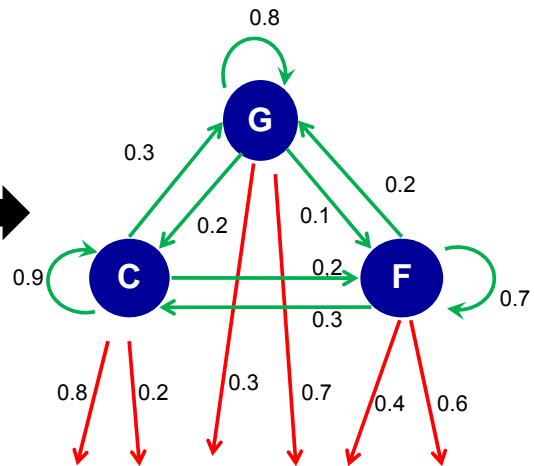
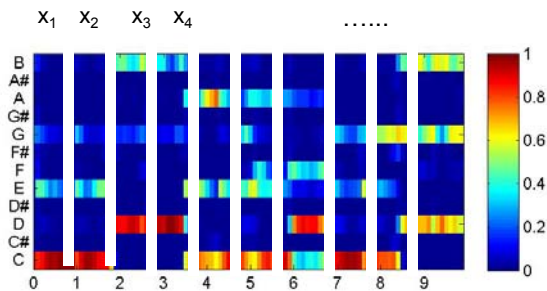
- Sequence of features
- Emission probabilities
- Transition probabilities

Output:

Optimal state sequence (estimated chord progression)

# Hidden Markov Models

## Evaluation



Input:

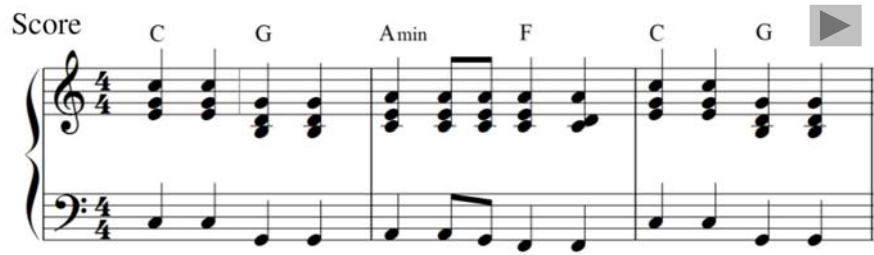
- Sequence of features
- Emission probabilities
- Transition probabilities

Output:

Optimal state sequence (estimated chord progression)

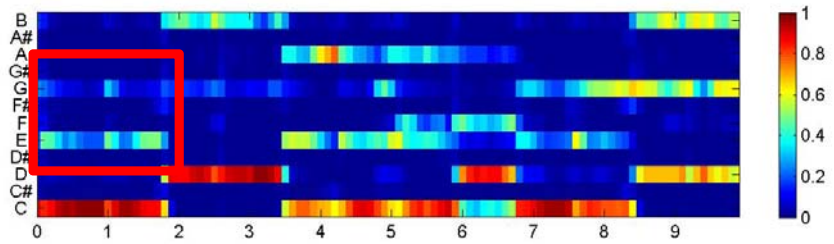
C C G G F F F C C

# Importance of Chroma Feature Variant



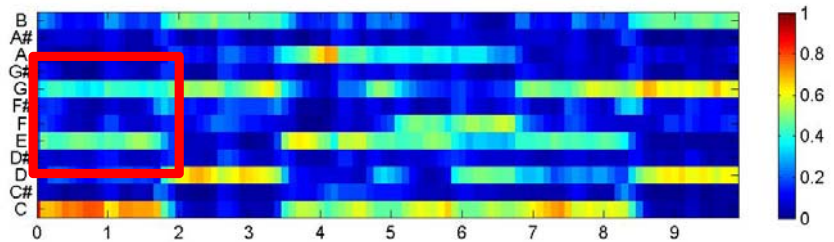
CP

Normalized  
chromagram

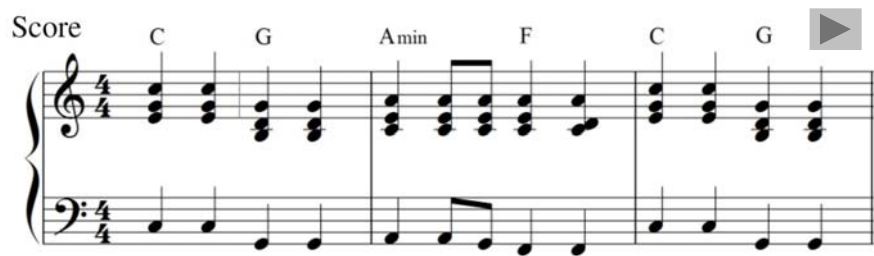


CLP

Logarithmic  
compression

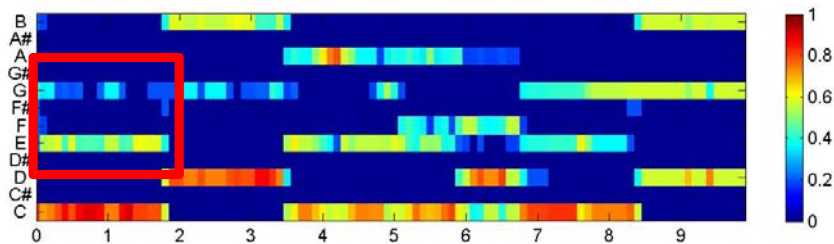


# Importance of Chroma Feature Variant



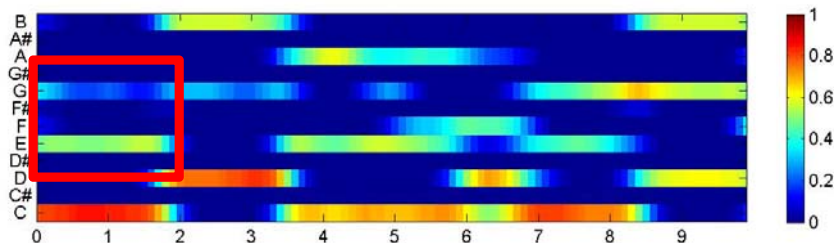
CENS[1]

Quantized  
chromagram

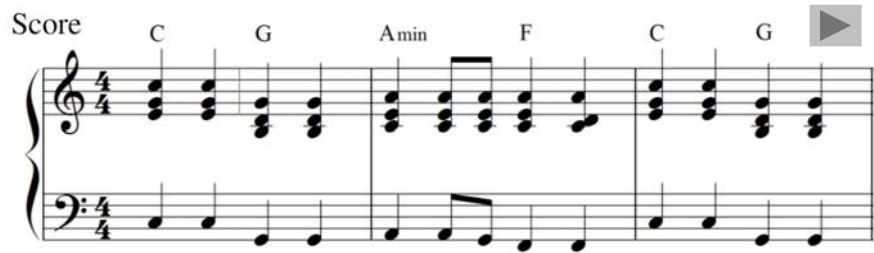


CENS[11]

Temporal  
smoothing

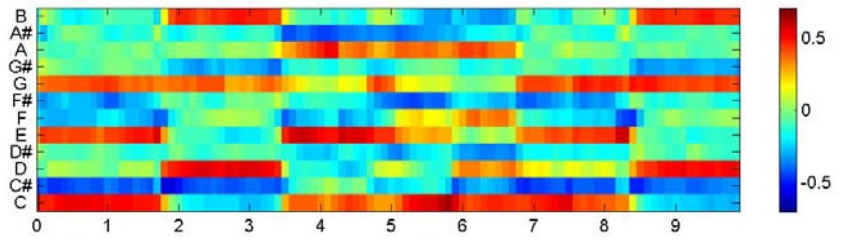


# Importance of Chroma Feature Variant



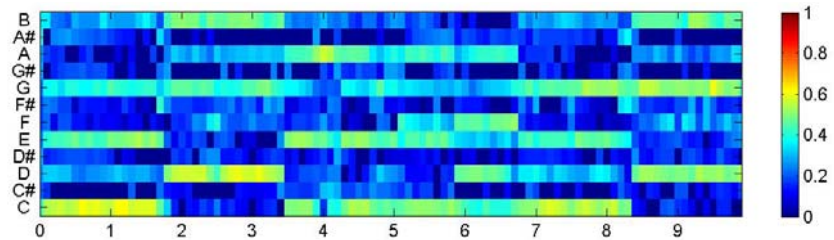
CRP

Boosting timbre invariance



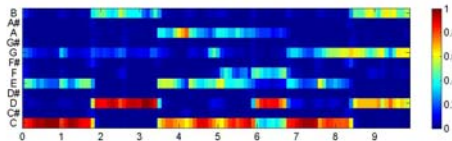
CISP

Instantaneous frequency

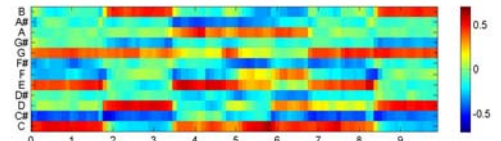


# Importance of Chroma Feature Variant

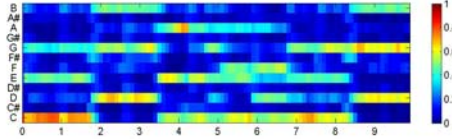
CP



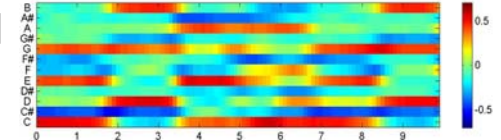
CRP[1]



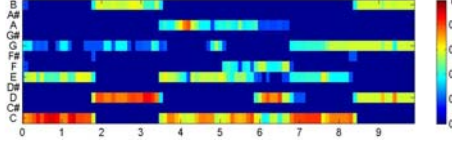
CLP



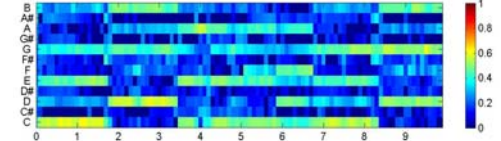
CRP[11]



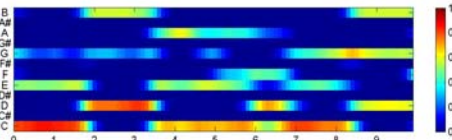
CENS[1]



CISP



CENS[11]



And many more chroma variants!

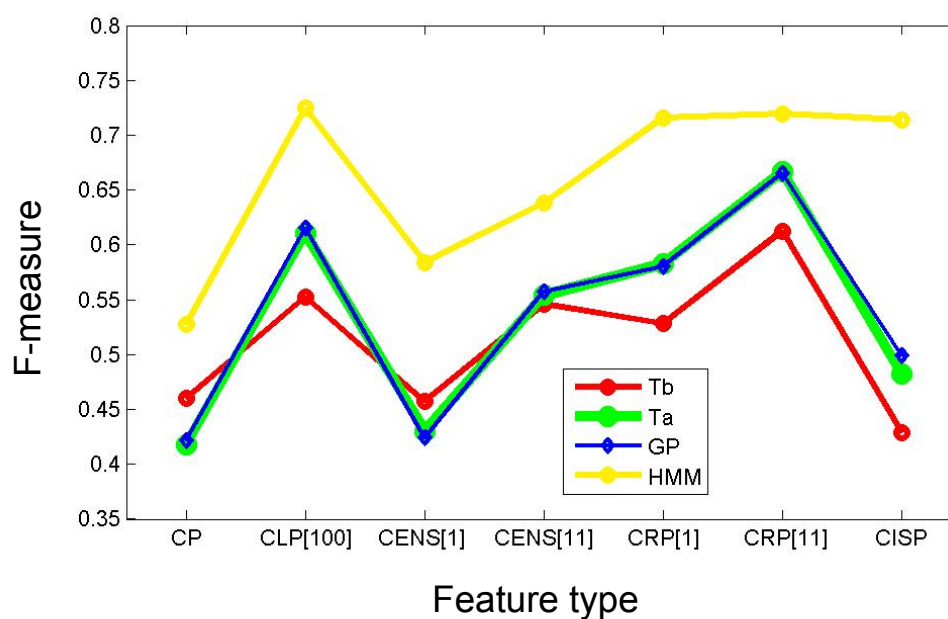
# Importance of Chroma Feature Variant

## Experiment

- Beatles dataset
- Three-fold cross validation
- Measurement: F-measure
- Framewise evaluation, each frame = 100 ms
- 12 major and 12 minor triads

# Importance of Chroma Feature Variant

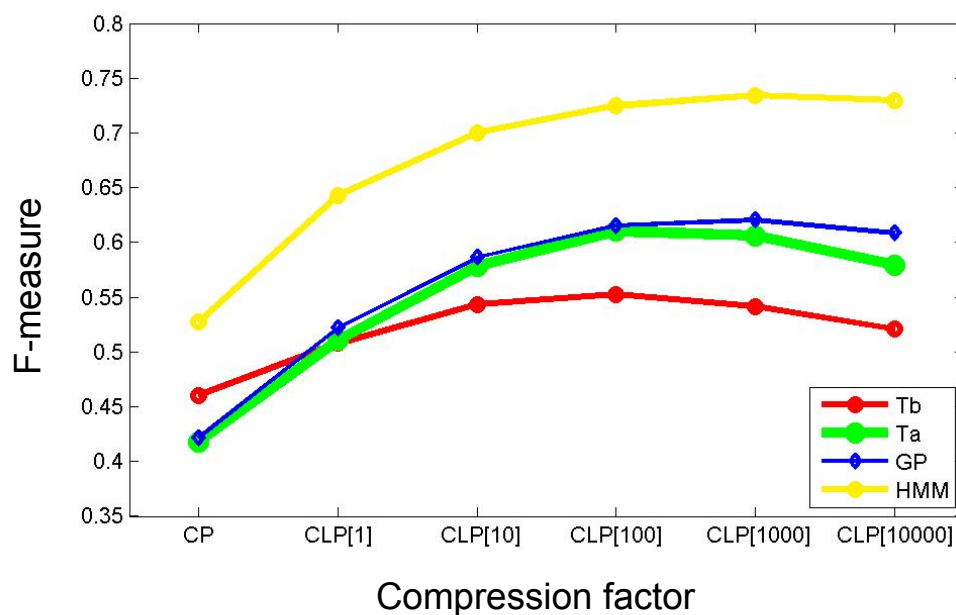
## Dependency on feature type





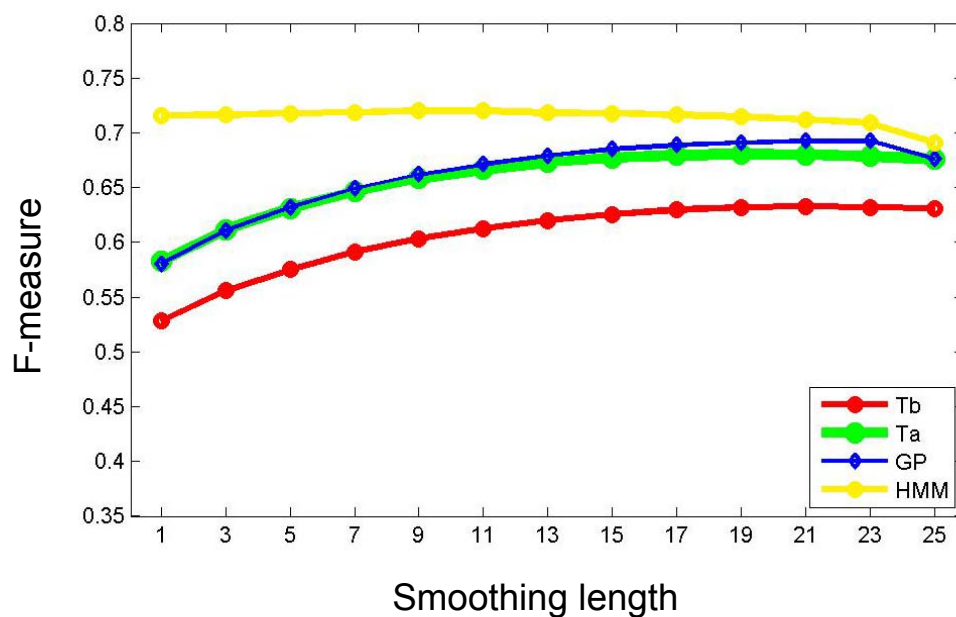
# Importance of Chroma Feature Variant

Dependency on logarithmic compression



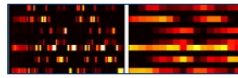
# Importance of Chroma Feature Variant

Dependency on smoothing (using CRP features)



# Chroma Toolbox

## Chroma Toolbox: Pitch, Chroma, CENS, CRP



Chroma Toolbox
Feature description
MATLAB Code
References
Links
MPI Informatik
Bonn University
ISMIR

**Chroma Toolbox: Pitch, Chroma, CENS, CRP**

The **Chroma Toolbox** has been developed by [Meinard Müller](#) and his collaborators from the research group headed by [Michael Clausen](#). It contains MATLAB implementations for extracting various types of novel pitch-based and chroma-based audio features. The MATLAB implementations provided on this website are free for use in non-commercial research projects worldwide. If you publish results obtained using these implementations, please cite the references below, [\[1\]](#), [\[2\]](#), [\[3\]](#), [\[4\]](#).

**Description of Pitch, Chroma, CENS, CRP features**

Chroma-based audio features have turned out to be a powerful tool for various analysis tasks in [Music Information Retrieval](#) including task such as chord labeling, music summarization, structure analysis, music synchronization and audio alignment. A 12-dimensional chroma feature encodes the short-time energy distribution of the underlying music signals over the twelve chroma bands, which correspond to the twelve traditional pitch classes of the equal-tempered scale encoded by the attributes C, C#, D, D#, ..., B. Such features strongly correlate to the harmonic progression of the music signal, often prominent in Western music. By identifying spectral components that differ by a musical octave, chroma features possess a significant degree of robustness to changes in timbre and instrumentation.

- Freely available Matlab toolbox
- Feature types: Pitch, Chroma, CENS, CRP
- <http://www.mpi-inf.mpg.de/resources/MIR/chromatoolbox/>

## Cross-Version Analysis

### General Procedure

- Conduct **analysis** for **multiple versions** of the **same object**
  - **Harmonic analysis**
  - **Different music recordings**
  - **Same piece of music**
- **Relate** the versions (using a **reference**)
  - **Music synchronization**
  - **Musical score**
- Compare analysis results across different versions
- Look for consistencies and inconsistencies

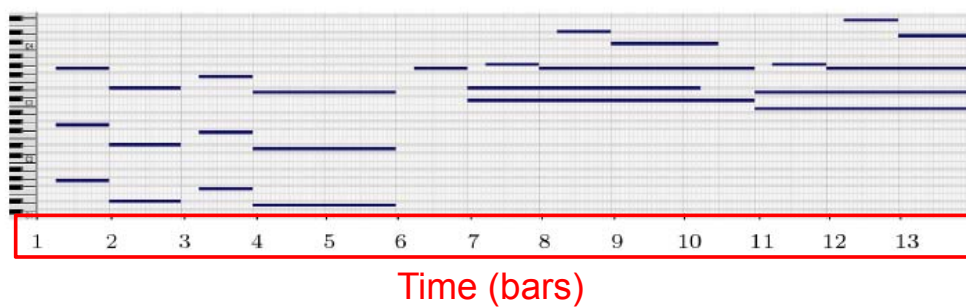


# Barwise Synchronization

A musical score in 2/4 time, key of B-flat major, consisting of 13 bars. The score is divided into two systems. The first system contains bars 1 through 6, and the second system contains bars 7 through 13. Each bar is numbered in a red box above it. The first system starts with a fortissimo (*ff*) dynamic and ends with a piano (*p*) dynamic. The second system includes markings for *rit.* and *\*.* under bars 9 and 11. The notation includes various rhythmic patterns, rests, and articulation marks.

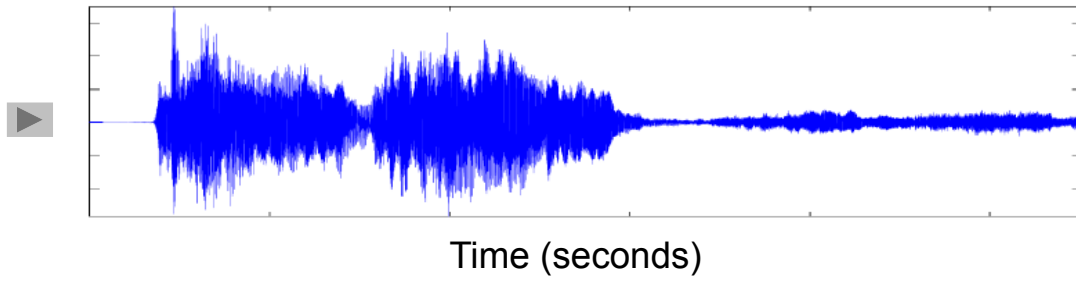
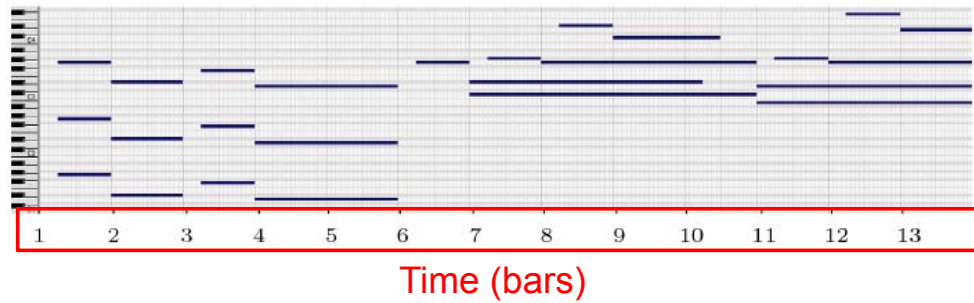
# Barwise Synchronization

MIDI representation with bar information



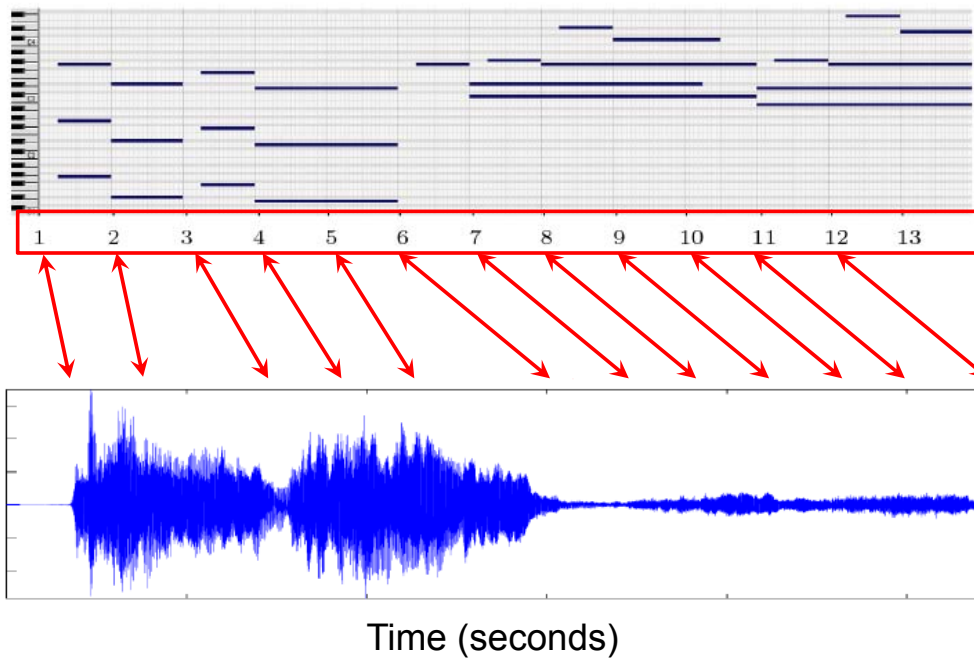
# Barwise Synchronization

MIDI representation with bar information



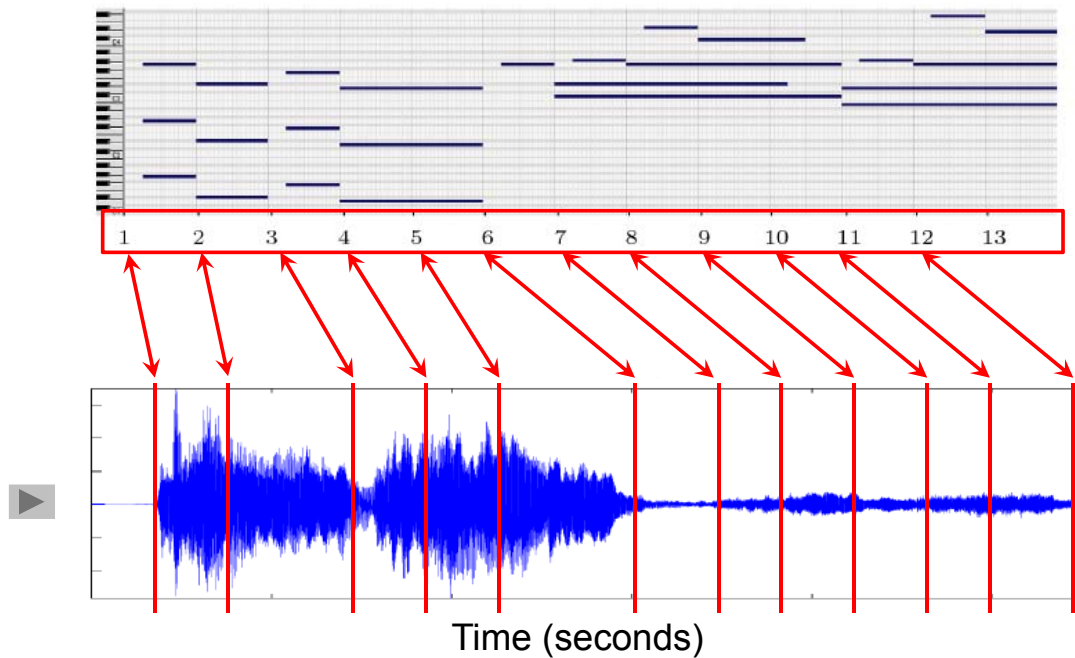
# Barwise Synchronization

Music synchronization



# Barwise Synchronization

Transfer bar information to audio domain

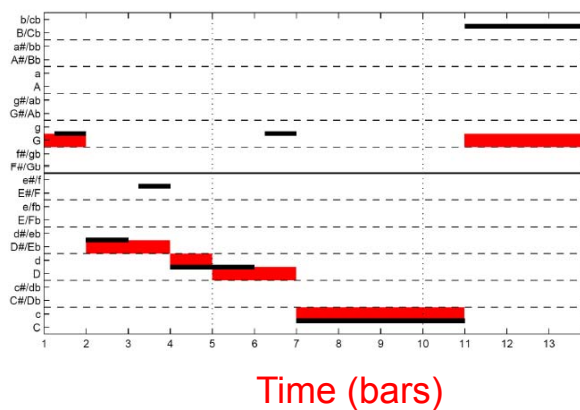
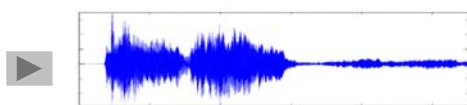


# Cross-Version Harmonic Analysis



Chord recognition result

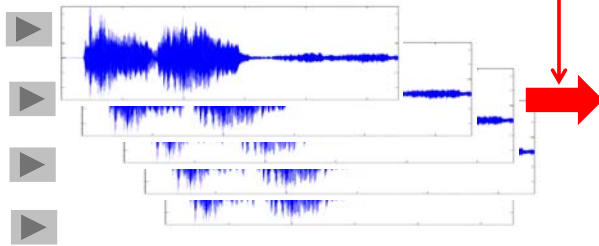
Barwise presentation of analysis results is of great benefit!



Time (seconds)

Time (bars)

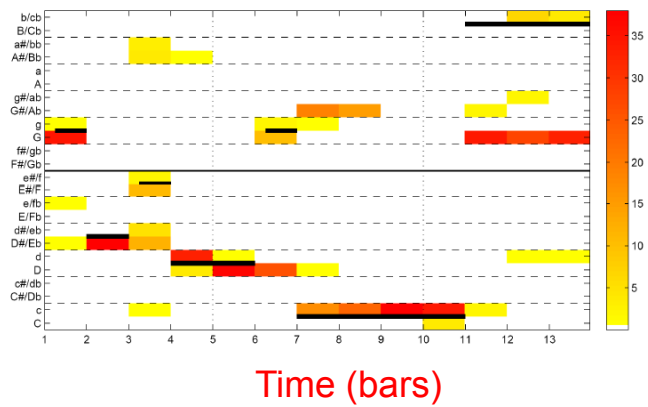
# Cross-Version Harmonic Analysis



Time (seconds)

Chord recognition result

Barwise overlay across different music recordings



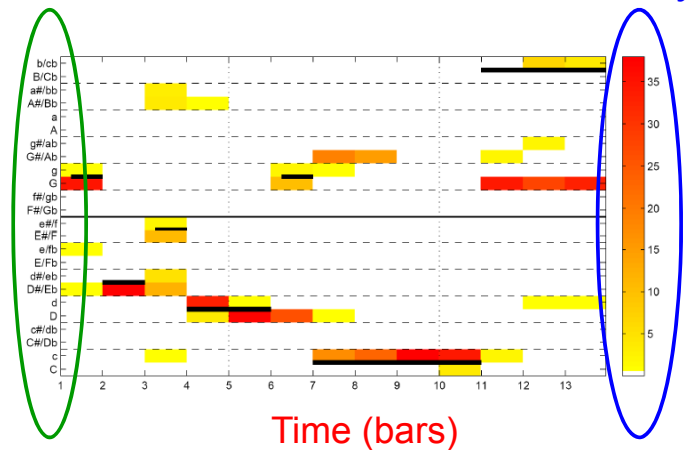
# Cross-Version Harmonic Analysis



Cross-version chord recognition result

Chord labels

Consistency



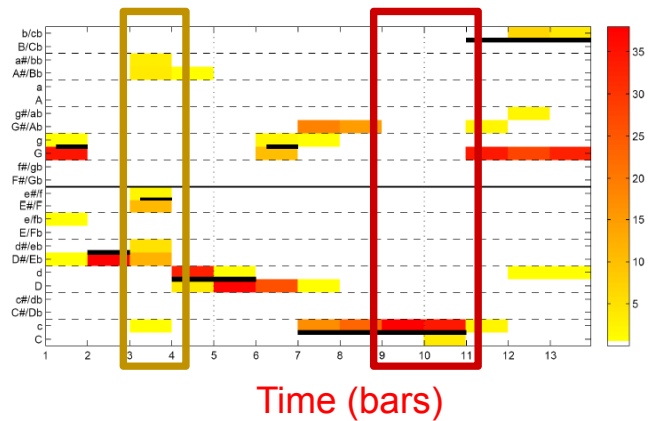
# Cross-Version Harmonic Analysis



Cross-version chord recognition result

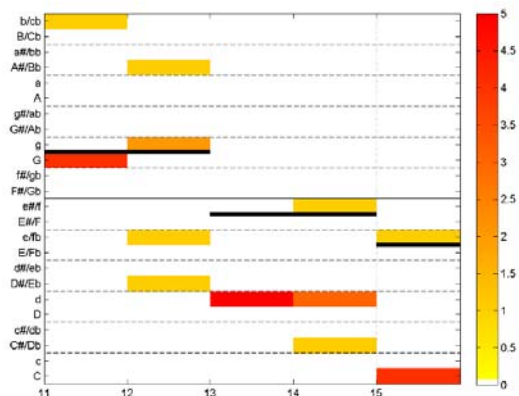
Highly consistent:  
C-minor

Inconsistent:  
F-minor, F-major,  
E<sup>b</sup>-major ... ???



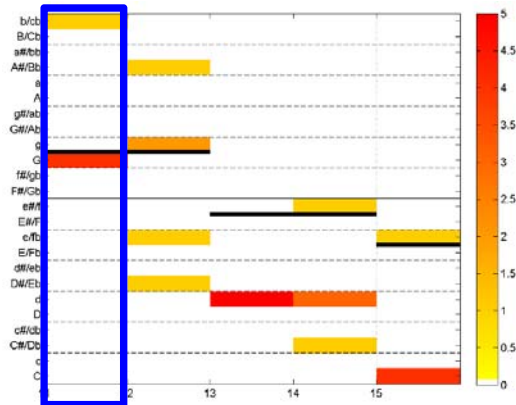
# Cross-Version Visualization

Example: Bach's Prelude BWV 846 in C major (bars 11-15)



# Cross-Version Visualization

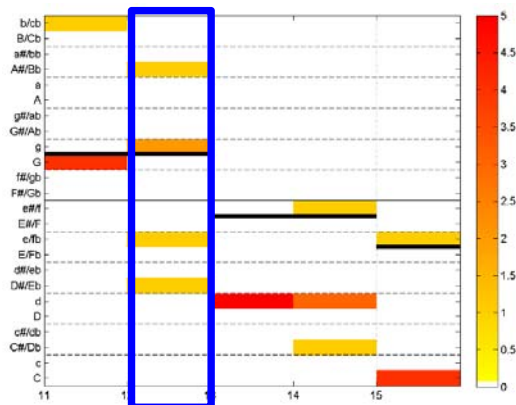
Example: Bach's Prelude BWV 846 in C major (bars 11-15)



Highly consistent: G-major

# Cross-Version Visualization

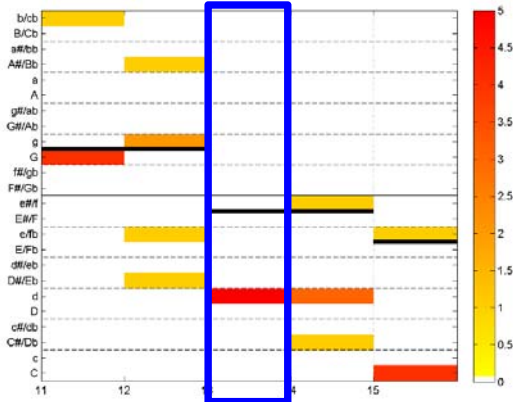
Example: Bach's Prelude BWV 846 in C major (bars 11-15)



Inconsistent!

# Cross-Version Visualization

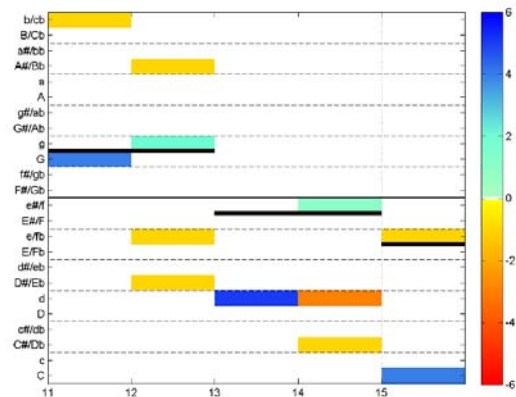
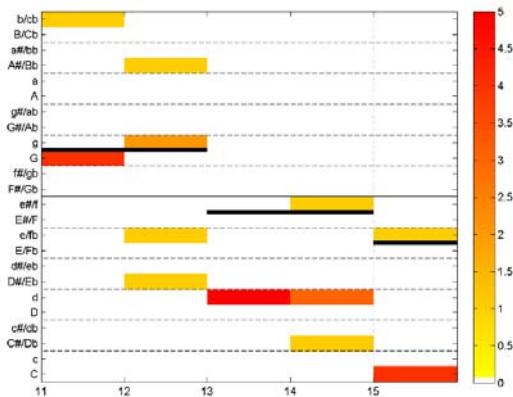
Example: Bach's Prelude BWV 846 in C major (bars 11-15)



Highly consistent: D-minor

# Cross-Version Visualization

Example: Bach's Prelude BWV 846 in C major (bars 11-15)

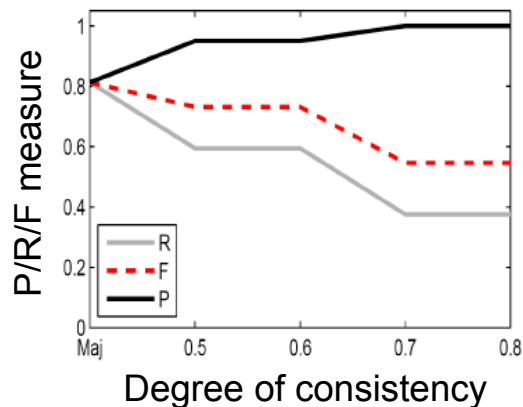


Ground-truth visualization

Convenient tool for manual error analysis and evaluation

## Quantitative Evaluation

Example: Bach's Prelude BWV 846



F-measures for individual recordings:

Min: 0.44

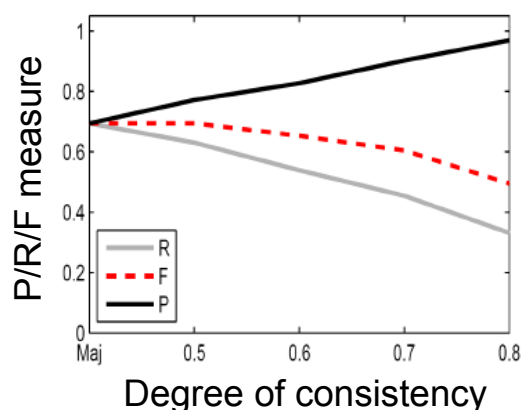
Max: 0.87

Mean: 0.70

- Consistent regions tend to be classified correctly
  - Precision high
  - Recall not too bad
- Indication of harmonically stable, well-defined tonal centers

## Quantitative Evaluation

Example: Beethoven's Fifth



F-measures for individual recordings:

Min: 0.53

Max: 0.83

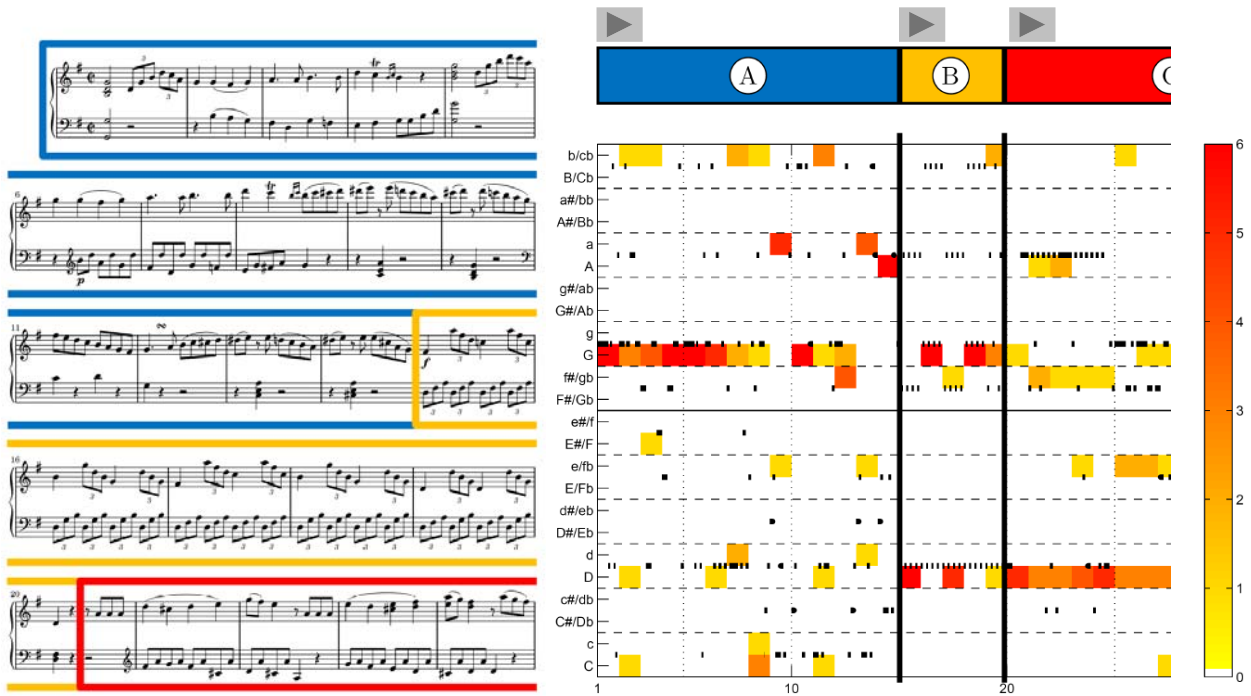
Mean: 0.60

- Consistent regions tend to be classified correctly
  - Precision high
  - Recall not too bad
- Indication of harmonically stable, well-defined tonal centers



# Application: Exploring Harmonic Structures

Example: Beethoven's Piano Sonata Op. 49 No. 2



# Application: Exploring Harmonic Structures

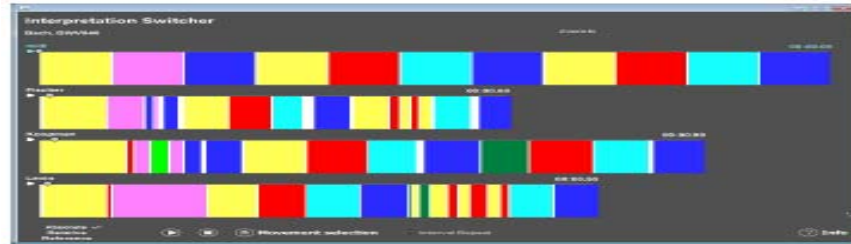
Example: Beethoven's Piano Sonata Op. 49 No. 2



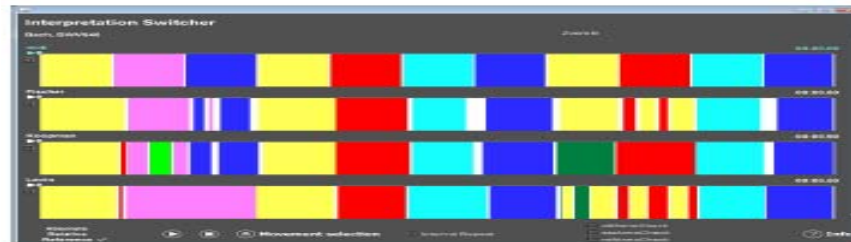
# Interface: Interpretation Switcher

Chord annotations for four versions

Absolute mode



Reference mode



Simultaneous comparison of different version-dependent analysis results (here: chord labels)

## Conclusions & Future Work

- Importance of feature design step
- Cross-version framework
  - Harmonic analysis
  - Tempo analysis
  - Structure analysis
- Musically meaningful timeline in bars → very convenient!
- Stabilization of analysis results
  - Consistencies seem to have musical meaning
  - Which meaning? Tonal centers?
- Towards interdisciplinary research (MIR + musicology)
  - Visualization as meaningful tool in musicology?
  - Helpful for analysis of harmonic relations across entire music corpora?

# Literature

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