Lecture

Music Processing

Music Structure Analysis

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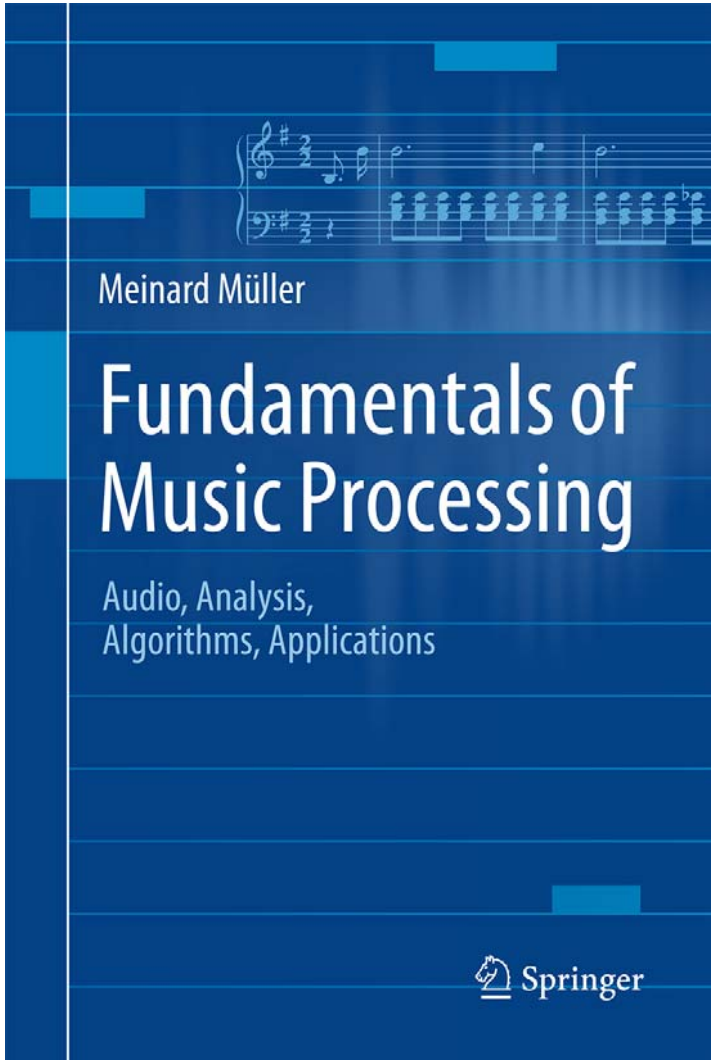
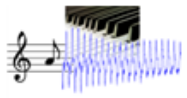
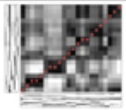
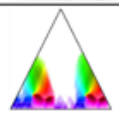
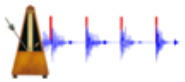
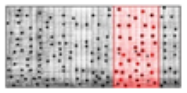
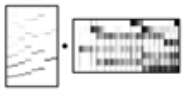
Book: Fundamentals of Music Processing



Meinard Müller
Fundamentals of Music Processing
Audio, Analysis, Algorithms, Applications
483 p., 249 illus., hardcover
ISBN: 978-3-319-21944-8
Springer, 2015

Accompanying website:
www.music-processing.de

Book: Fundamentals of Music Processing

Chapter		Music Processing Scenario
1		Music Represenations
2		Fourier Analysis of Signals
3		Music Synchronization
4		Music Structure Analysis
5		Chord Recognition
6		Tempo and Beat Tracking
7		Content-Based Audio Retrieval
8		Musically Informed Audio Decomposition

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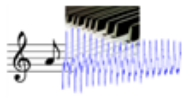
1		Music Represenations
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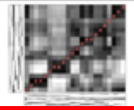
3		Music Synchronization
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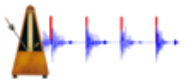
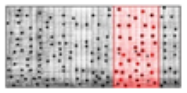
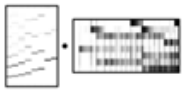
6		Tempo and Beat Tracking
7		Content-Based Audio Retrieval
8		Musically Informed Audio Decomposition

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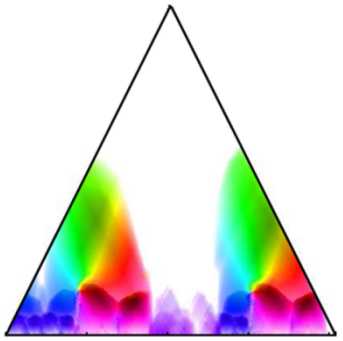
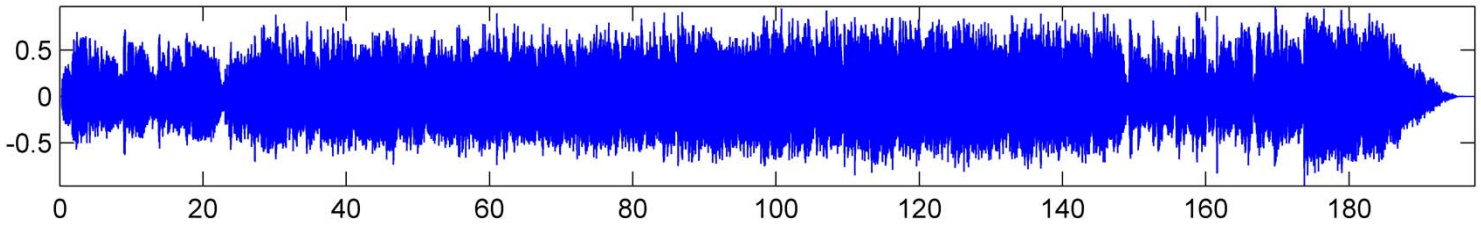
Chapter 4: Music Structure Analysis



In Chapter 4, we address a central and well-researched area within MIR known as music structure analysis. Given a music recording, the objective is to identify important structural elements and to temporally segment the recording according to these elements. Within this scenario, we discuss fundamental segmentation principles based on repetitions, homogeneity, and novelty—principles that also apply to other types of multimedia beyond music. As an important technical tool, we study in detail the concept of self-similarity matrices and discuss their structural properties. Finally, we briefly touch the topic of evaluation, introducing the notions of precision, recall, and F-measure.

Music Structure Analysis

Example: Zager & Evans “In The Year 2525”



Music Structure Analysis

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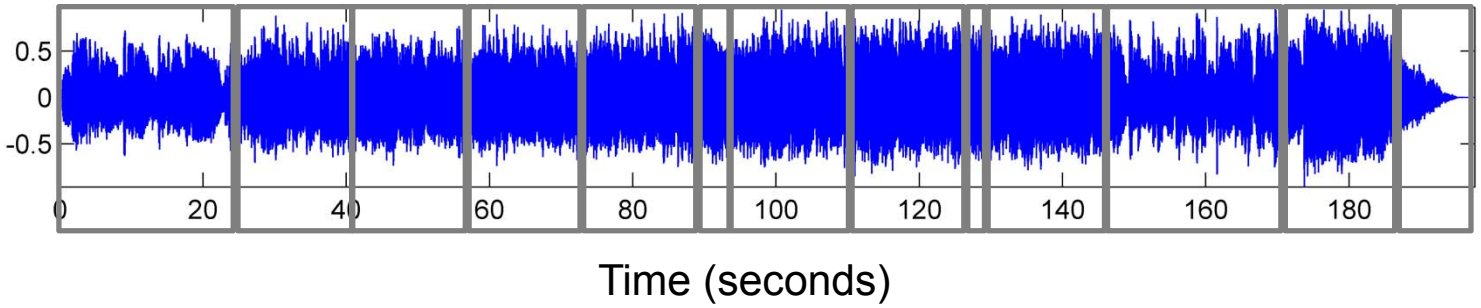

Music Structure Analysis

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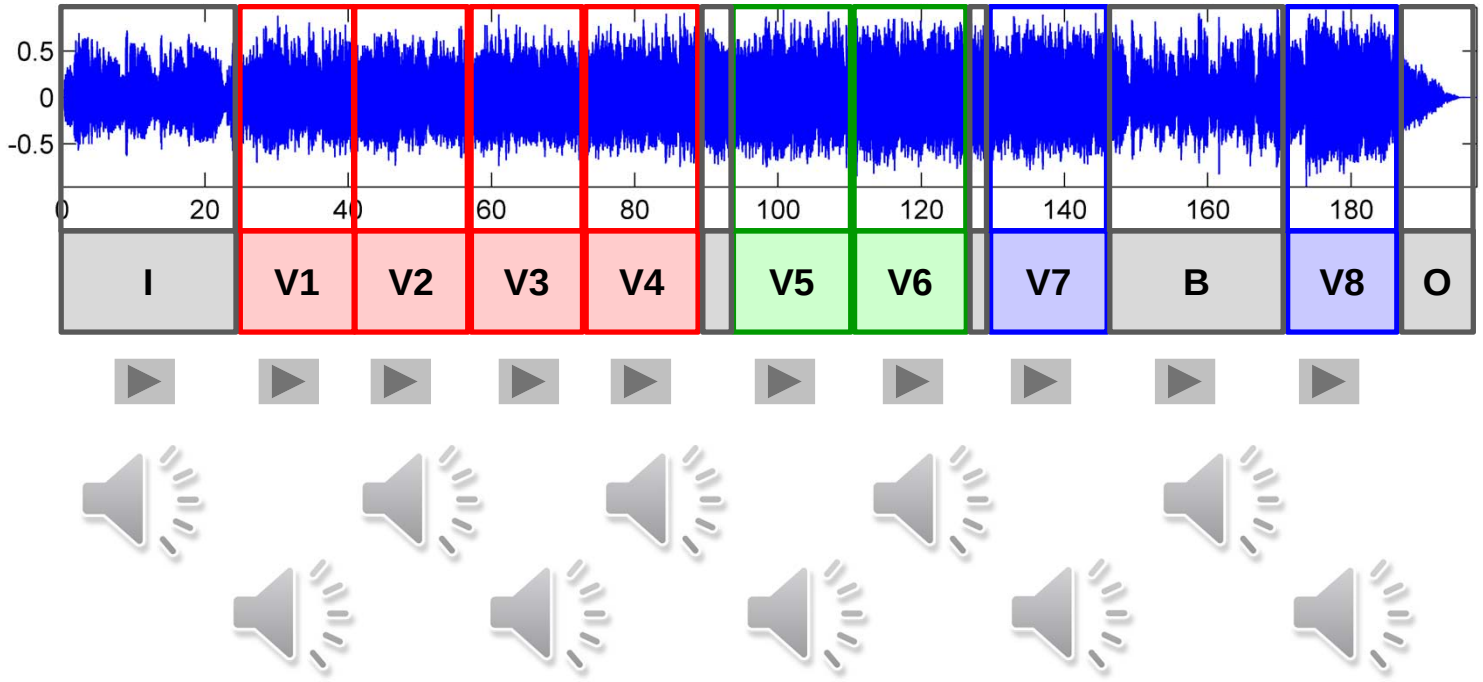
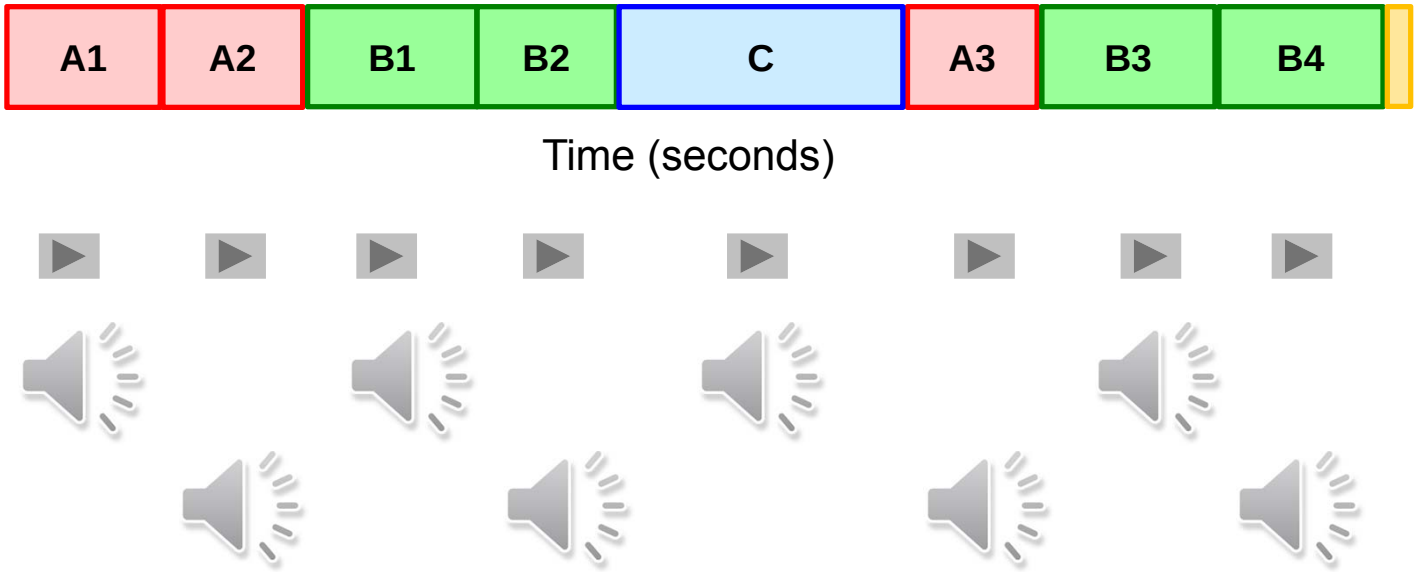


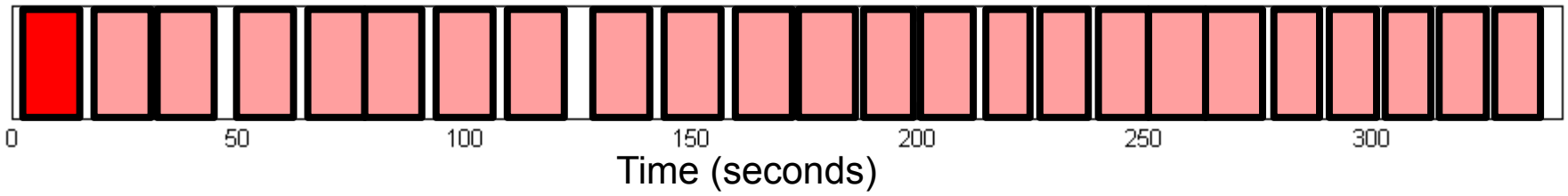
Music Structure Analysis

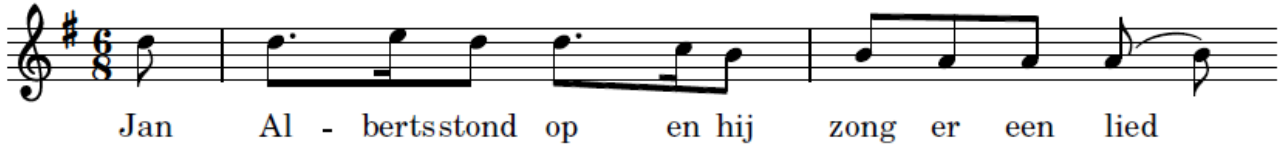
Example: Brahms Hungarian Dance No. 5 (Ormandy)



Music Structure Analysis

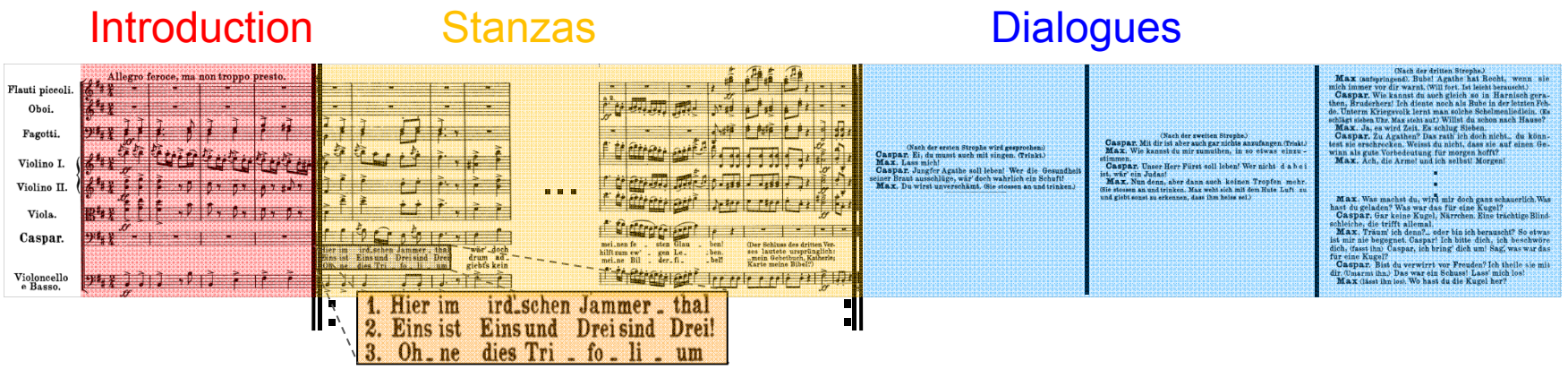
Example: Folk Song Field Recording
(Nederlandse Liederenbank)

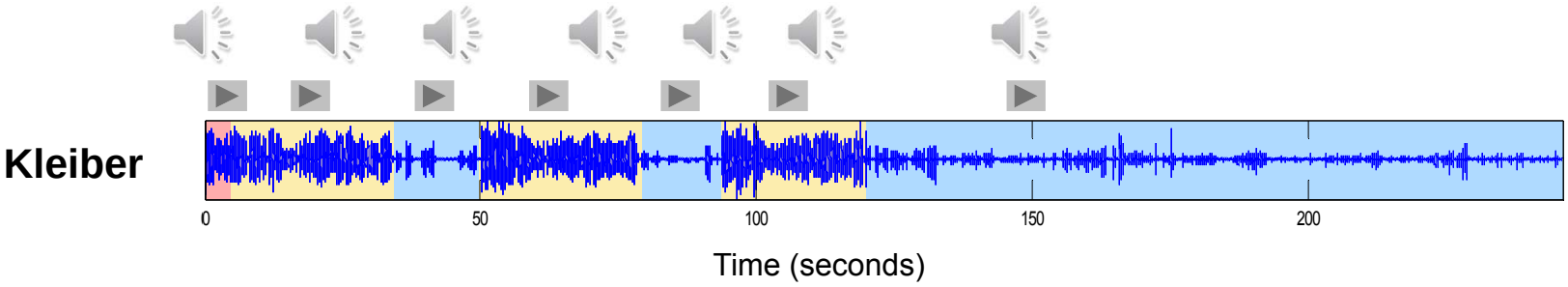


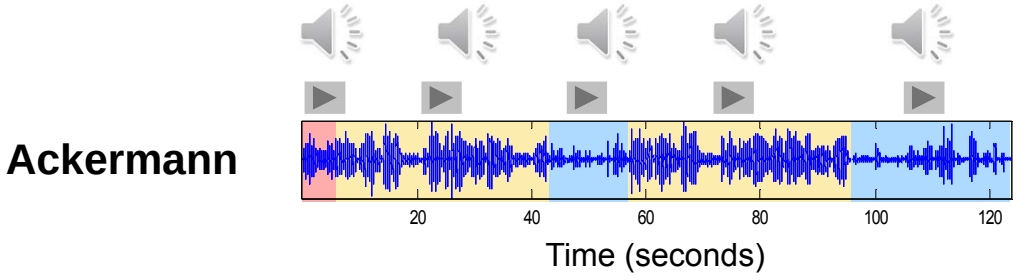


Music Structure Analysis

Example: Weber, Song (No. 4) from “Der Freischütz”







Music Structure Analysis

General goal: Divide an audio recording into temporal segments corresponding to musical parts and group these segments into musically meaningful categories.

Examples:

- Stanzas of a folk song
- Intro, verse, chorus, bridge, outro sections of a pop song
- Exposition, development, recapitulation, coda of a sonata
- Musical form ABACADA … of a rondo

Music Structure Analysis

General goal: Divide an audio recording into temporal segments corresponding to musical parts and group these segments into musically meaningful categories.

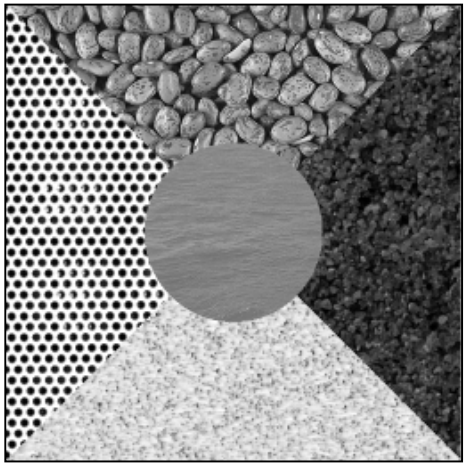
Challenge: There are many different principles for creating relationships that form the basis for the musical structure.

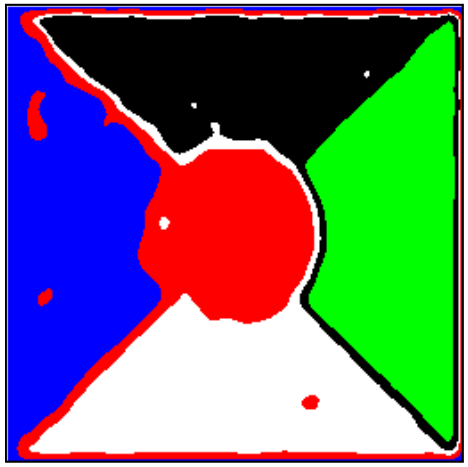
- Homogeneity: Consistency in tempo, instrumentation, key, …
- Novelty: Sudden changes, surprising elements …
- Repetition: Repeating themes, motives, rhythmic patterns,…

Music Structure Analysis

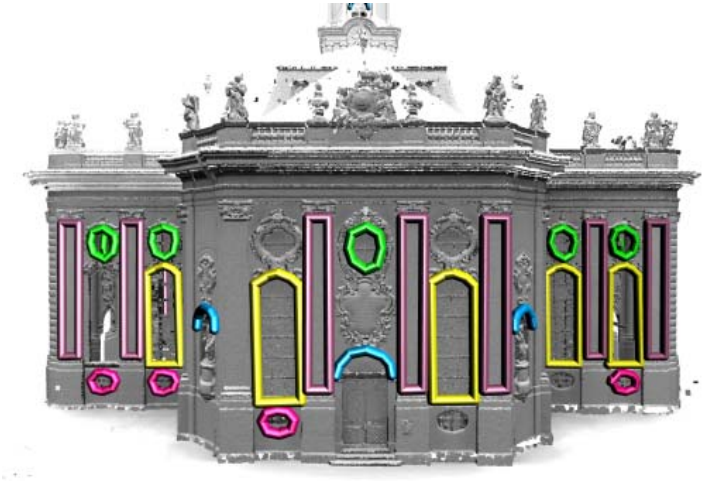
Novelty

Homogeneity





Repetition



Overview

- Introduction
- Feature Representations
- Self-Similarity Matrices
- Audio Thumbnailing
- Novelty-based Segmentation

Thanks:

- Clausen, Ewert, Kurth, Grohganz, …
- Dannenberg, Goto
- Grosche, Jiang
- Paulus, Klapuri
- Peeters, Kaiser, …
- Serra, Gómez, …
- Smith, Fujinaga, …
- Wiering, …
- Wand, Sunkel, Jansen
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Feature Representation

General goal: Convert an audio recording into a mid-level representation that captures certain musical properties while supressing other properties.

- Timbre / Instrumentation
- Tempo / Rhythm
- Pitch / Harmony

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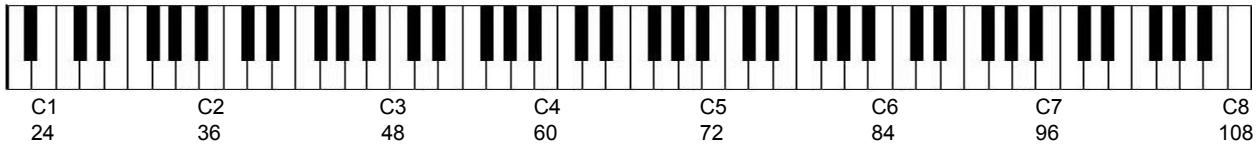
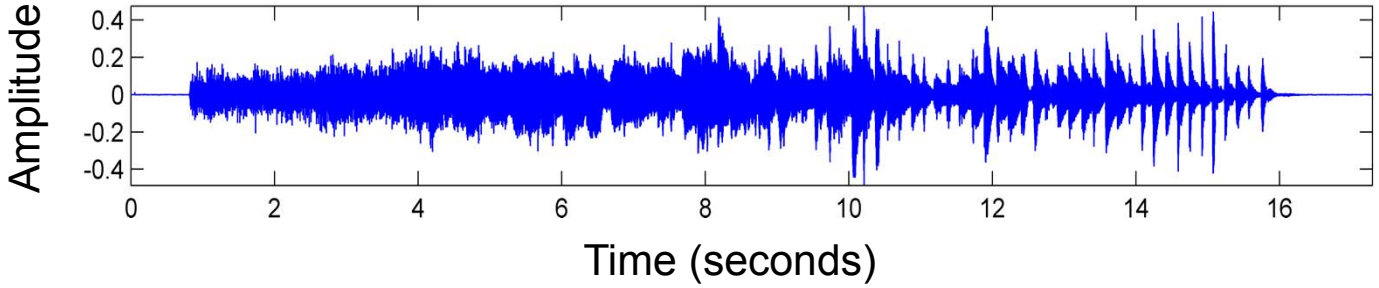
Feature Representation

Example: Chromatic scale



Waveform



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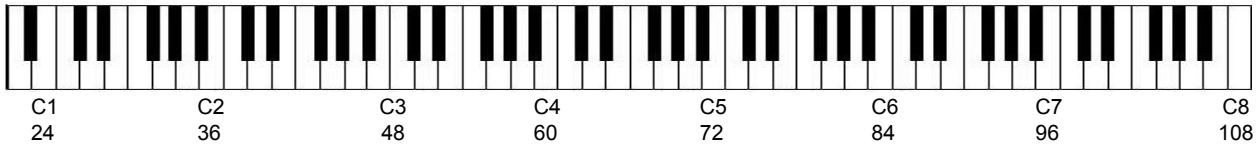
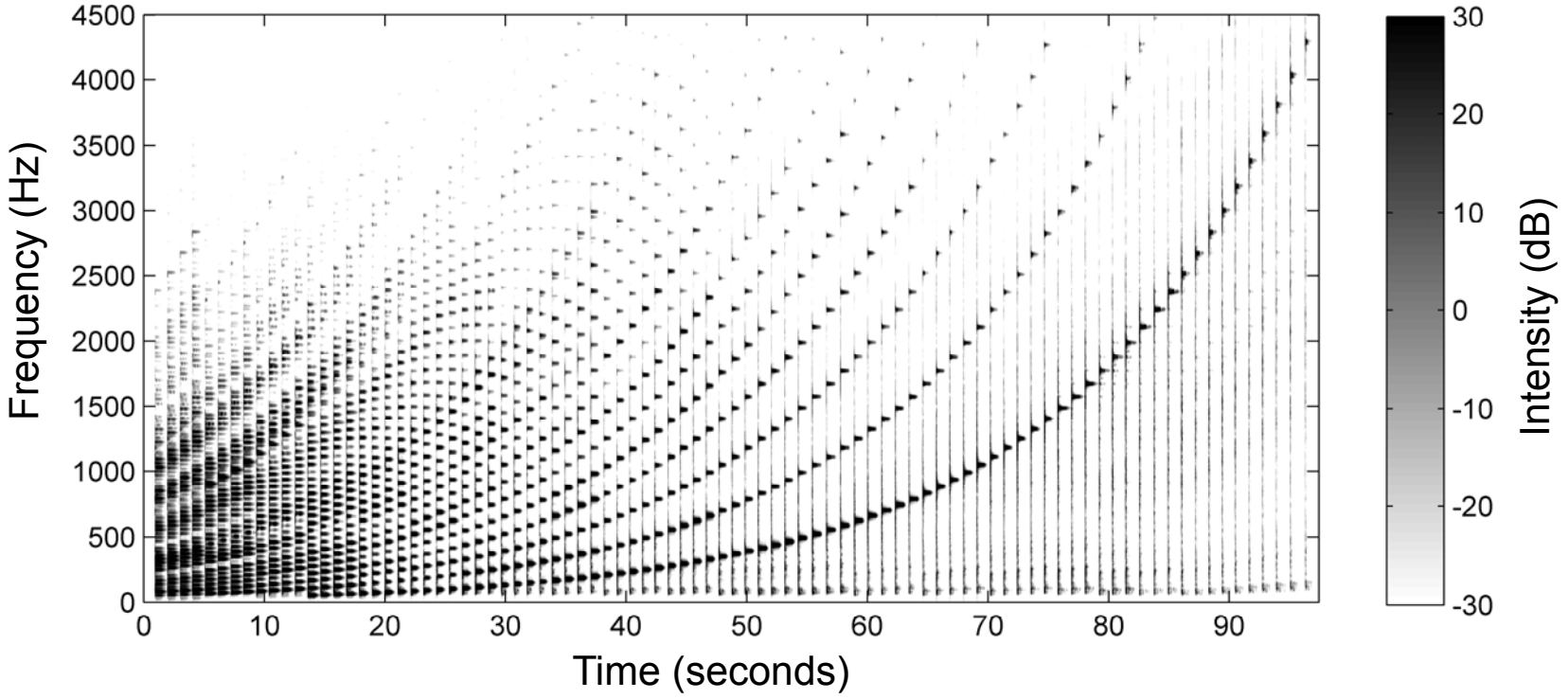


Spectrogram



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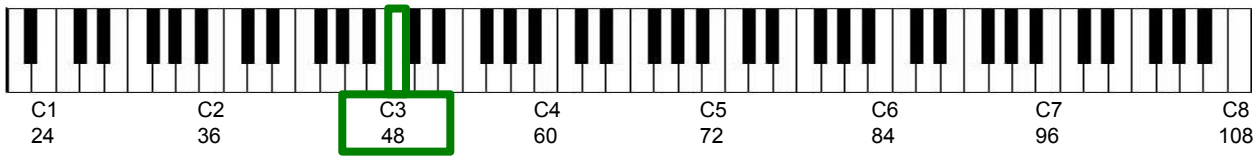

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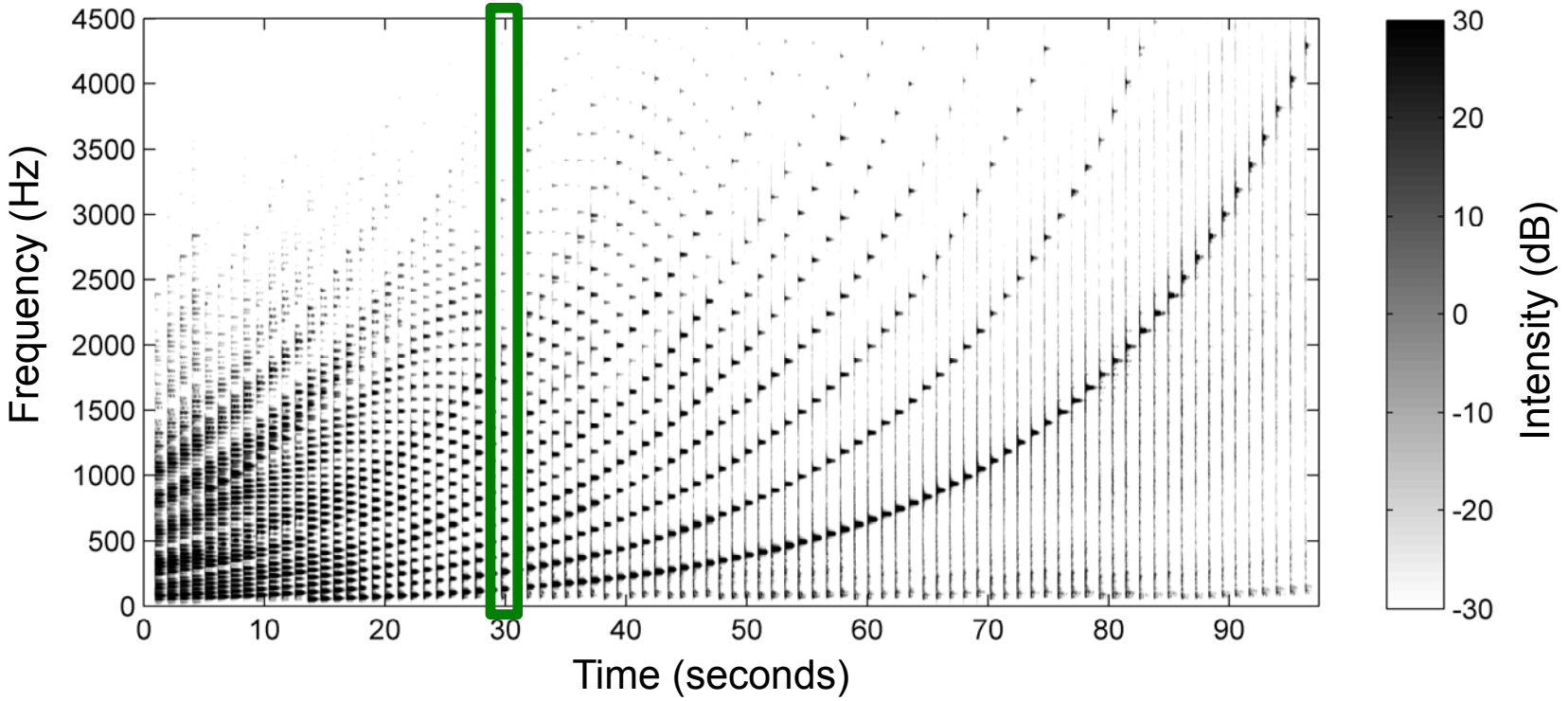

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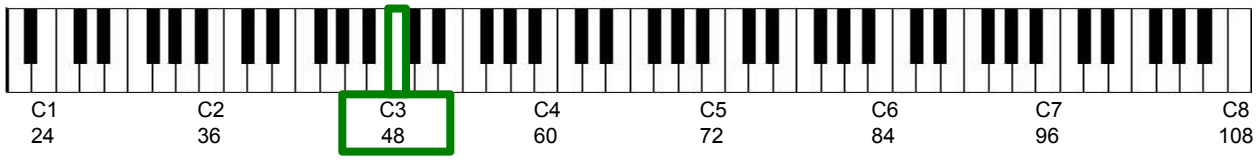

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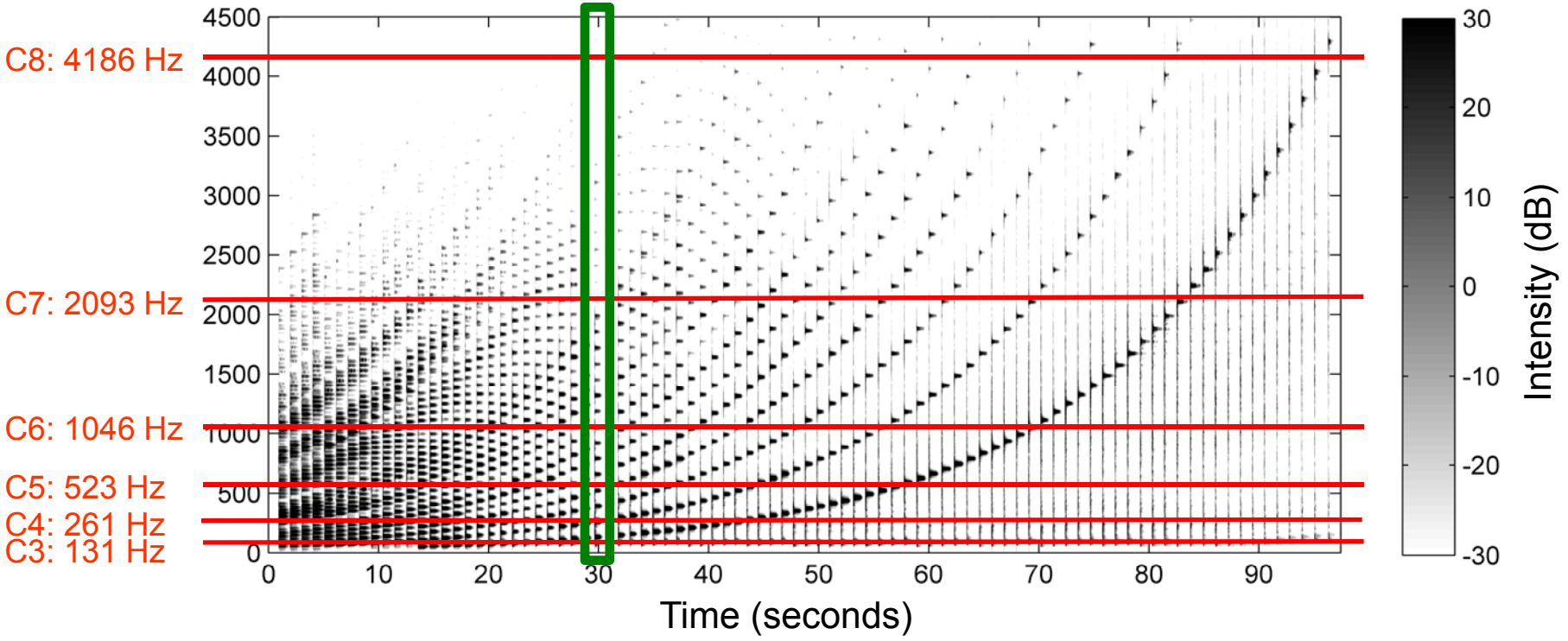

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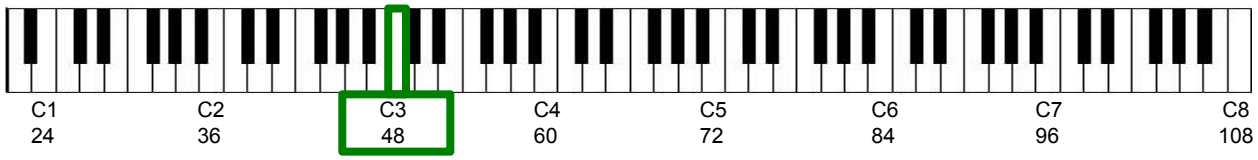
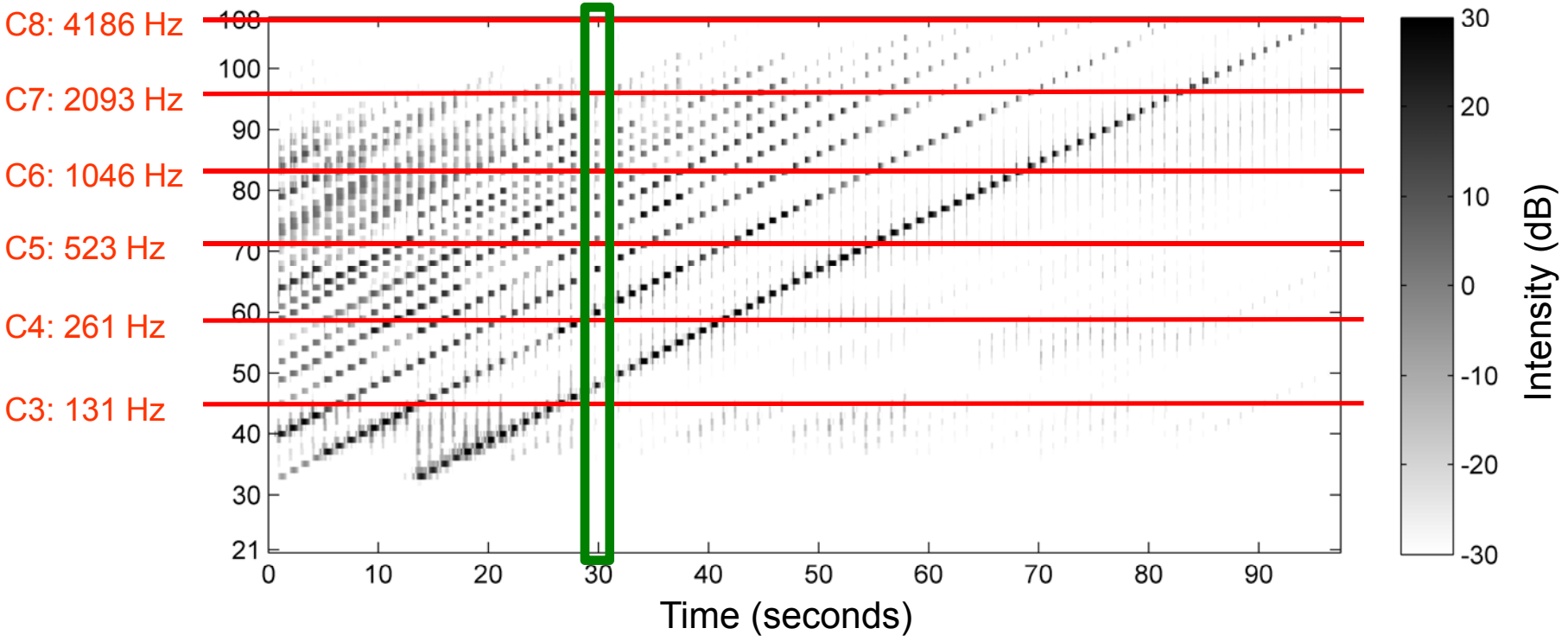


Log-frequency spectrogram



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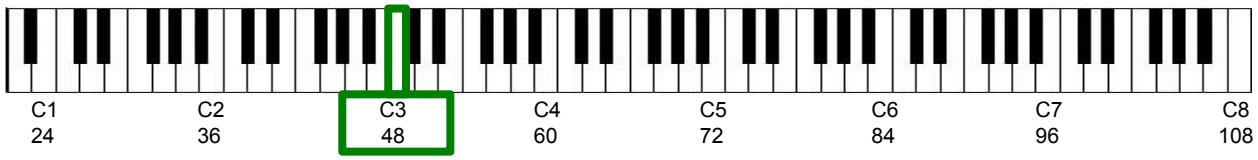

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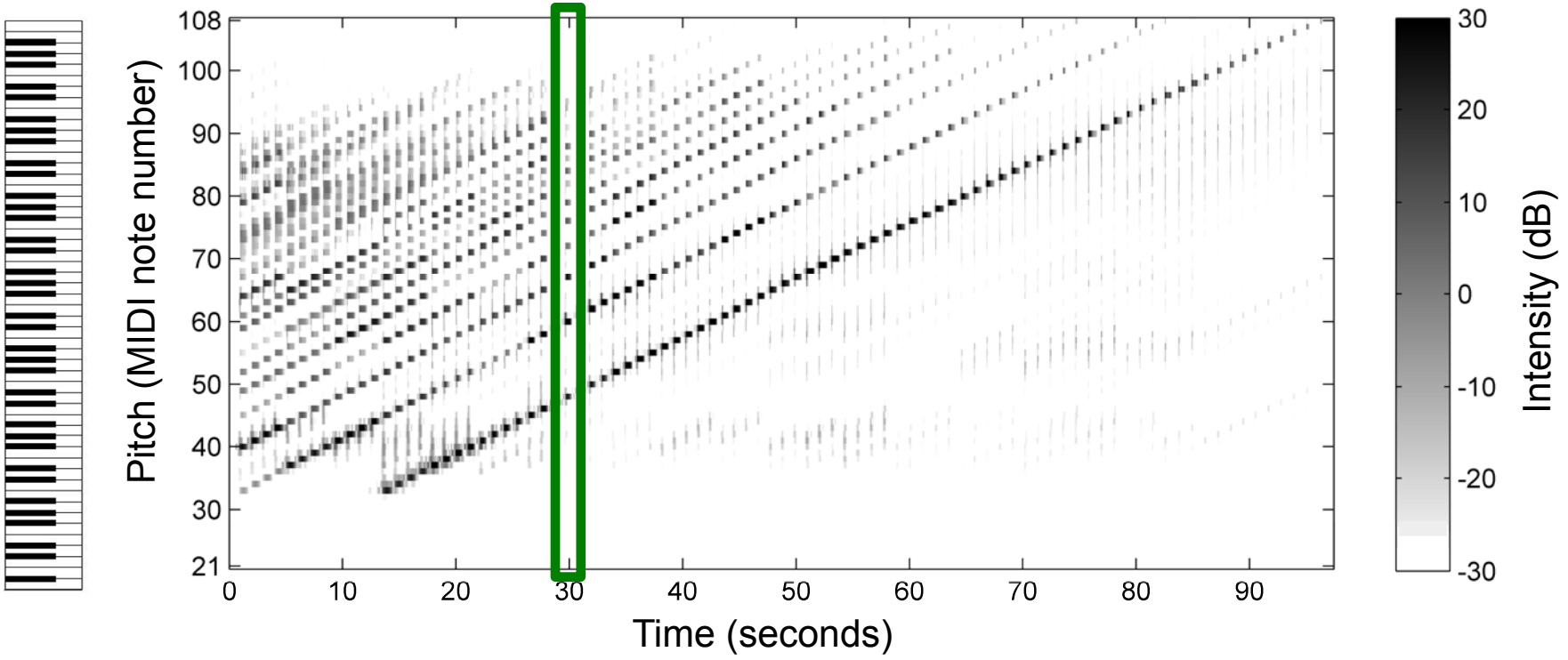

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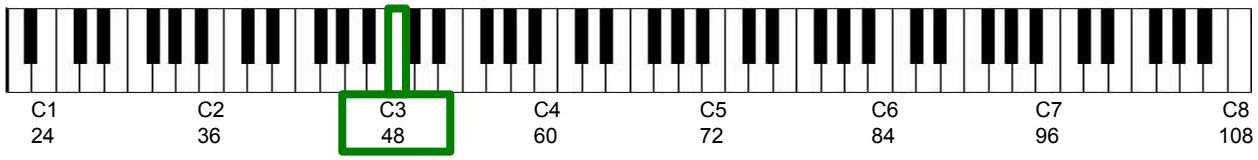

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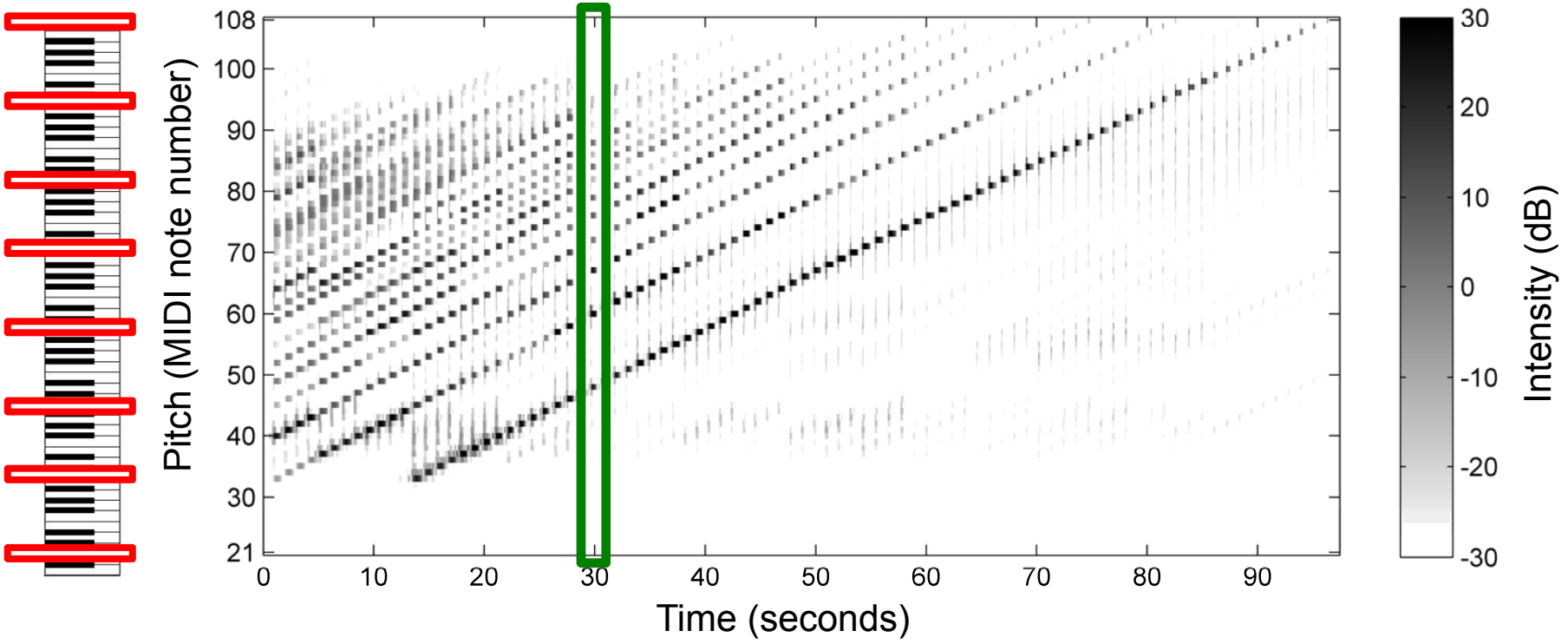
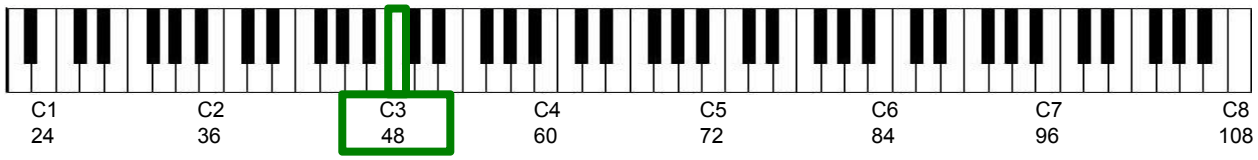


Chroma C

Feature Representation

Example: Chromatic scale



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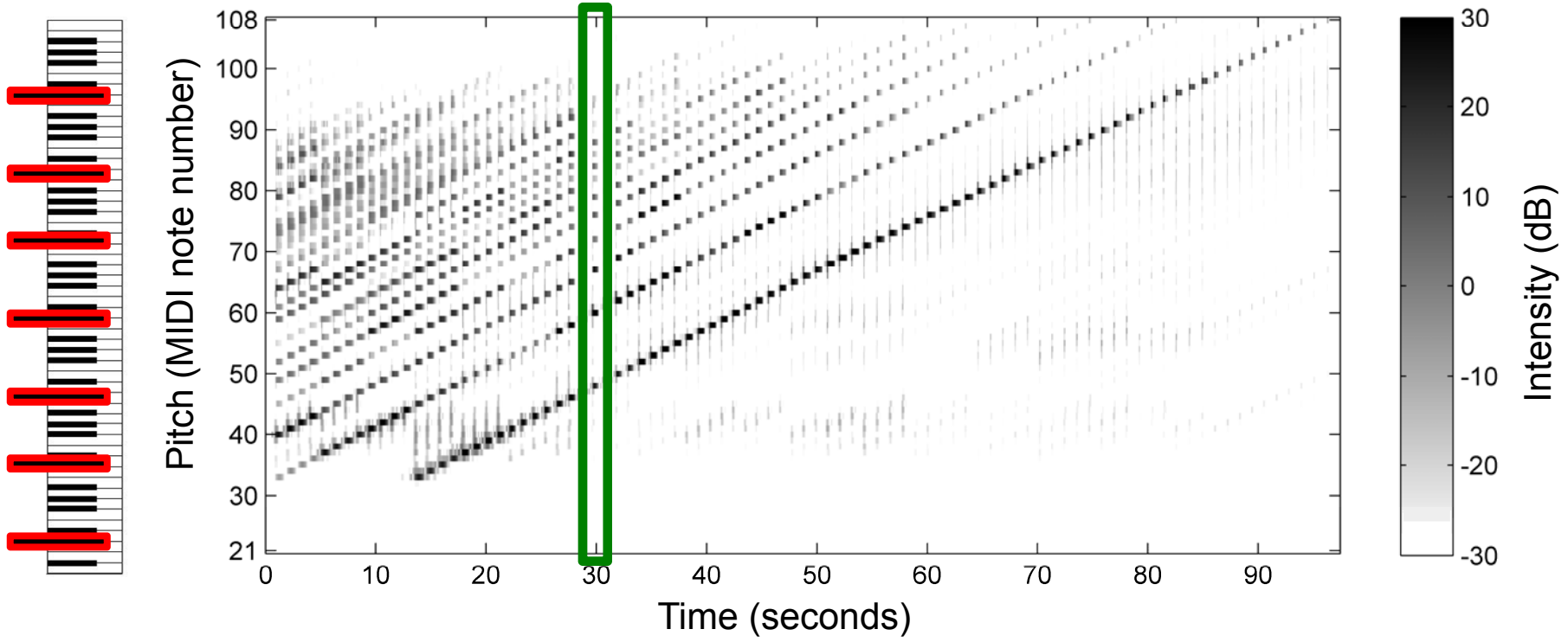

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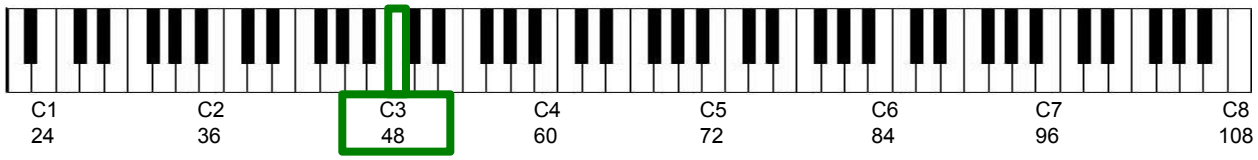

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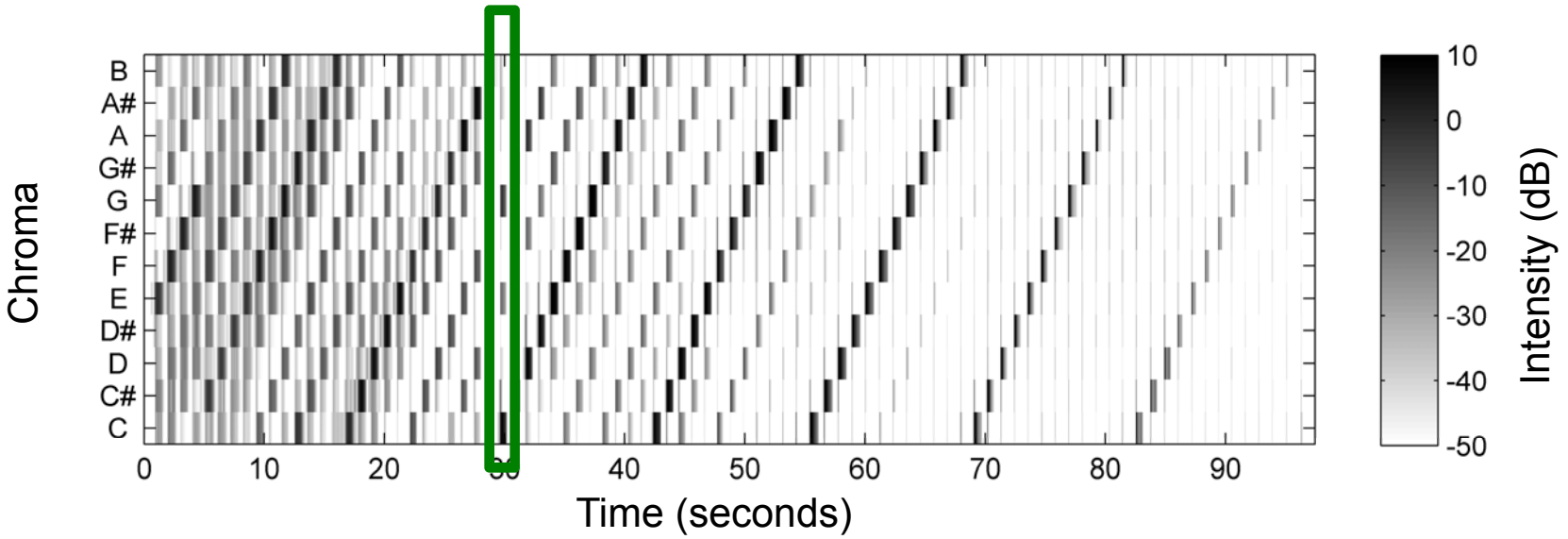
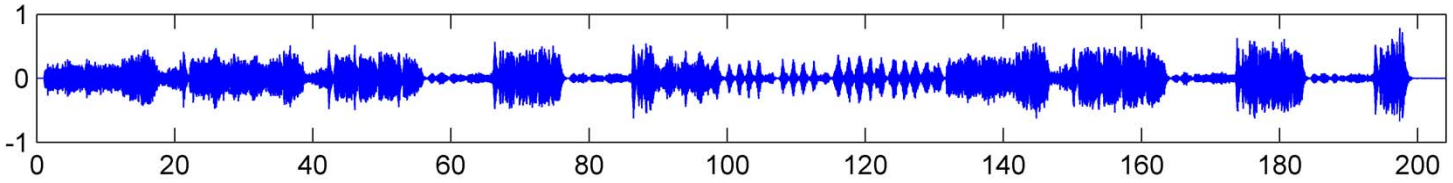
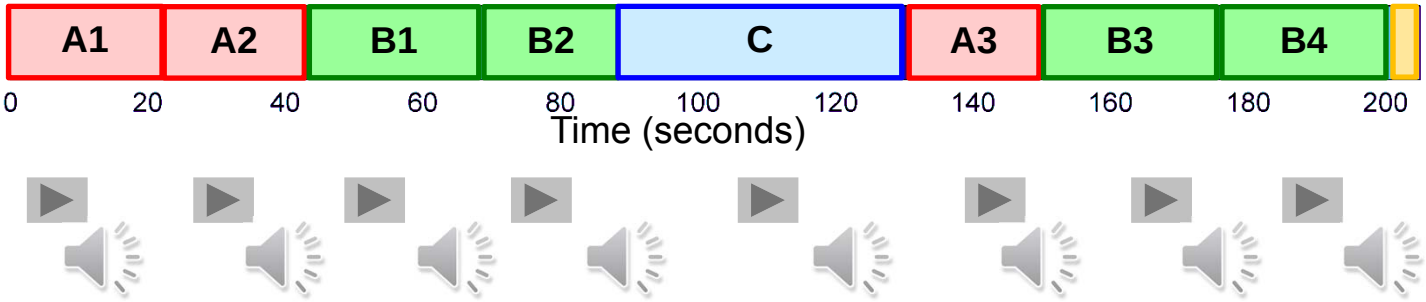


Feature Representation

Example: Brahms Hungarian Dance No. 5 (Ormandy)





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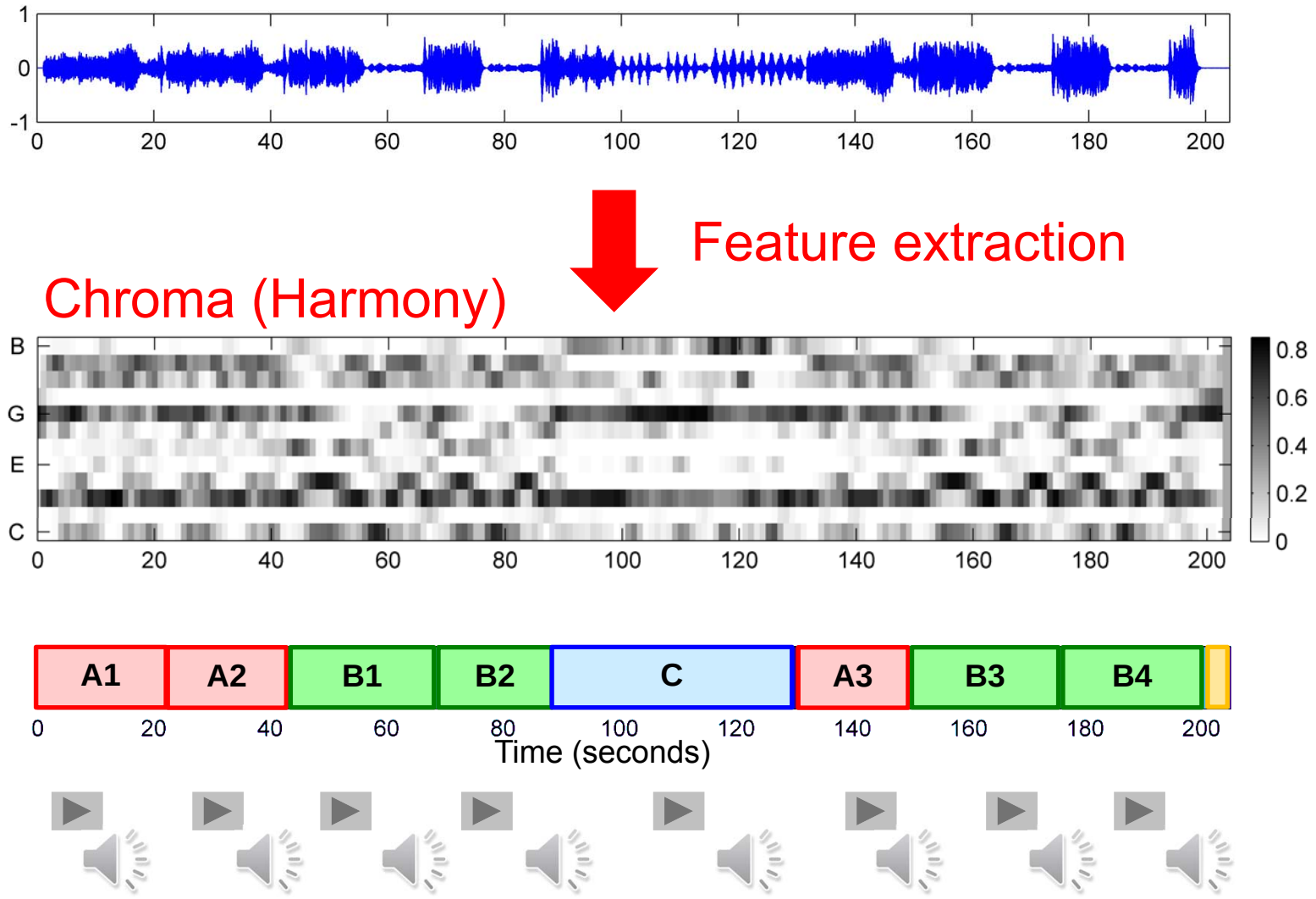

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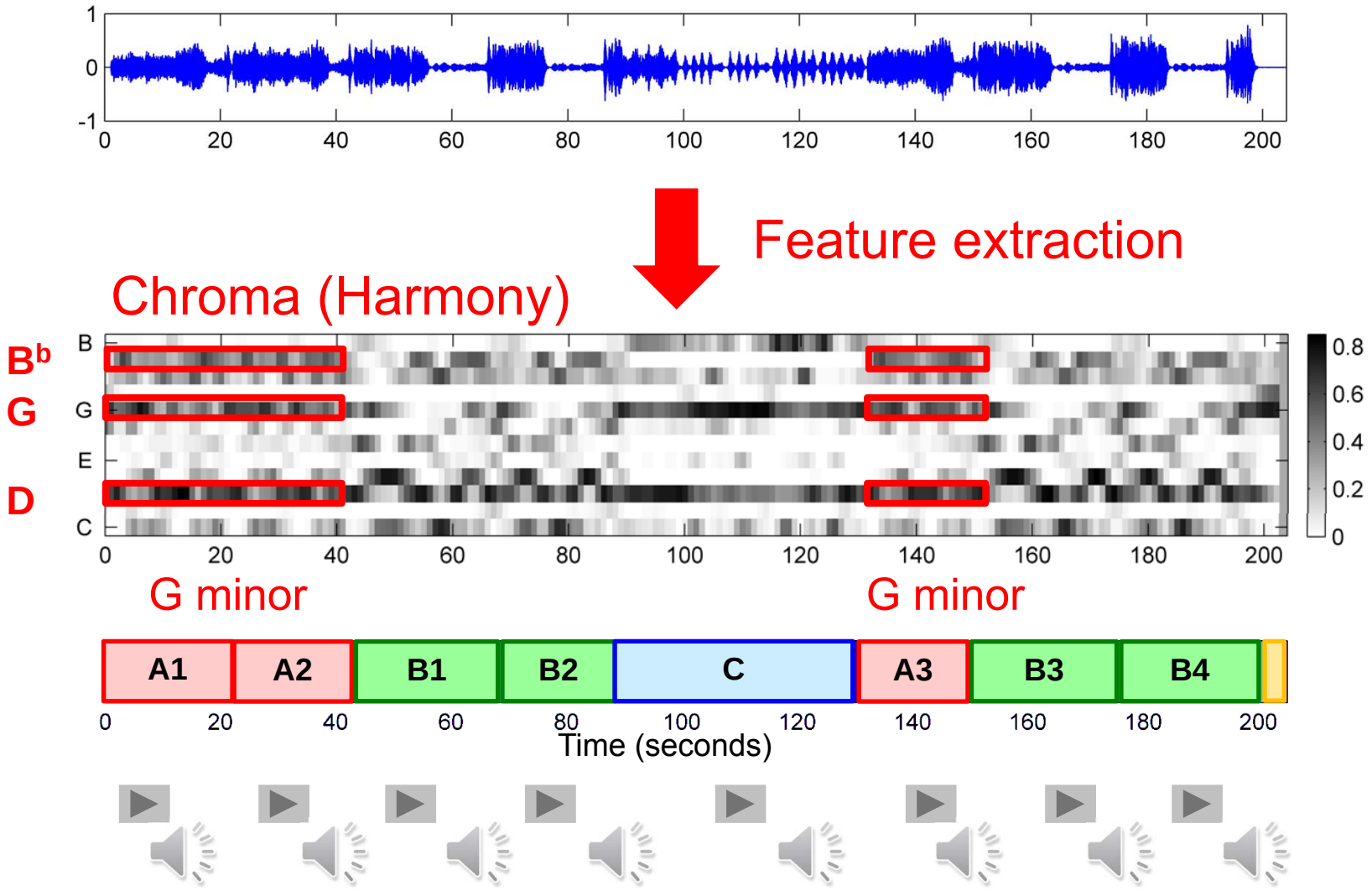

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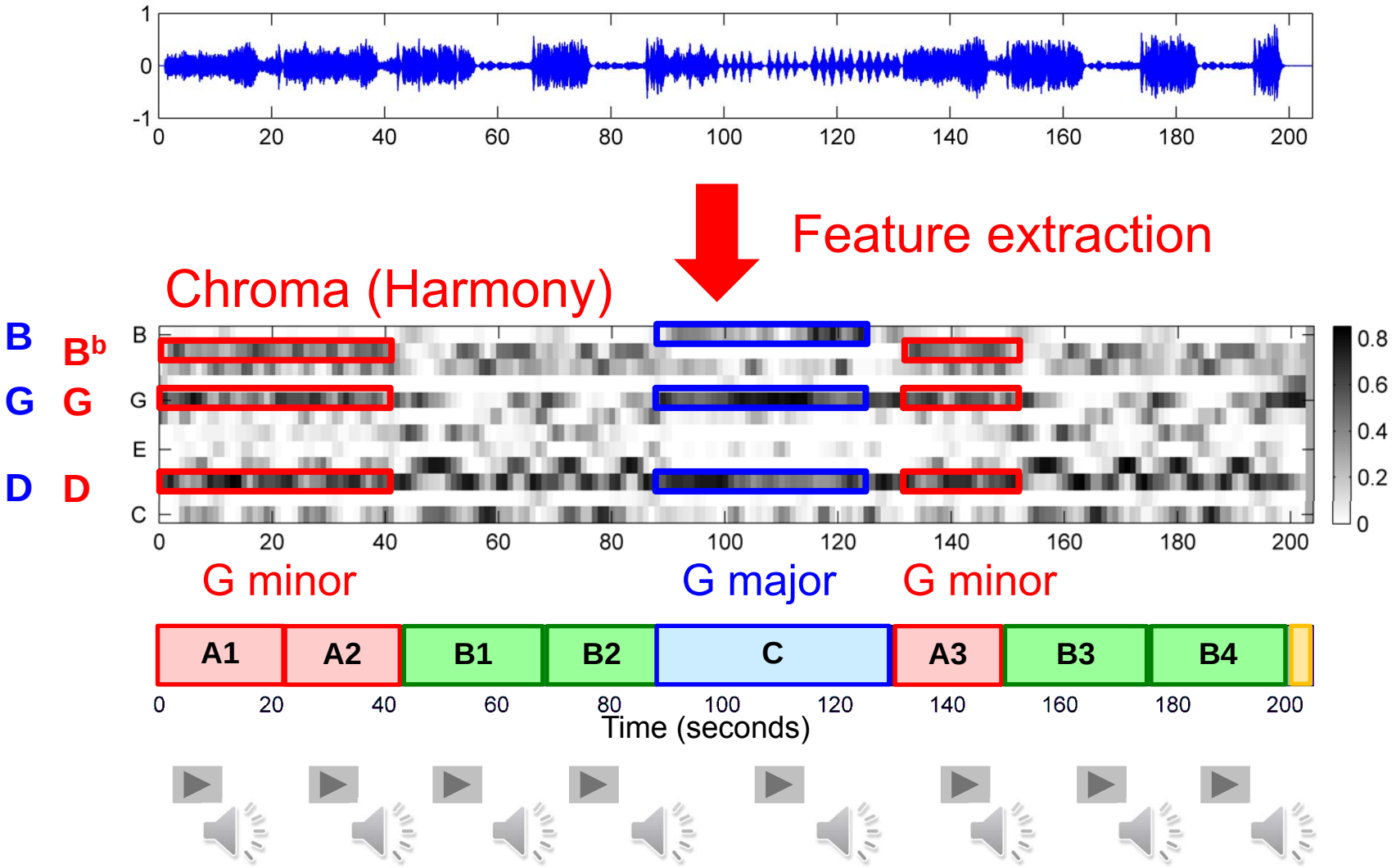

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- Self-Similarity Matrices
- Audio Thumbnailing
- Novelty-based Segmentation

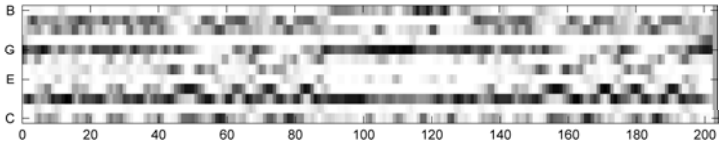
Self-Similarity Matrix (SSM)

General idea: Compare each element of the feature sequence with each other element of the feature sequence based on a suitable similarity measure.

→ Quadratic self-similarity matrix

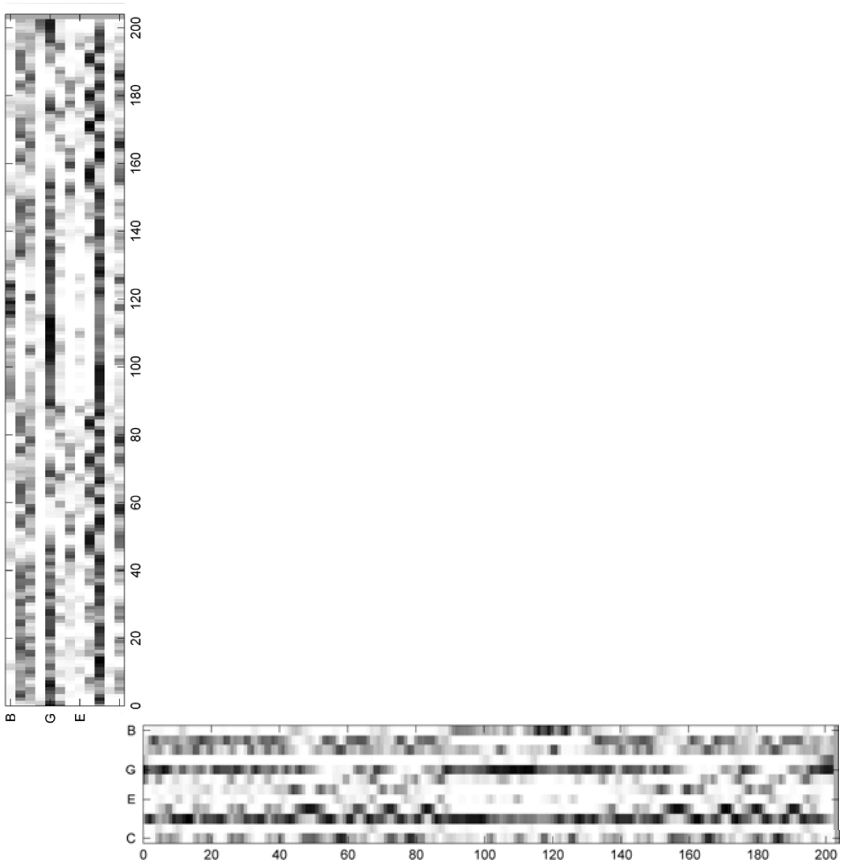
Self-Similarity Matrix (SSM)

Example: Brahms Hungarian Dance No. 5 (Ormandy)



Self-Similarity Matrix (SSM)

Example: Brahms Hungarian Dance No. 5 (Ormandy)



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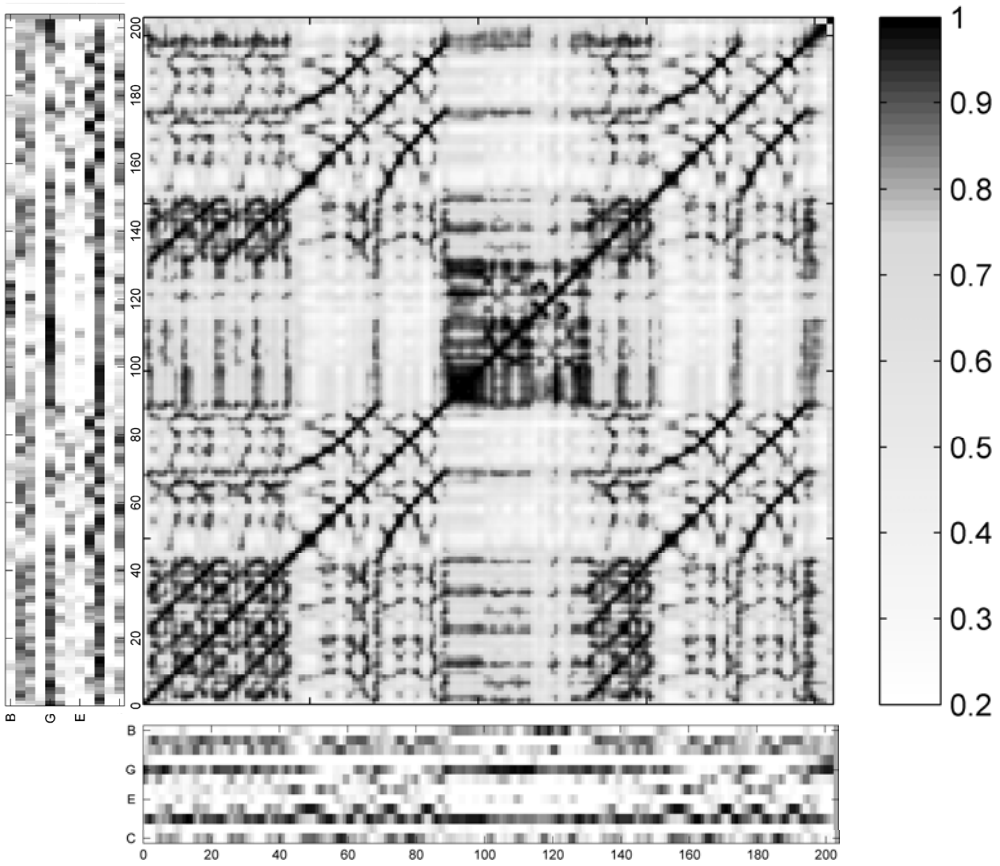

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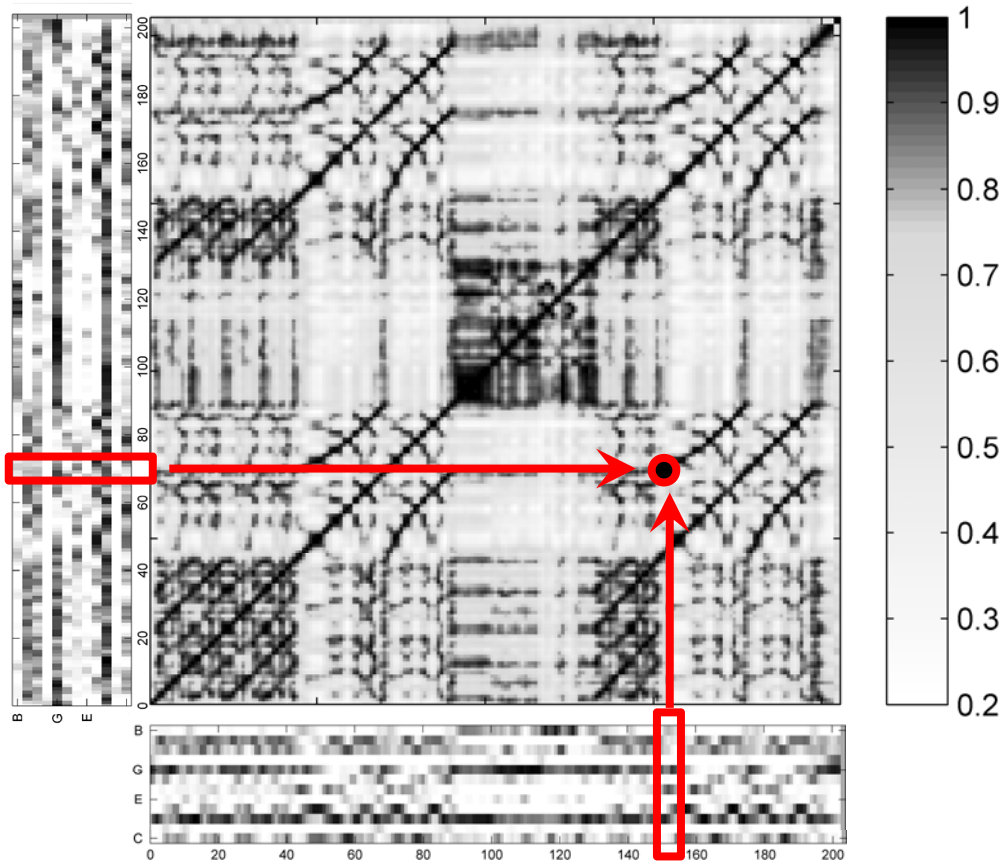

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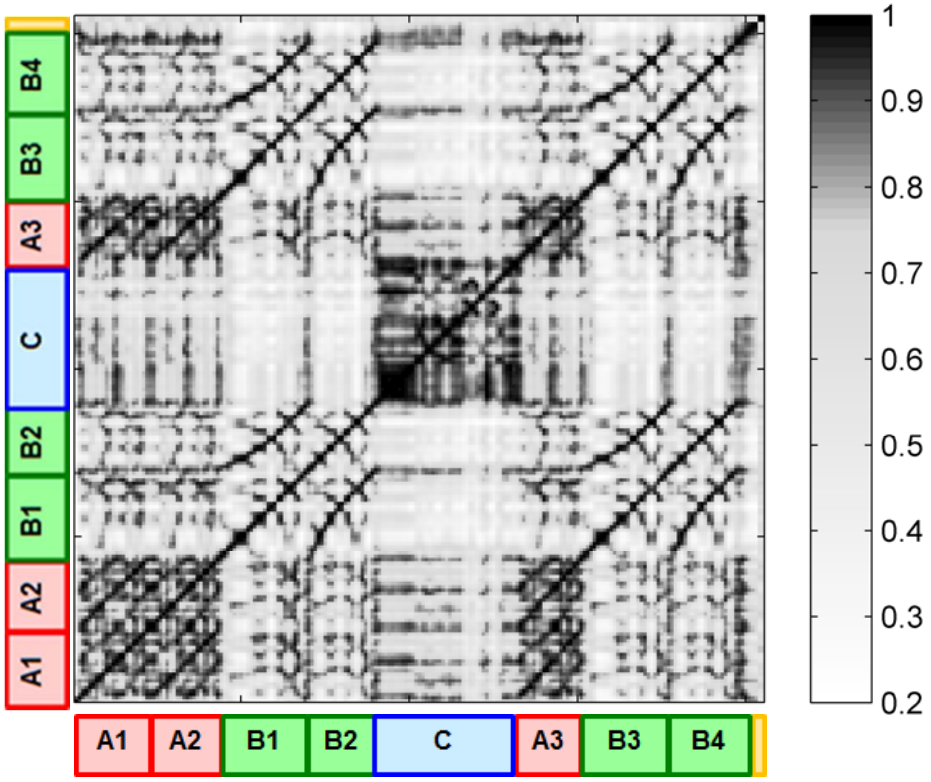

Self-Similarity Matrix (SSM)

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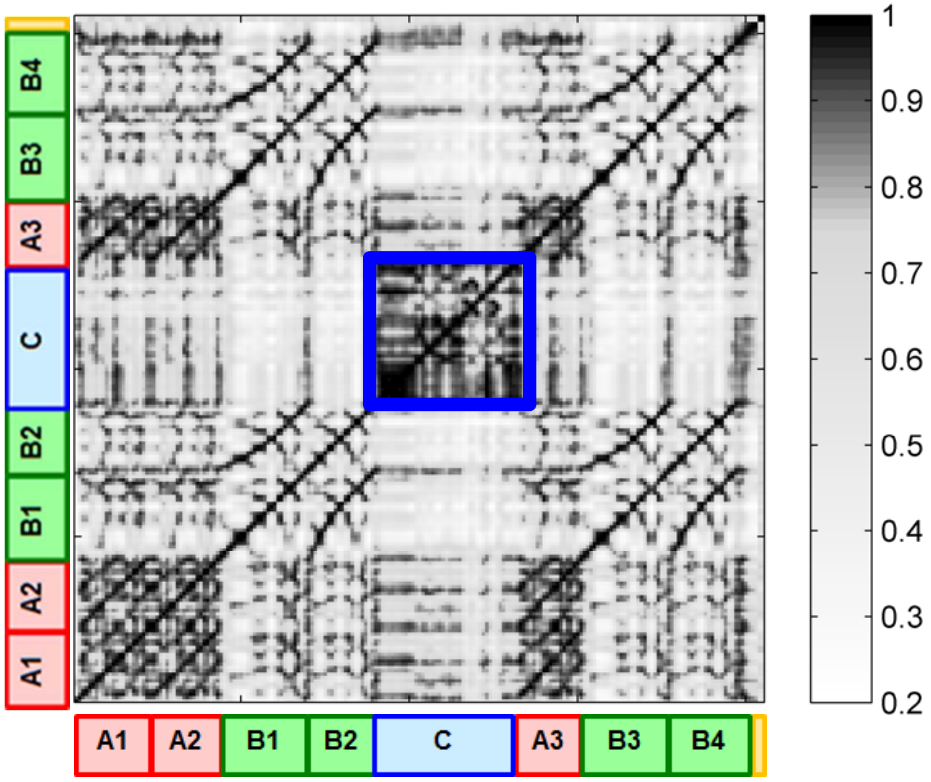

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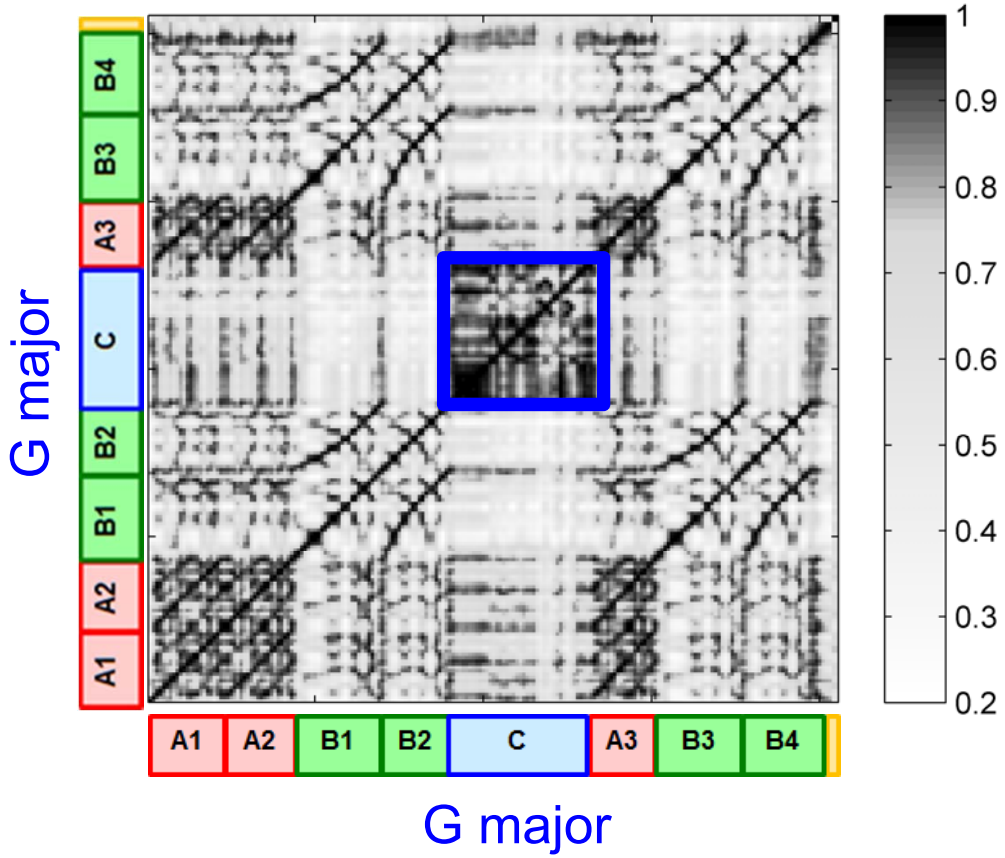

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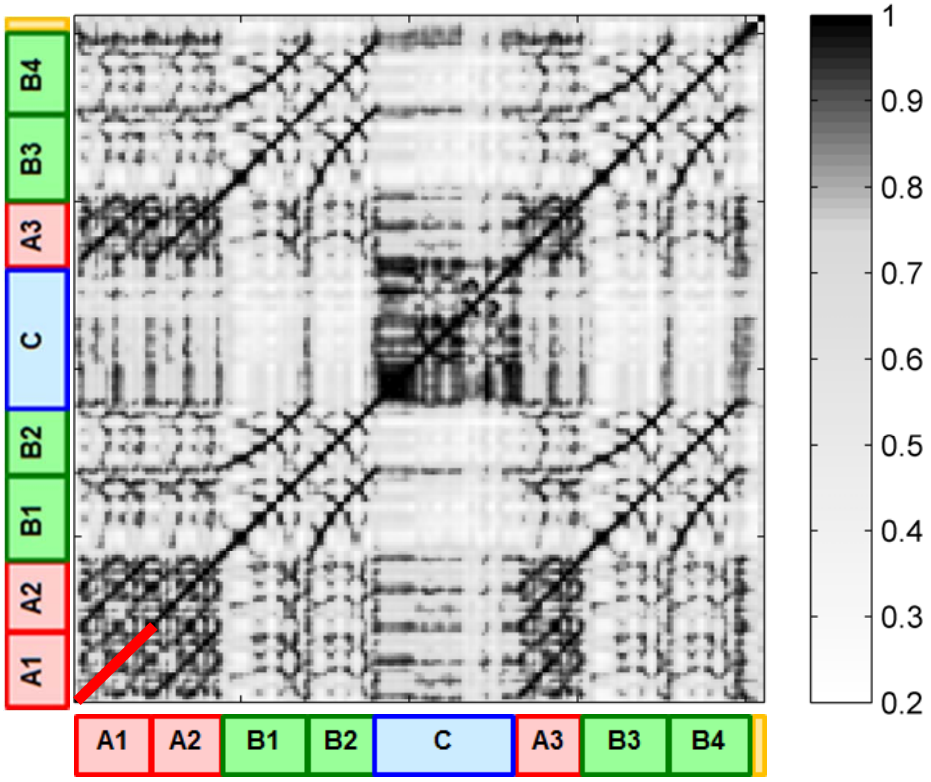

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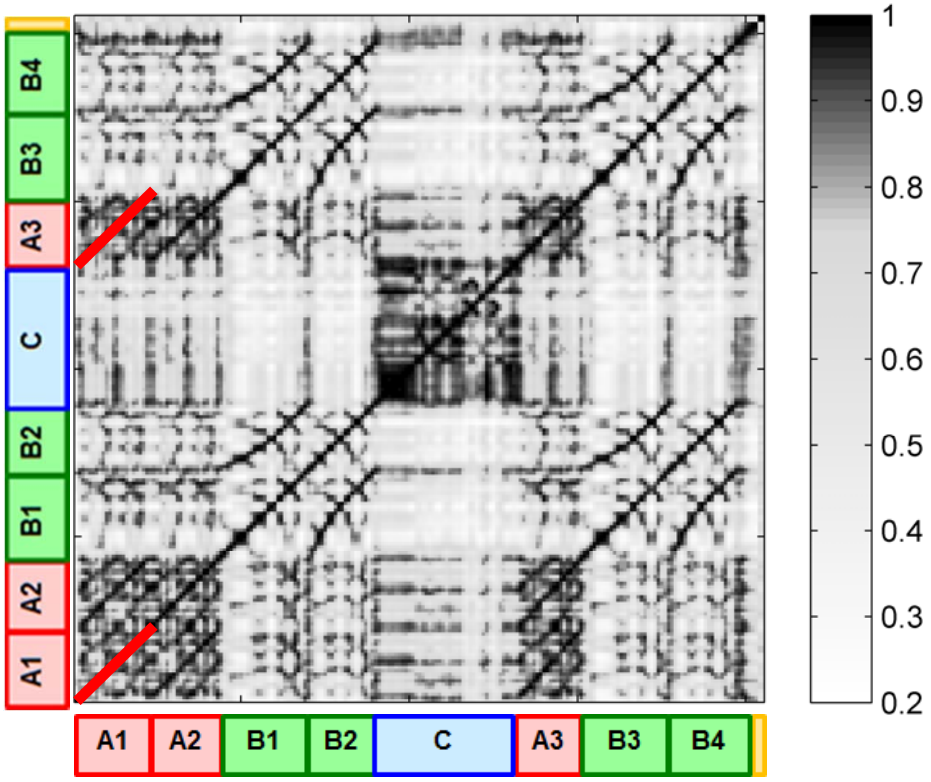

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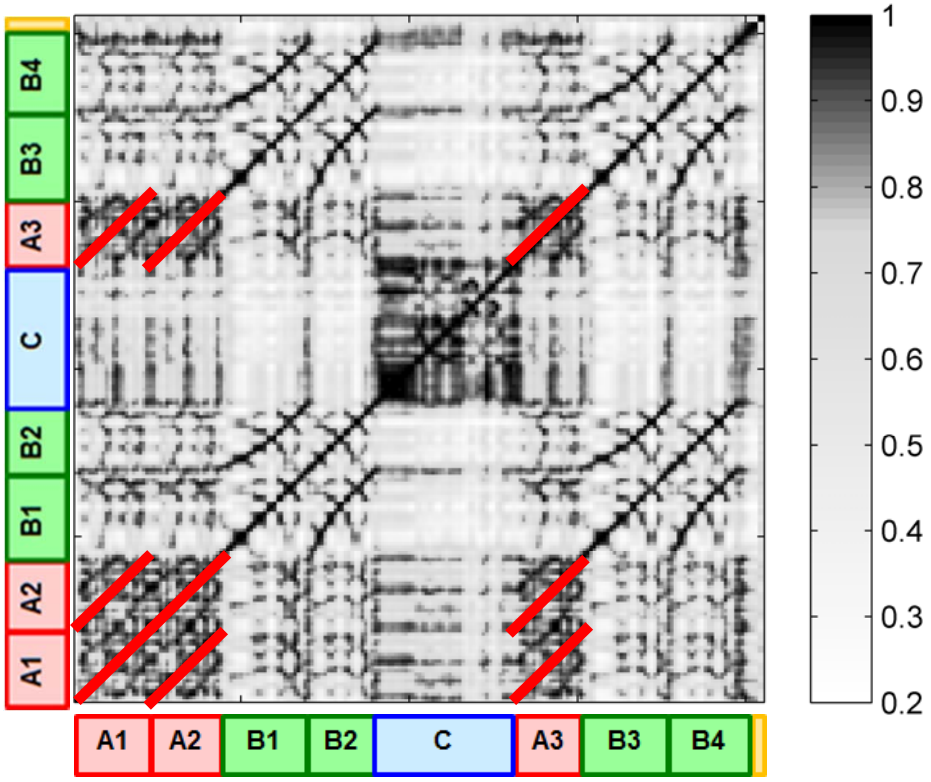

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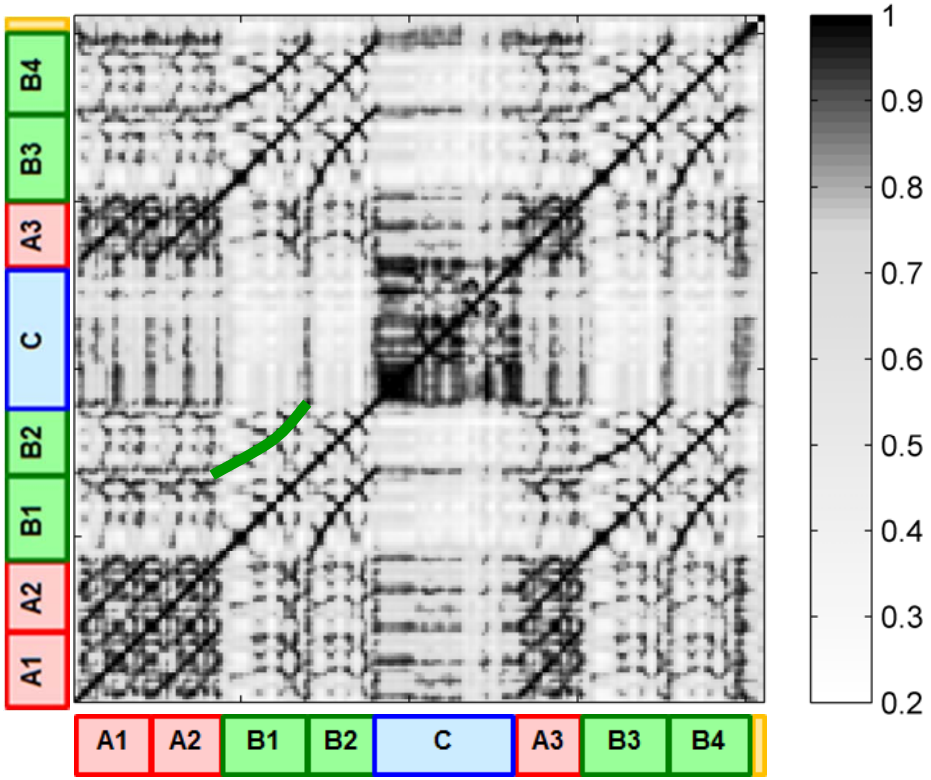

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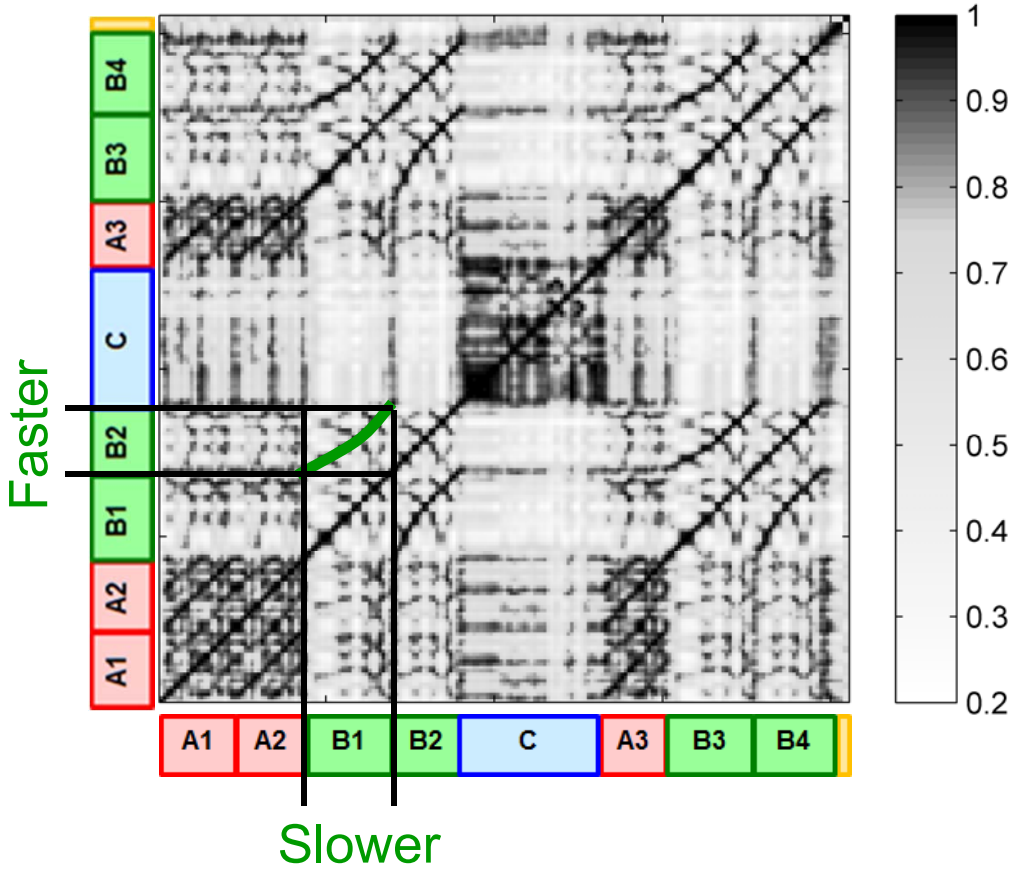

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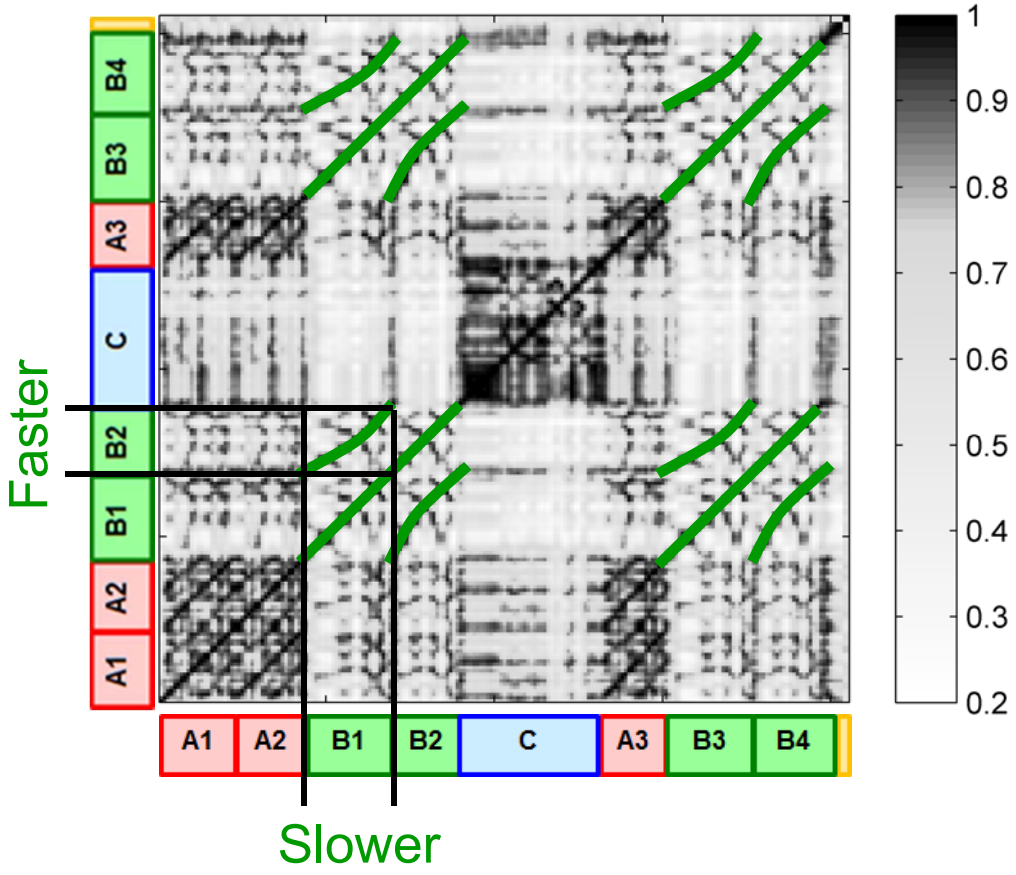

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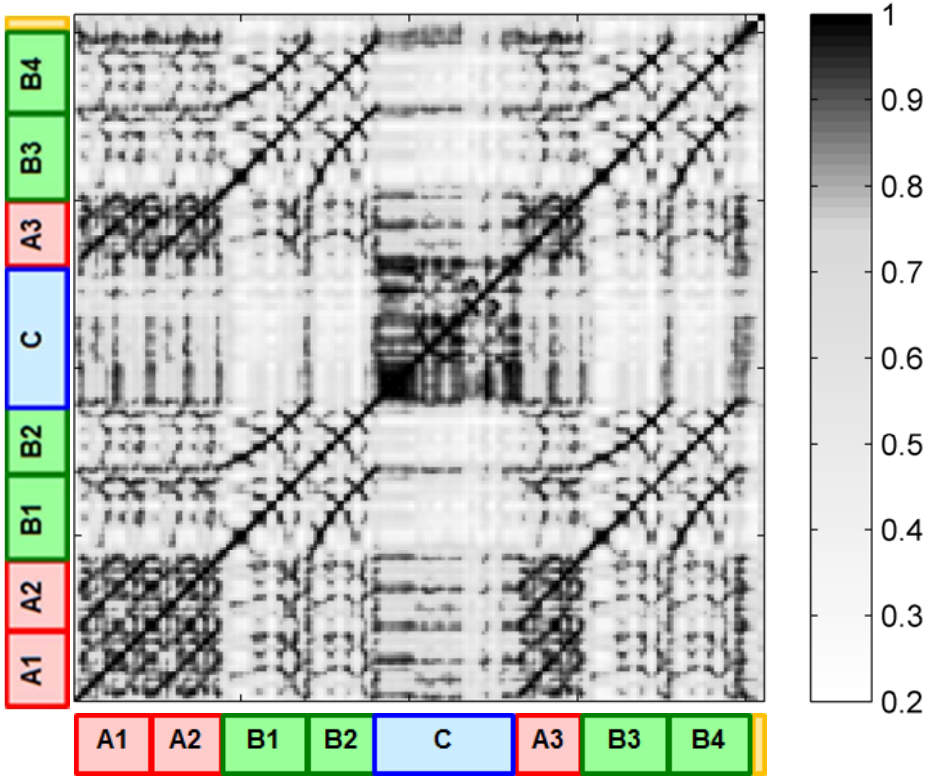
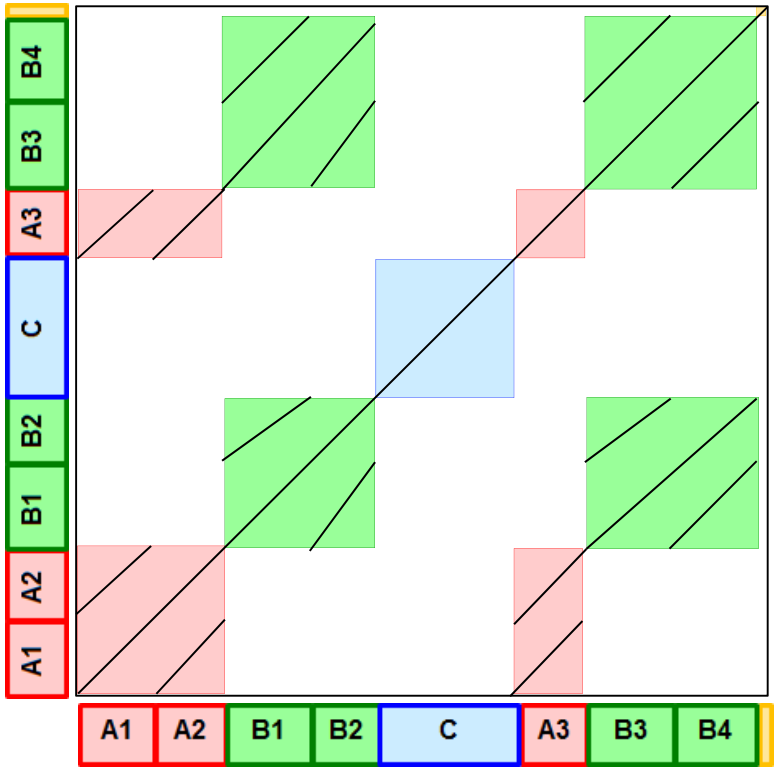


Idealized SSM



Self-Similarity Matrix (SSM)

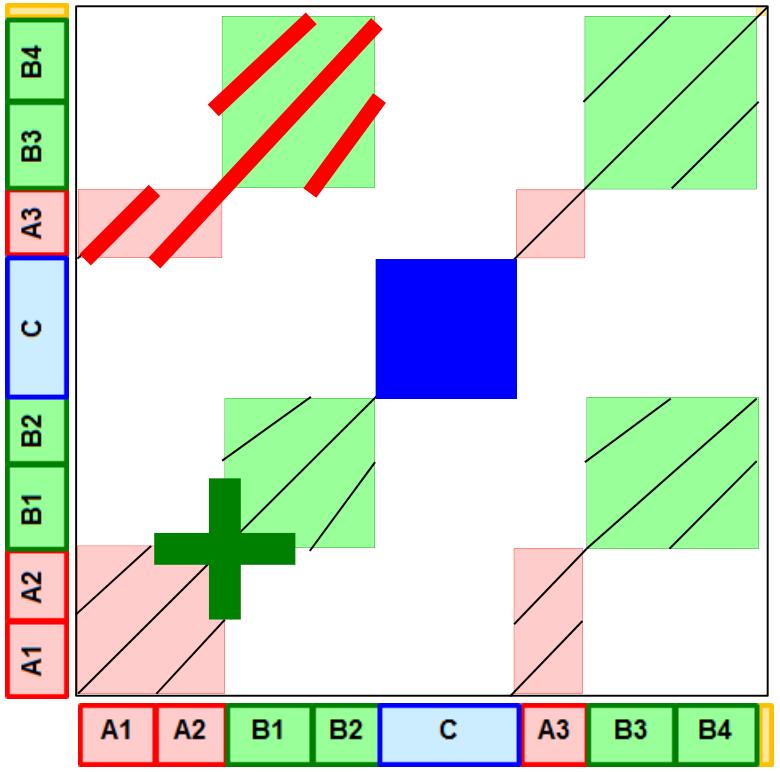
Example: Brahms Hungarian Dance No. 5 (Ormandy)

Blocks: Homogeneity

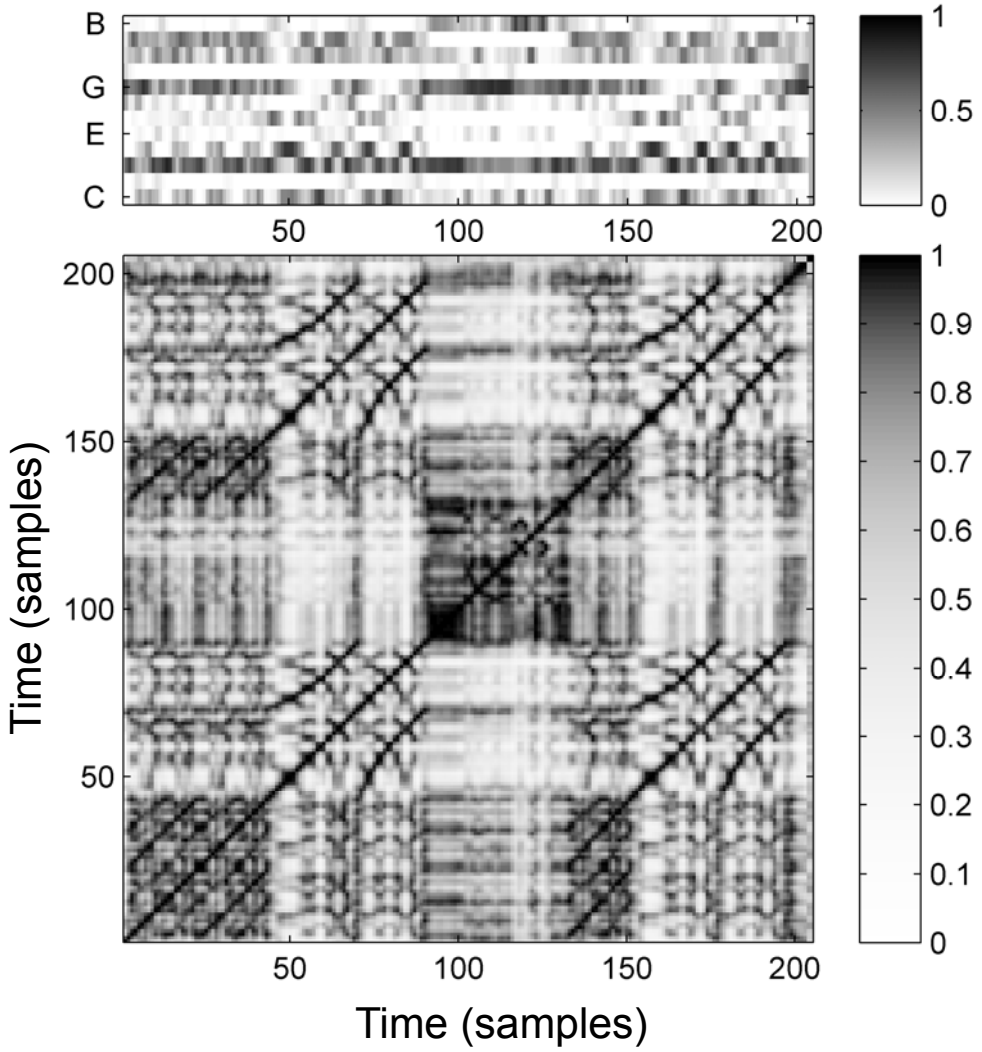
Paths: Repetition

Corners: Novelty

Idealized SSM



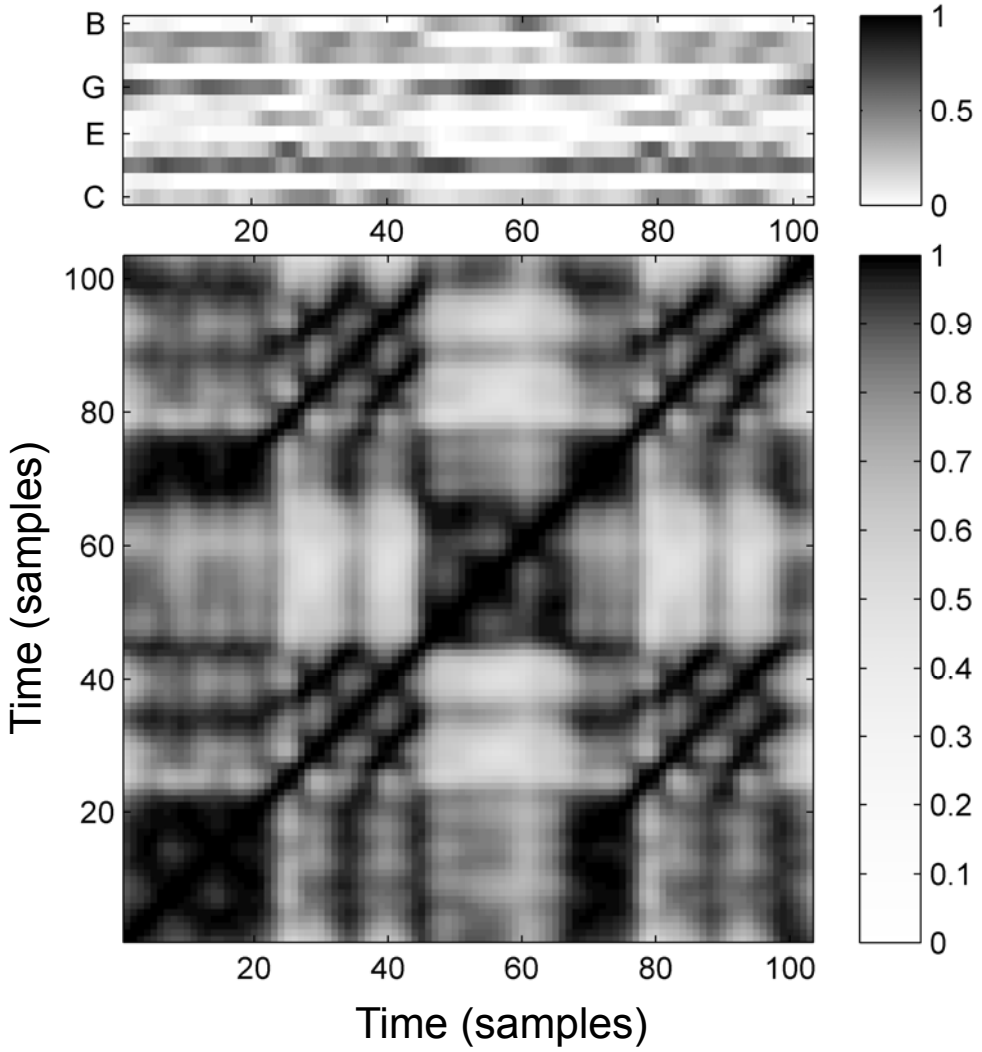
SSM Enhancement



Block Enhancement

- Feature smoothing
- Coarsening

SSM Enhancement



Block Enhancement

- Feature smoothing
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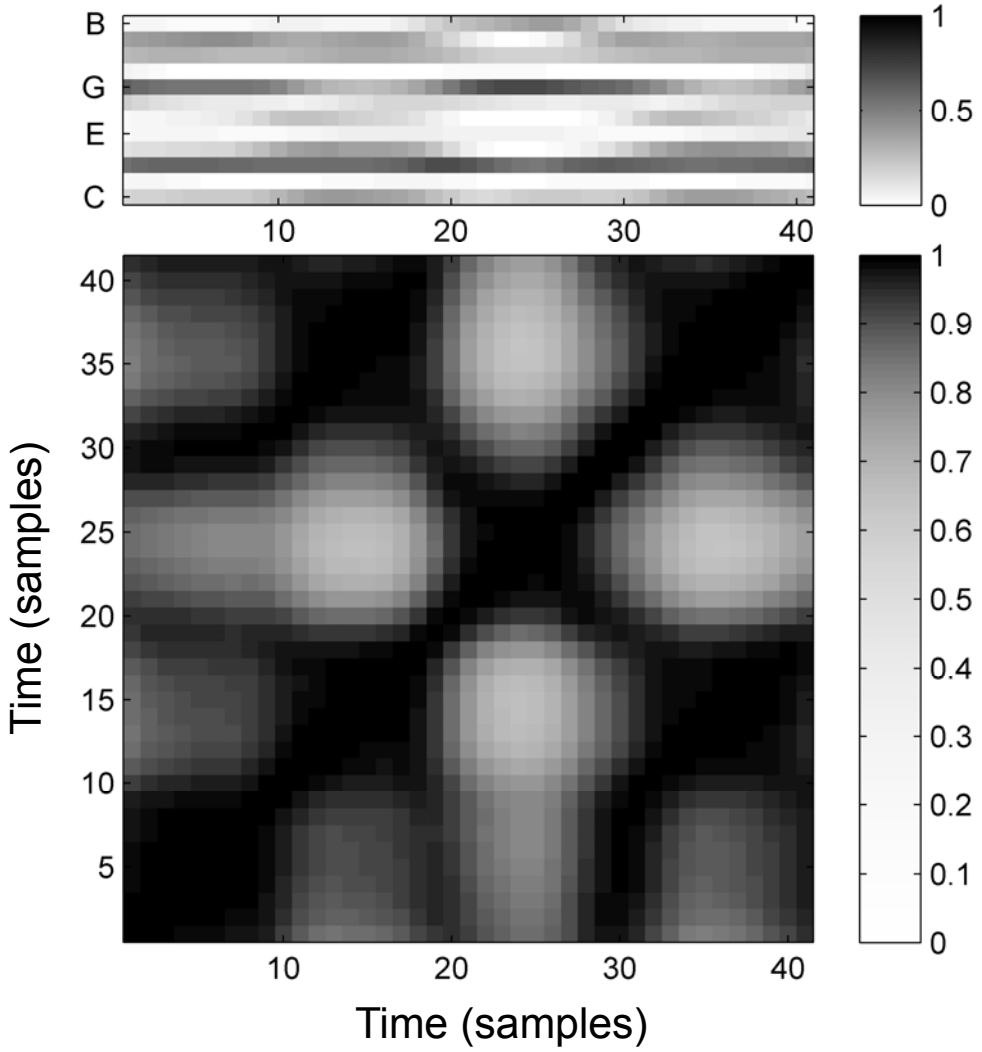
SSM Enhancement



Block Enhancement

- Feature smoothing
- Coarsening

SSM Enhancement

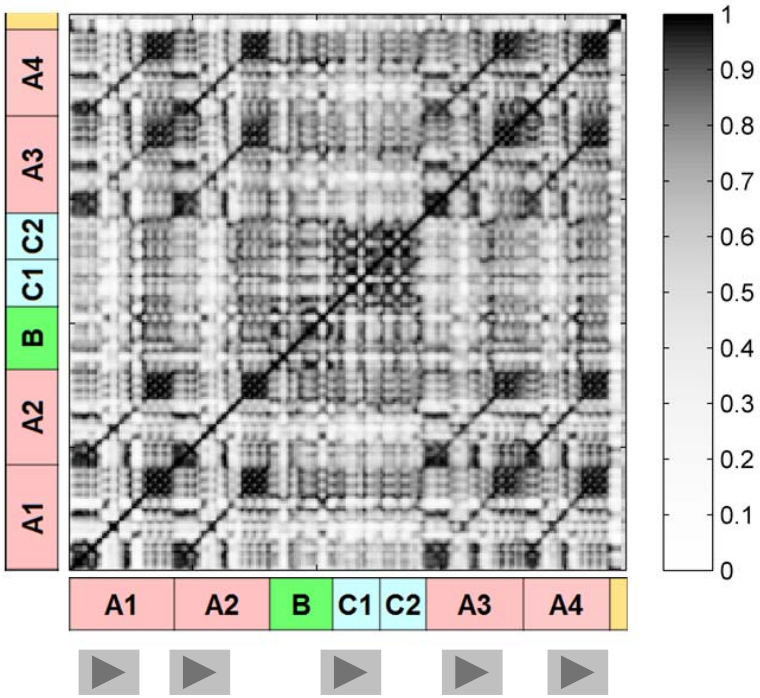
Challenge: Presence of musical variations

- Fragmented paths and gaps
- Paths of poor quality
- Regions of constant (high) similarity
- Curved paths

Idea: Enhancement of path structure

SSM Enhancement

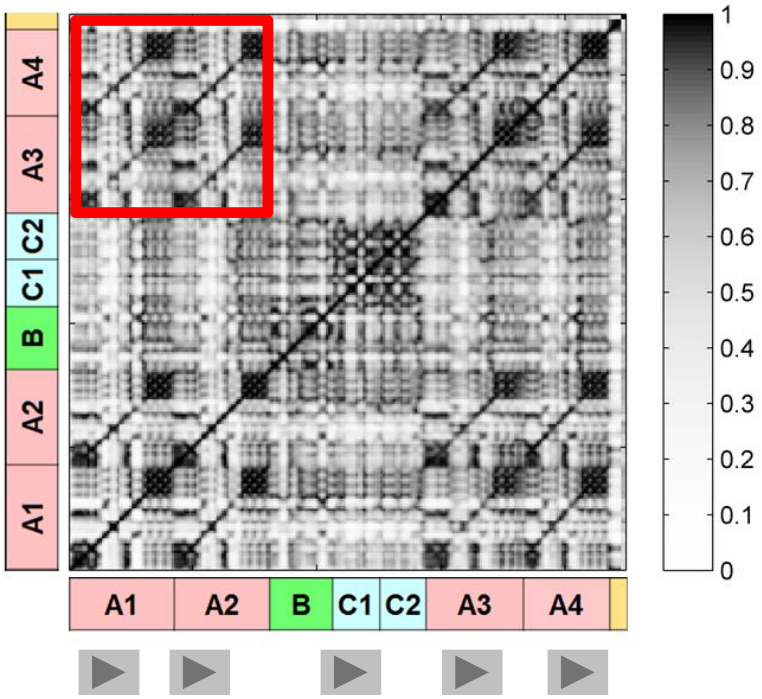
Shostakovich Waltz 2, Jazz Suite No. 2 (Chailly)



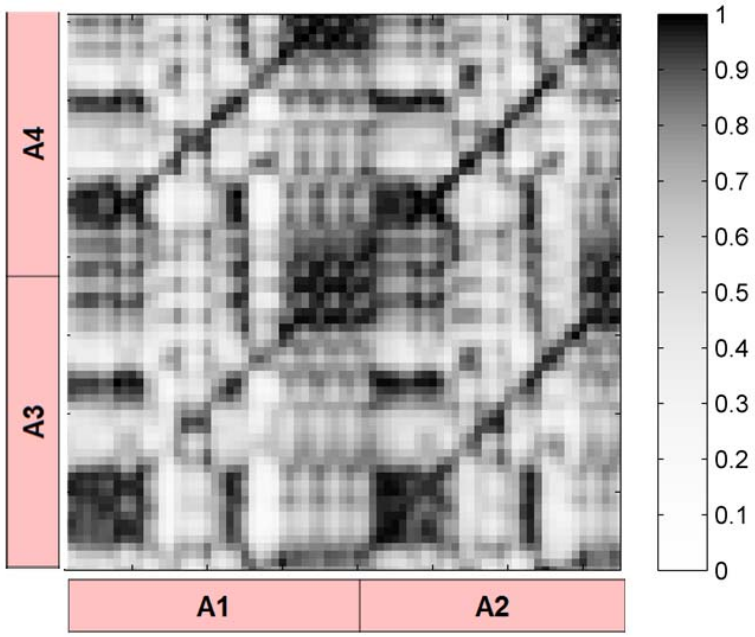
SSM

SSM Enhancement

Shostakovich Waltz 2, Jazz Suite No. 2 (Chailly)

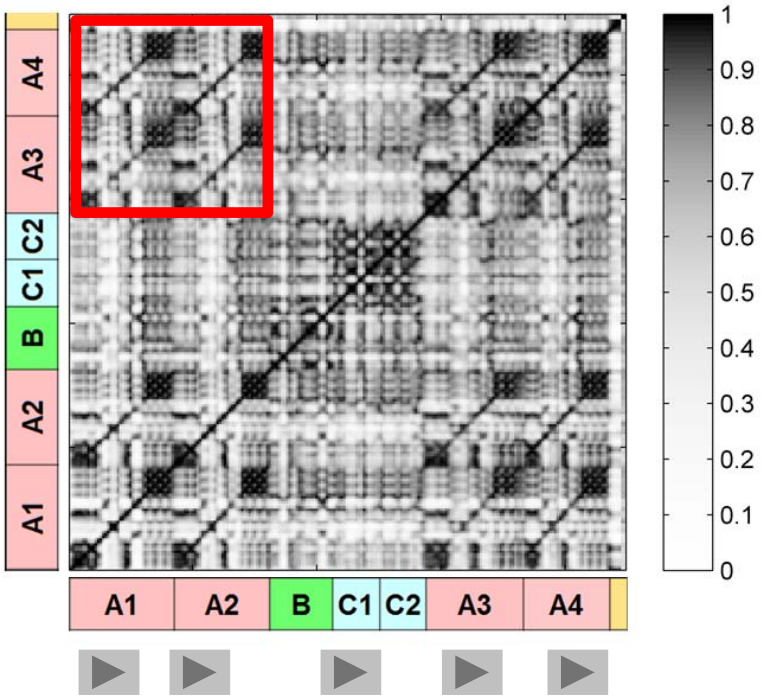


SSM

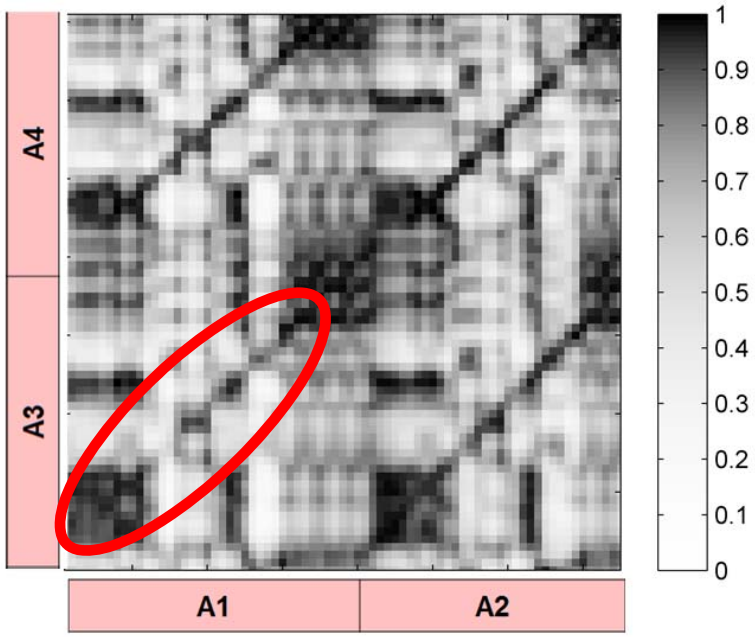


SSM Enhancement

Shostakovich Waltz 2, Jazz Suite No. 2 (Chailly)

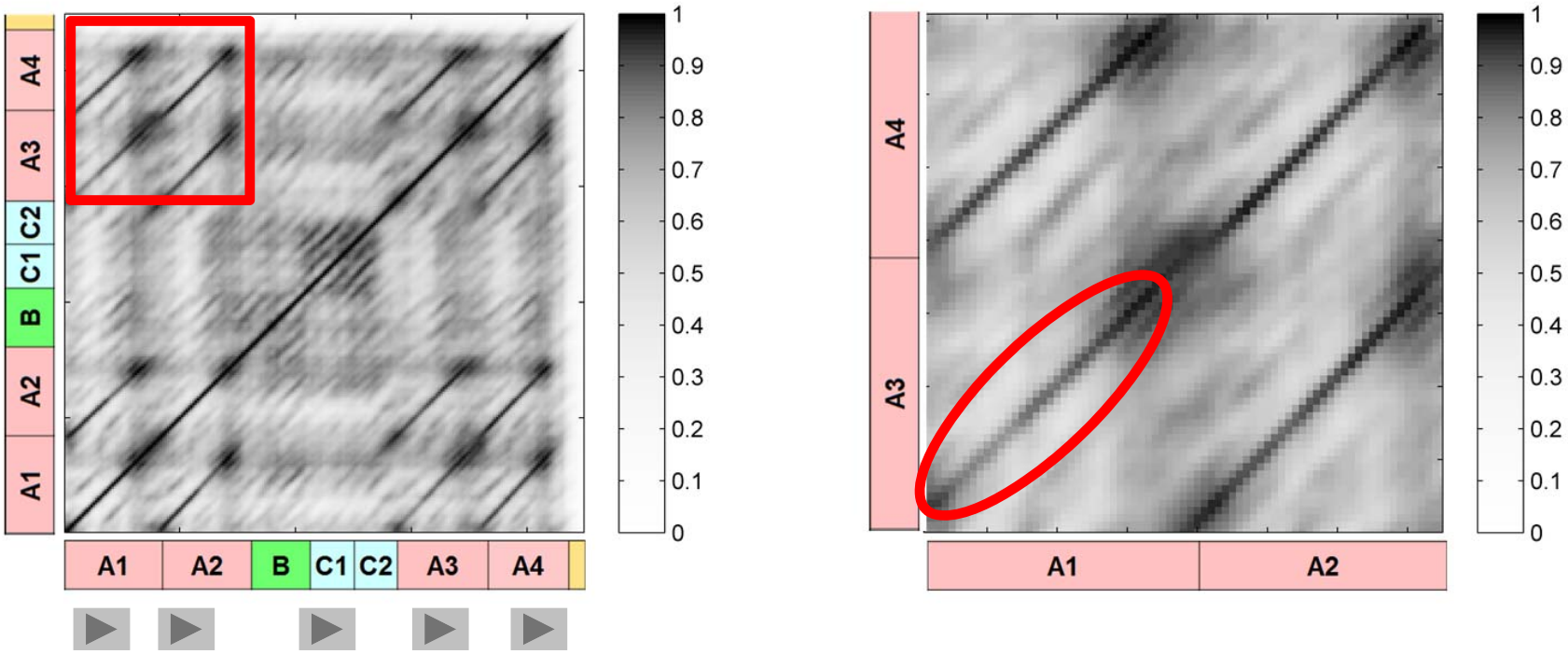


SSM



SSM Enhancement

Shostakovich Waltz 2, Jazz Suite No. 2 (Chailly)



Enhanced SSM

Filtering along main diagonal

SSM Enhancement

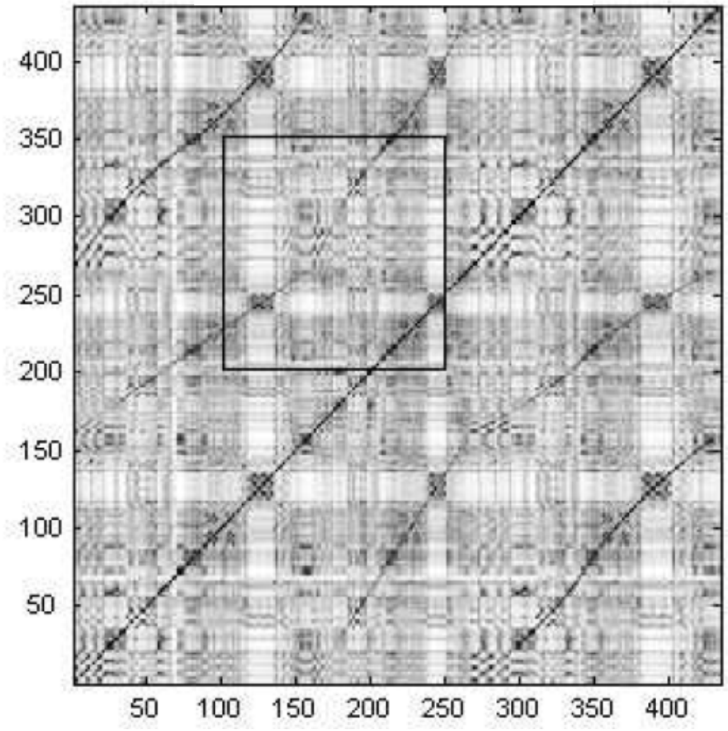
Idea: Usage of contextual information (Foote 1999)

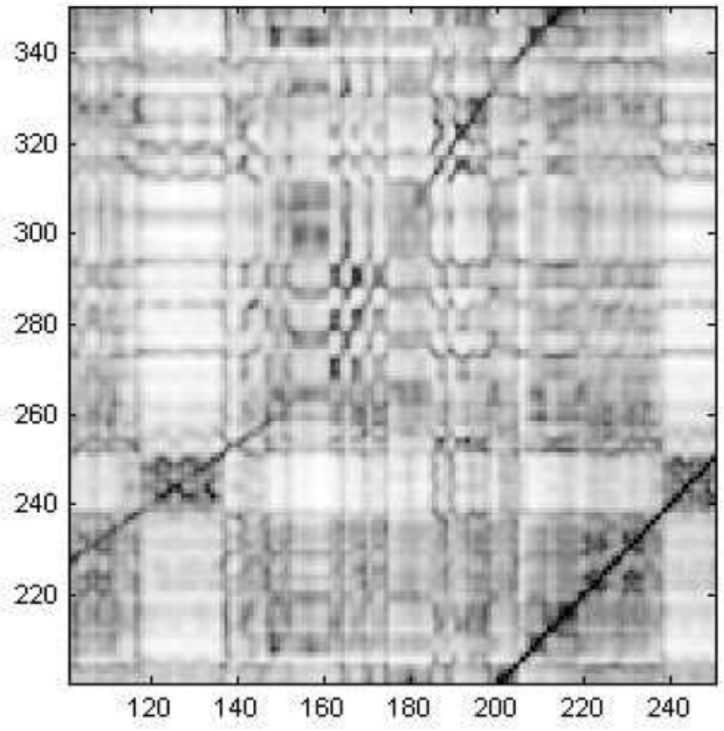
$$\mathbf{S}_L(n,m) := \frac{1}{L}\sum_{\ell=0}^{L-1}\mathbf{S}(n+\ell,m+\ell)$$

- Comparison of entire sequences
- L = length of sequences
- $\mathbf{S}_L$ = enhanced SSM

⇝ smoothing effect

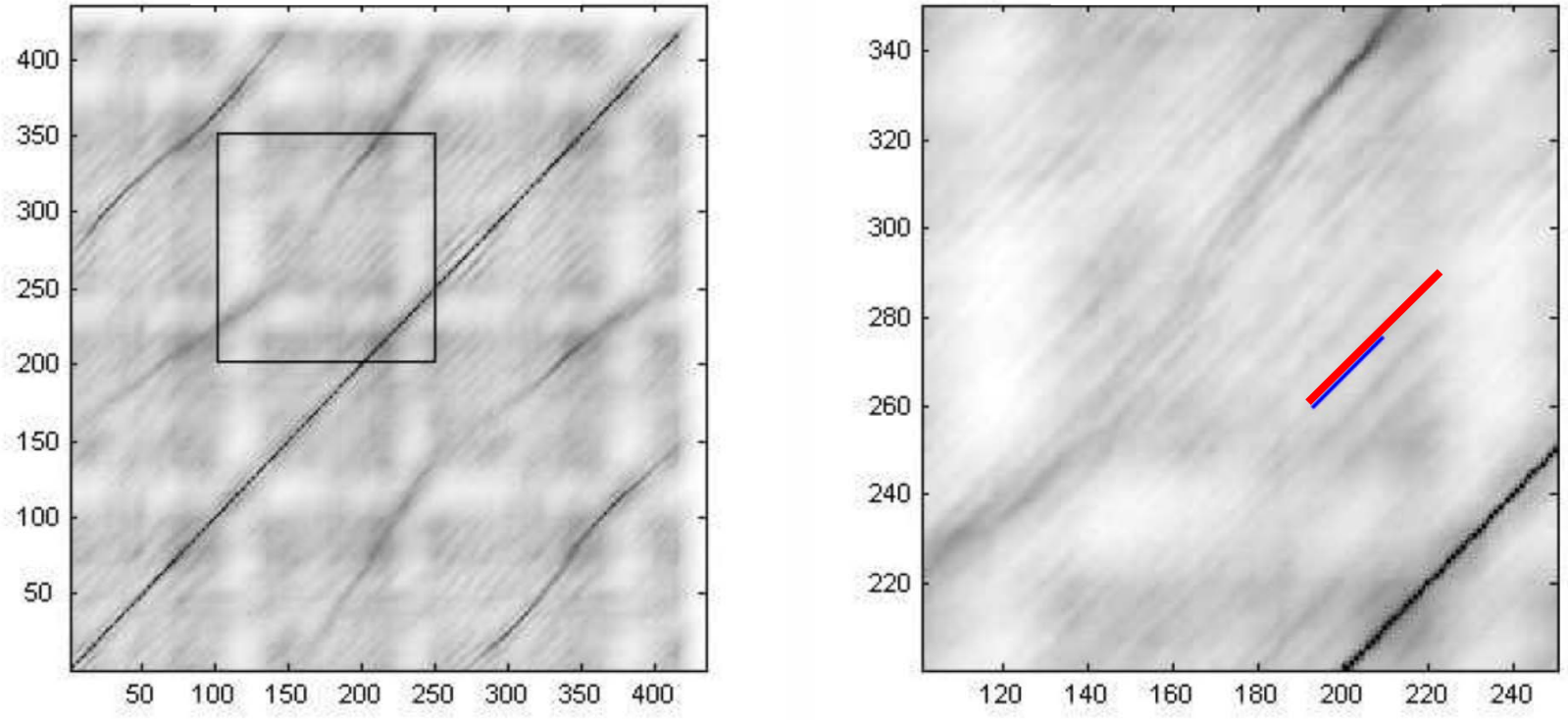
SSM Enhancement





SSM $\mathbf{S}$

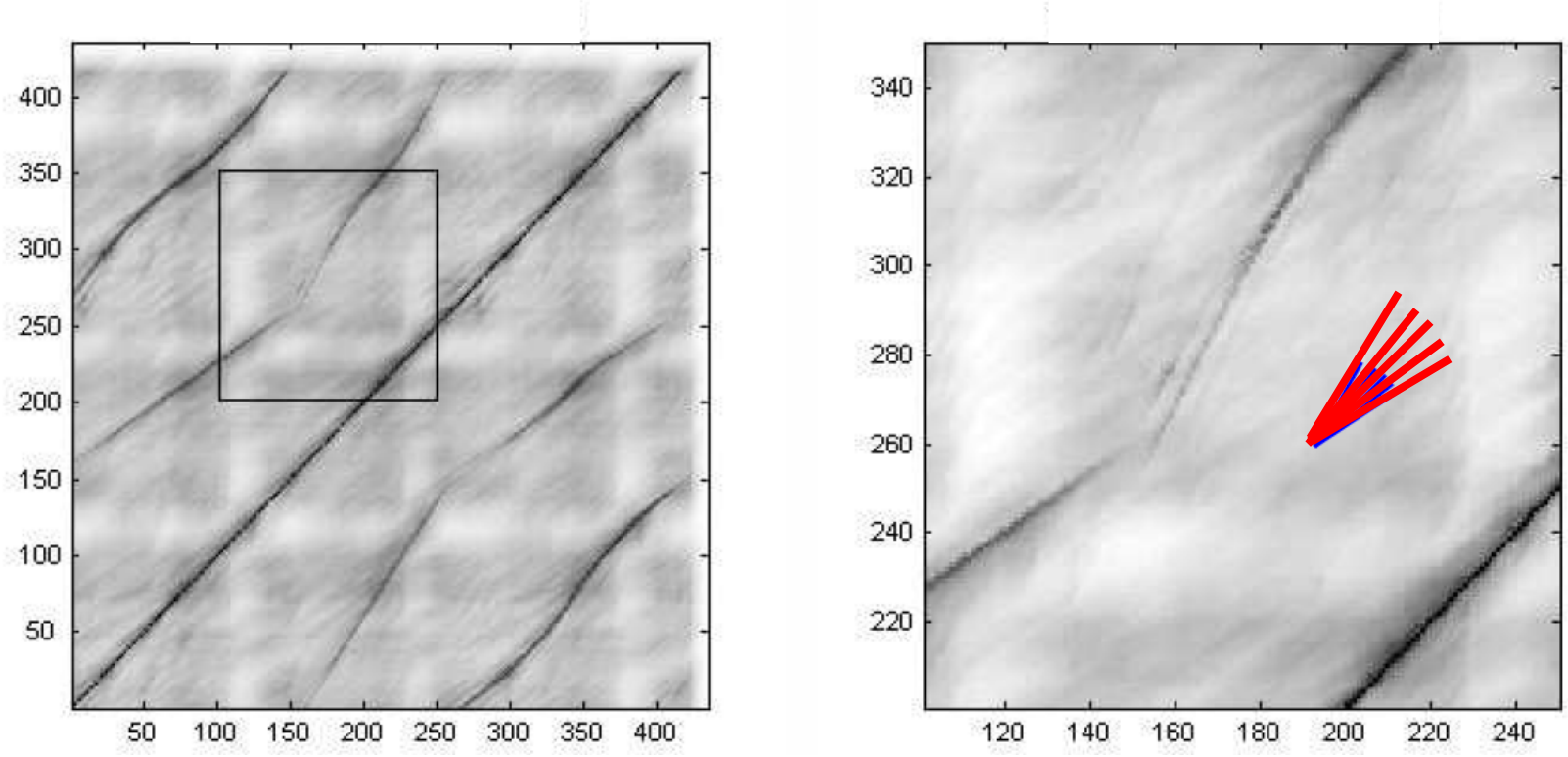
SSM Enhancement



Enhanced SSM $\mathbf{S}_L$ with $L = 20$

Filtering along main diagonal

SSM Enhancement



Enhanced SSM $\mathbf{S}_{L,\Theta}$ with $L = 20$

Filtering along 8 different directions and minimizing

SSM Enhancement

Idea: Smoothing along various directions
and minimizing over all directions

$$\Theta = \{0.66, 0.81, 1.00, 1.22, 1.50\}$$

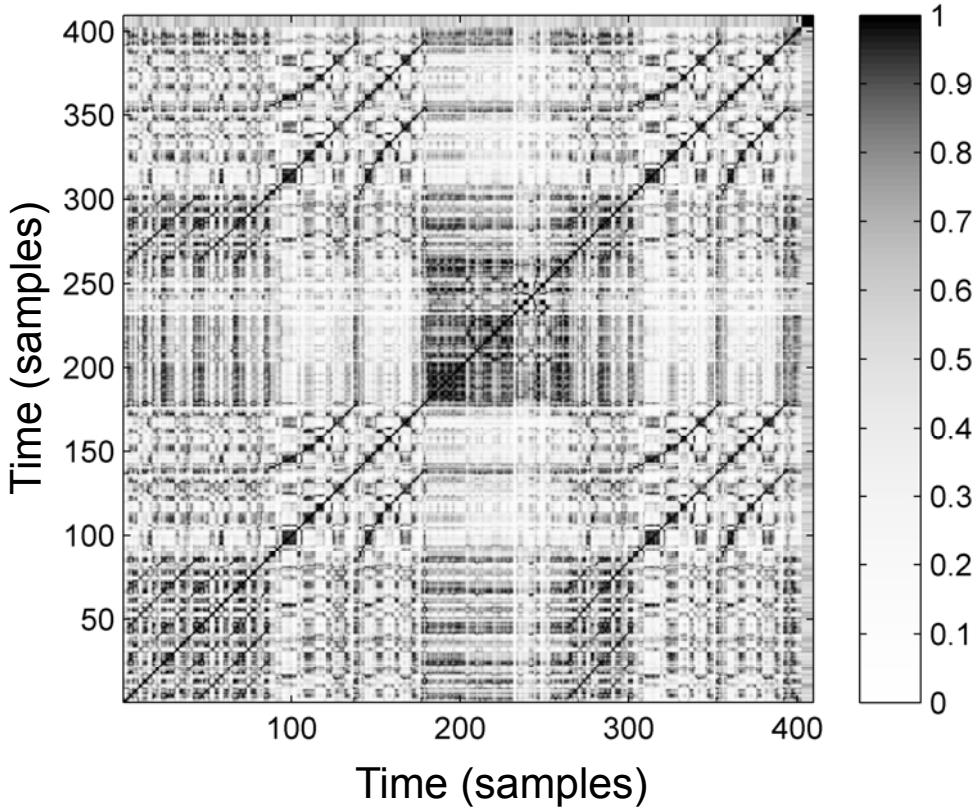
$$\mathbf{S}_{L,\theta}(n,m) := \frac{1}{L}\sum_{\ell=0}^{L-1}\mathbf{S}(n+\ell, m+[\ell\cdot\theta])$$

$$\mathbf{S}_{L,\Theta}(n,m) := \max_{\theta\in\Theta}\mathbf{S}_{L,\theta}(n,m)$$

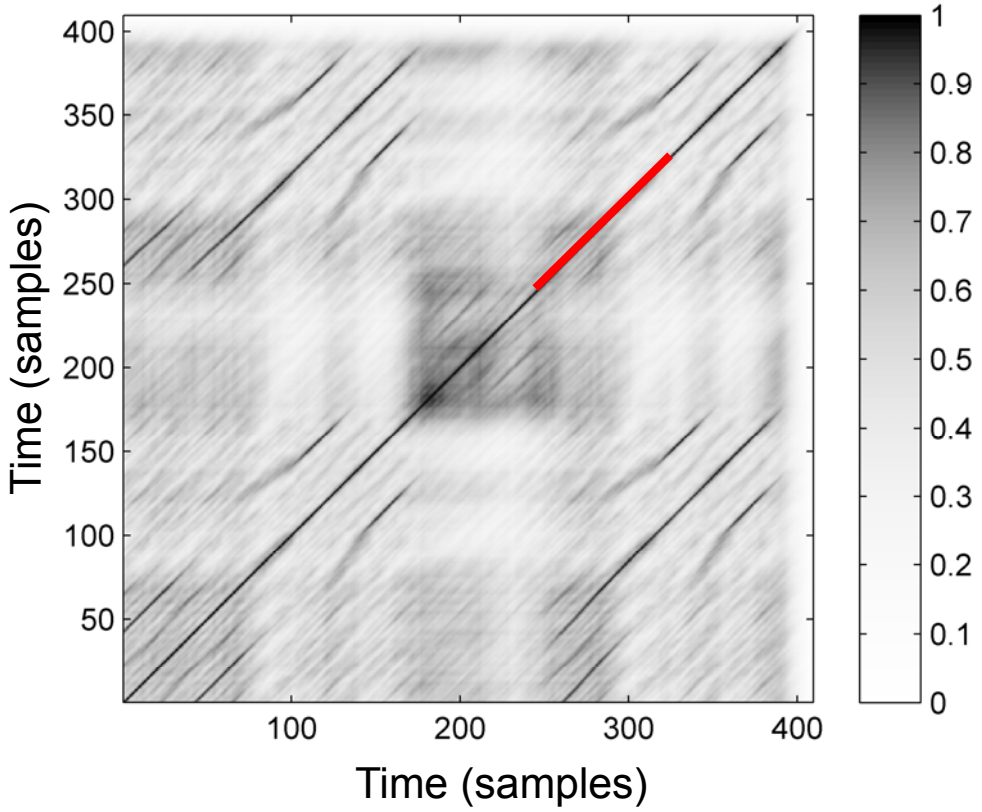
⇝ Tempo changes of -50 to +50 percent

SSM Enhancement

Path Enhancement



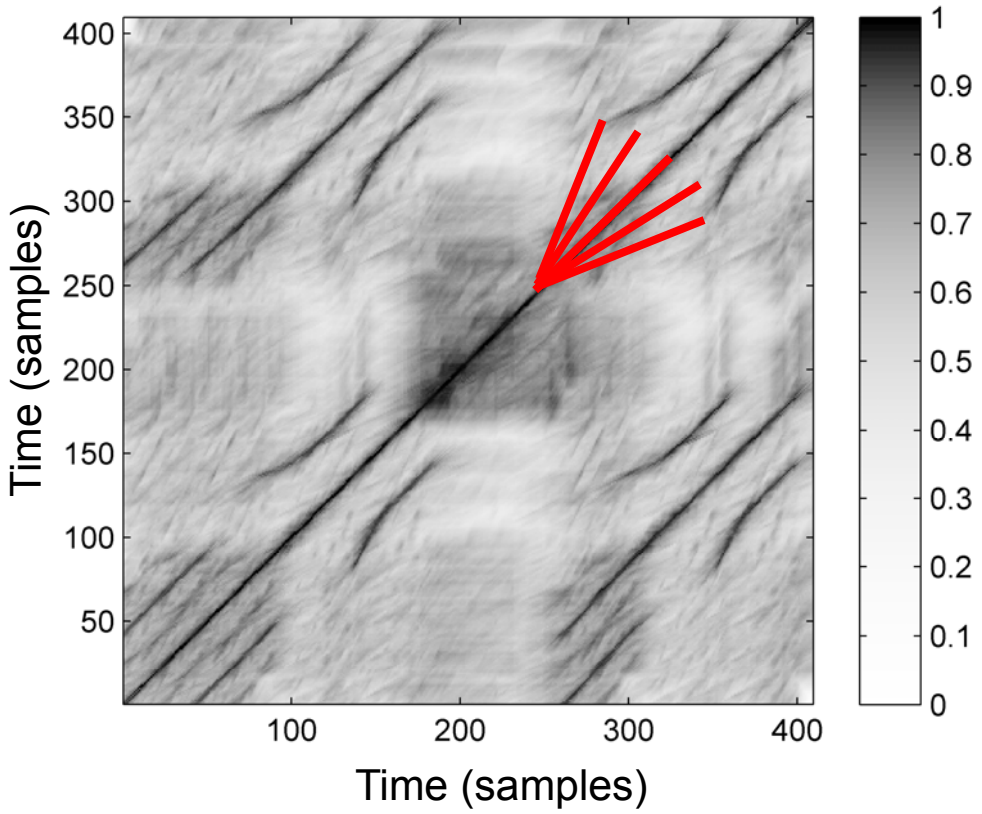
SSM Enhancement



Path Enhancement

- Diagonal smoothing

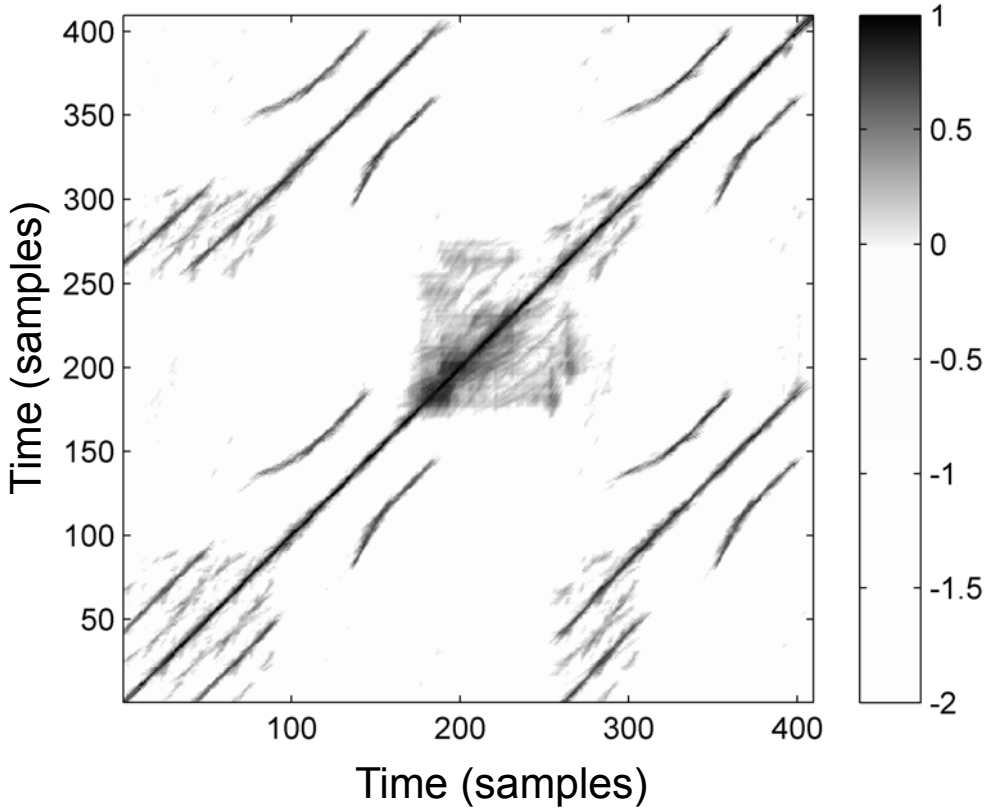
SSM Enhancement



Path Enhancement

- Diagonal smoothing
- Multiple filtering

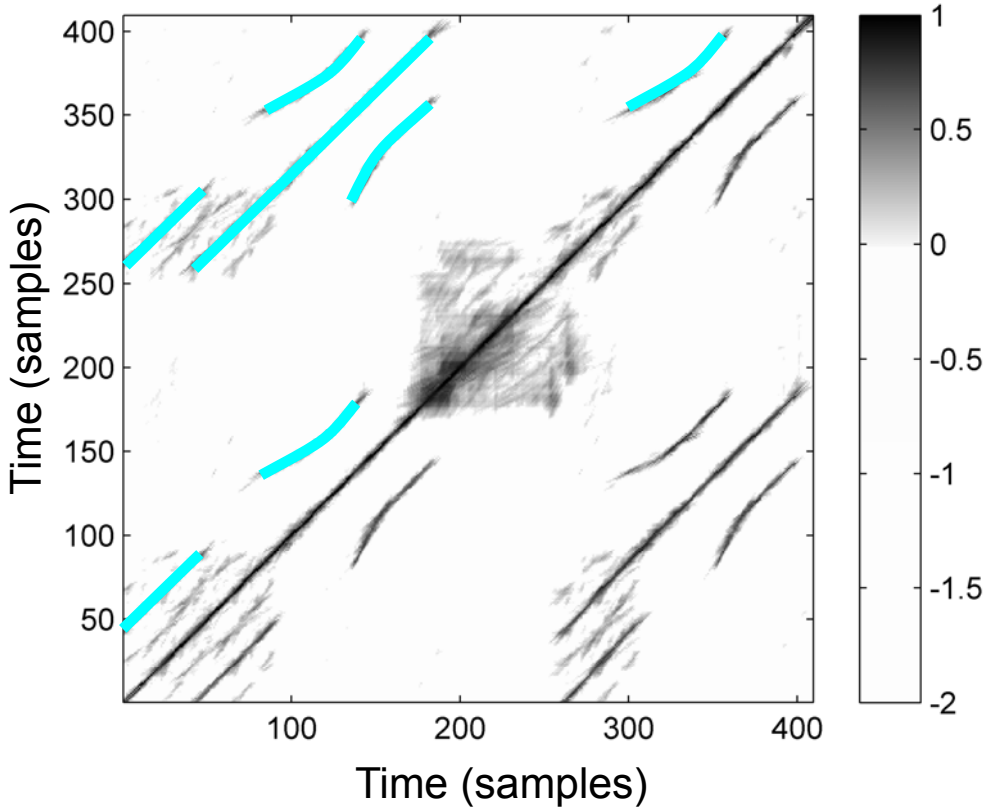
SSM Enhancement



Path Enhancement

- Diagonal smoothing
- Multiple filtering
- Thresholding (relative)
- Scaling & penalty

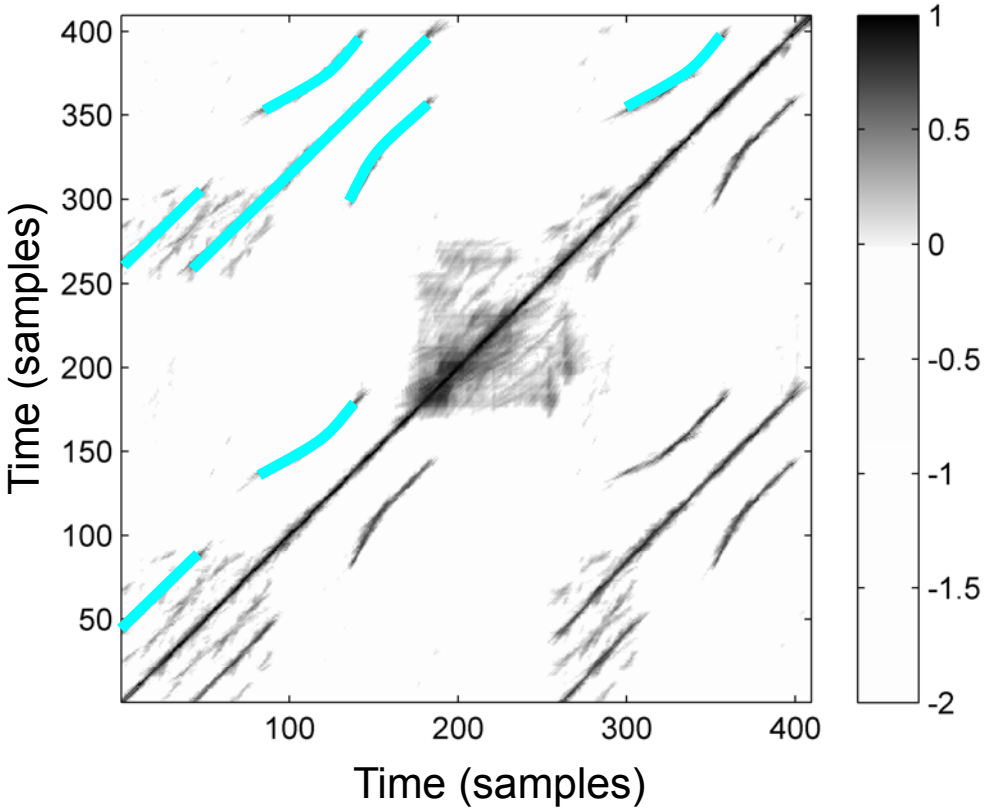
SSM Enhancement



Further Processing

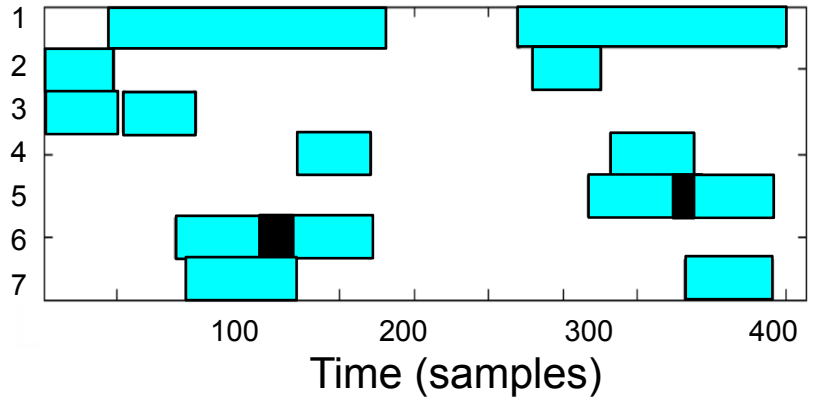
- Path extraction

SSM Enhancement

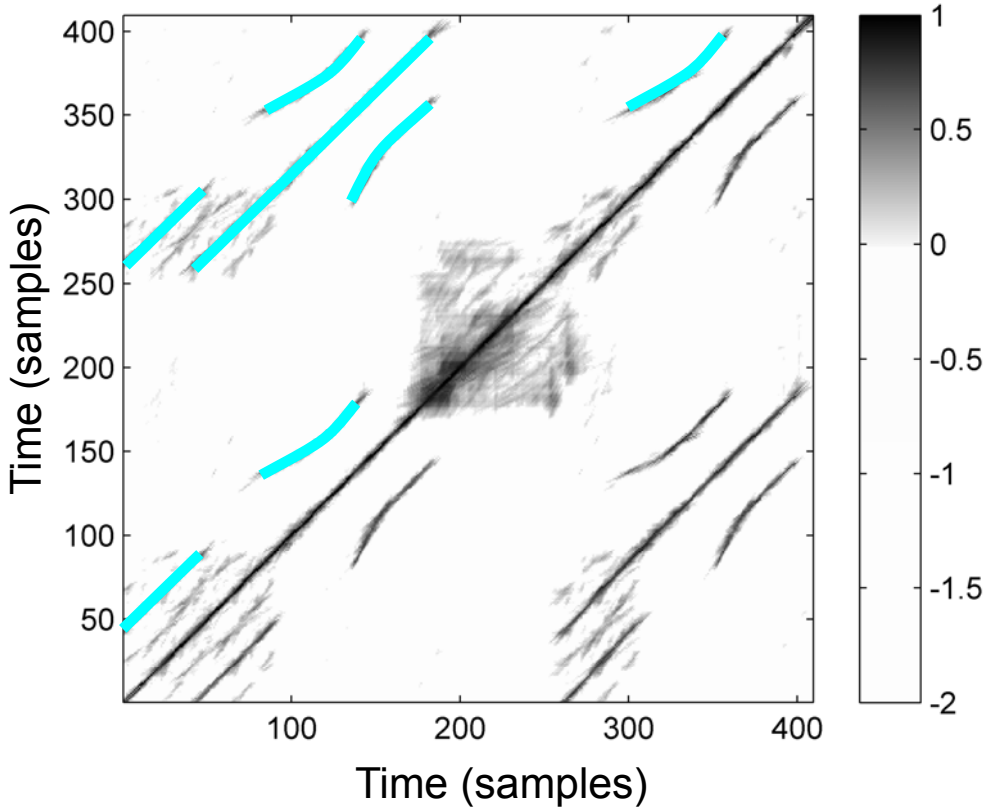


Further Processing

- Path extraction
- Pairwise relations

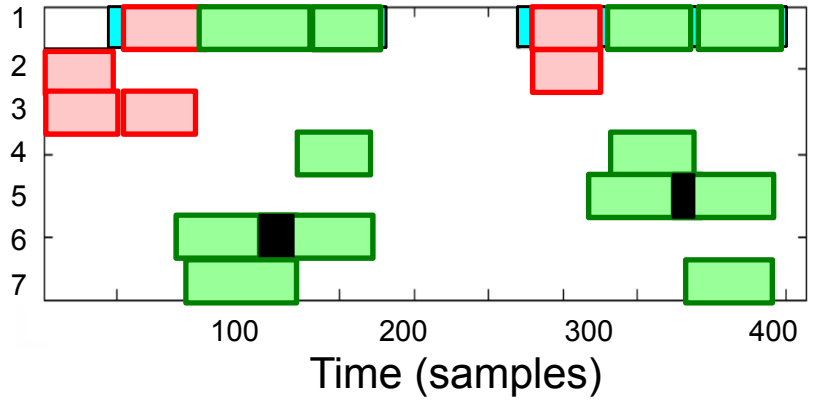


SSM Enhancement

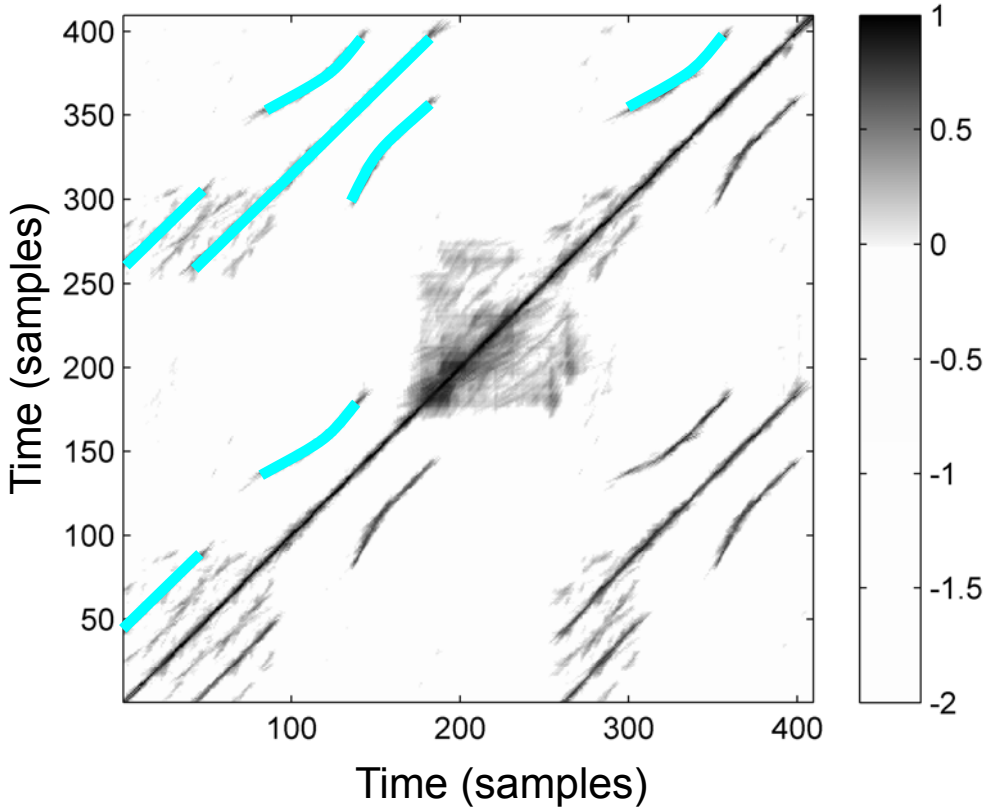


Further Processing

- Path extraction
- Pairwise relations
- Grouping (transitivity)



SSM Enhancement



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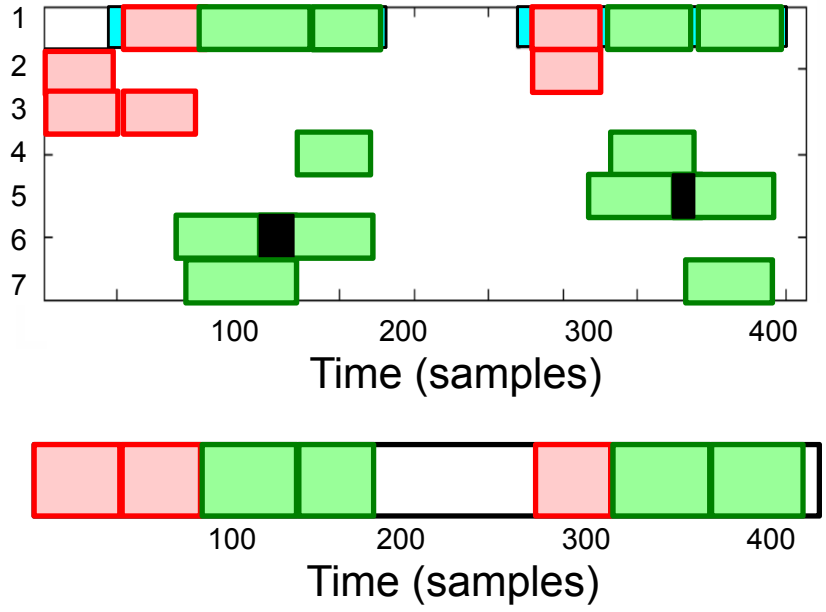
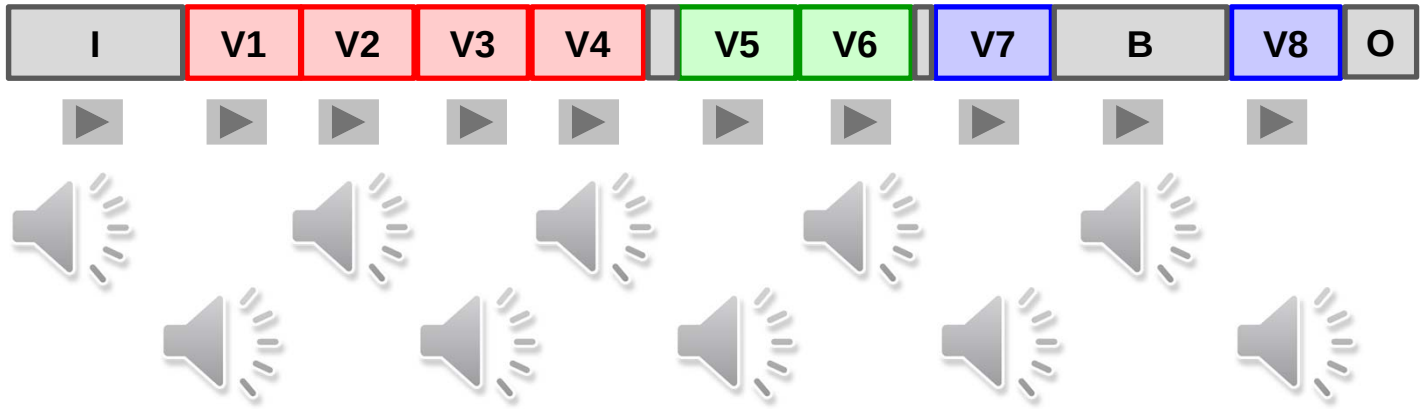


SSM Enhancement

Example: Zager & Evans “In The Year 2525”



SSM Enhancement

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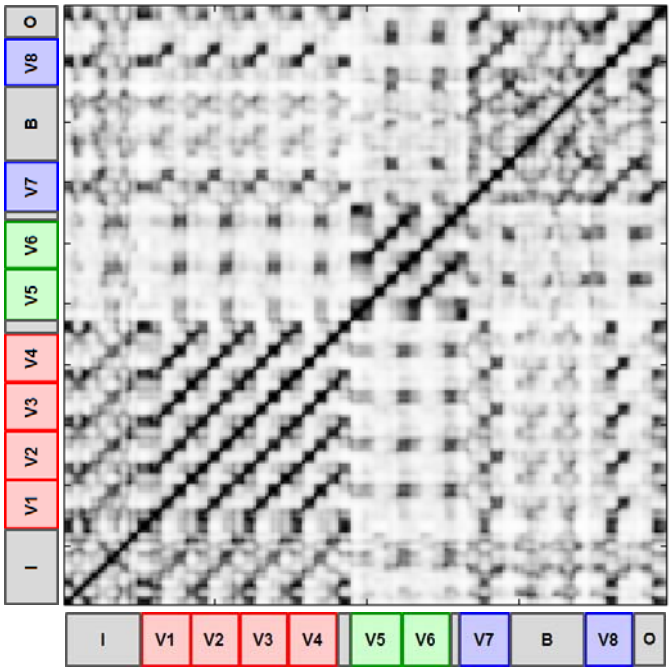
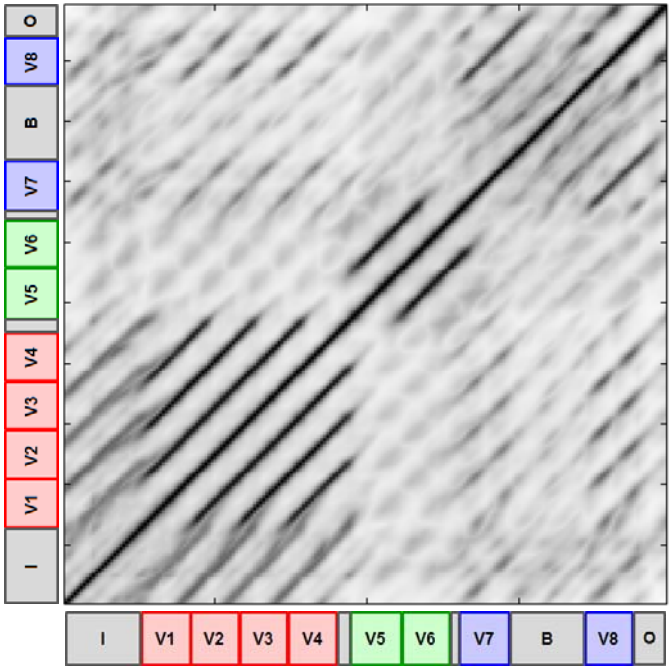


SSM Enhancement

Example: Zager & Evans “In The Year 2525”

Missing relations because of transposed sections

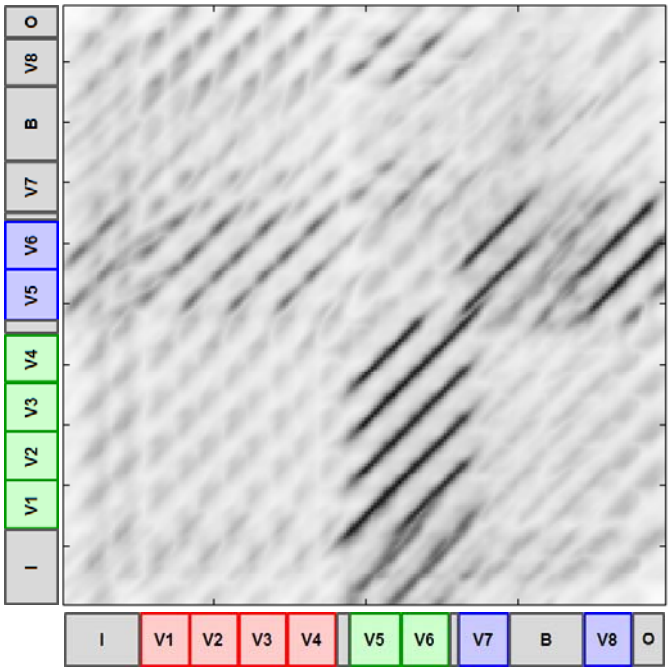


SSM Enhancement

Example: Zager & Evans “In The Year 2525”

Idea: Cyclic shift of one of the chroma sequences

One semitone up

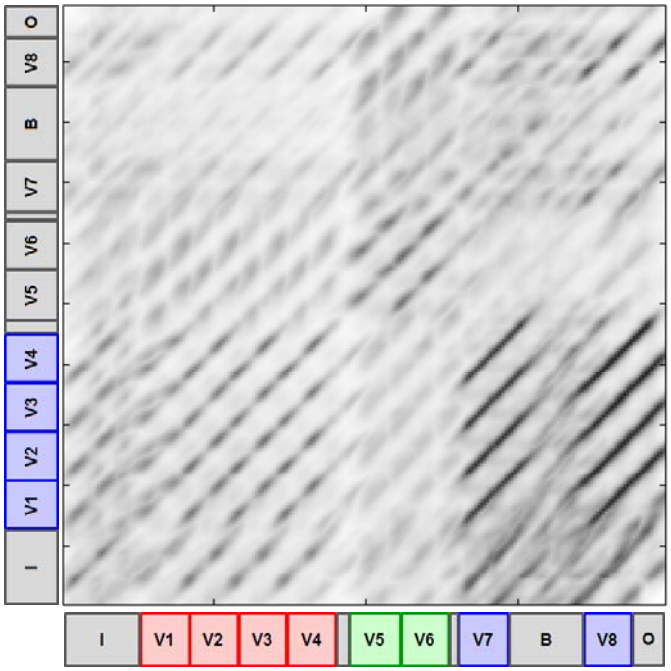


SSM Enhancement

Example: Zager & Evans “In The Year 2525”

Idea: Cyclic shift of one of the chroma sequences

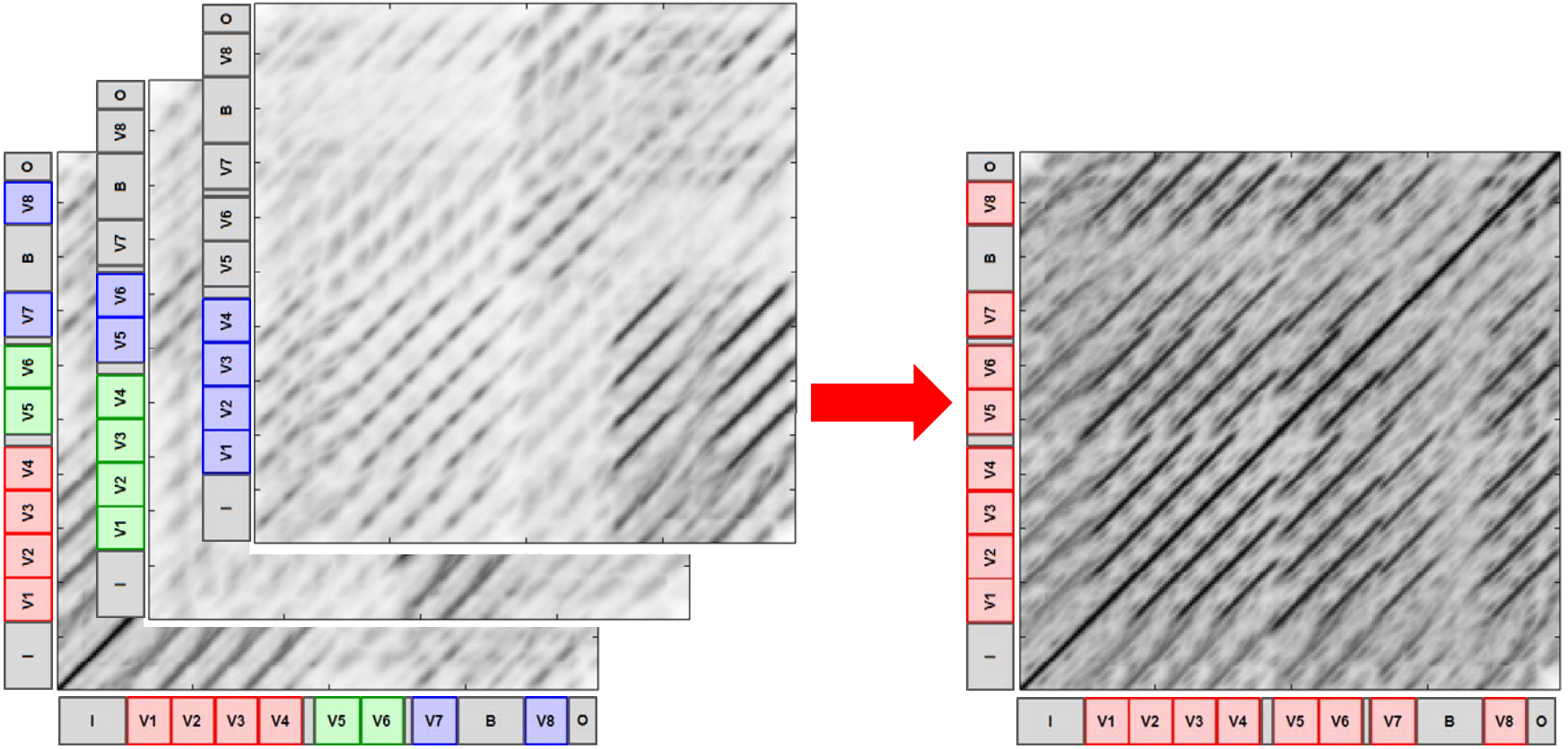
Two semitones up



SSM Enhancement

Example: Zager & Evans “In The Year 2525”

Idea: Overlay & Maximize ⟶ Transposition-invariant SSM

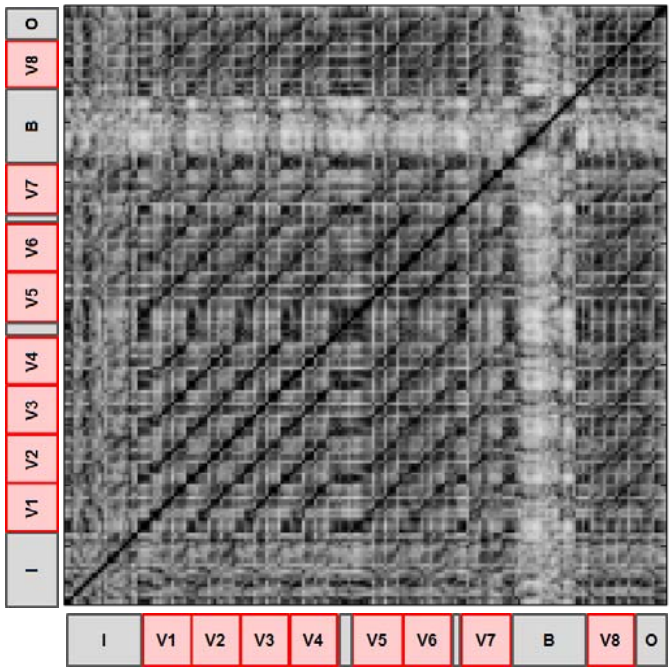


SSM Enhancement

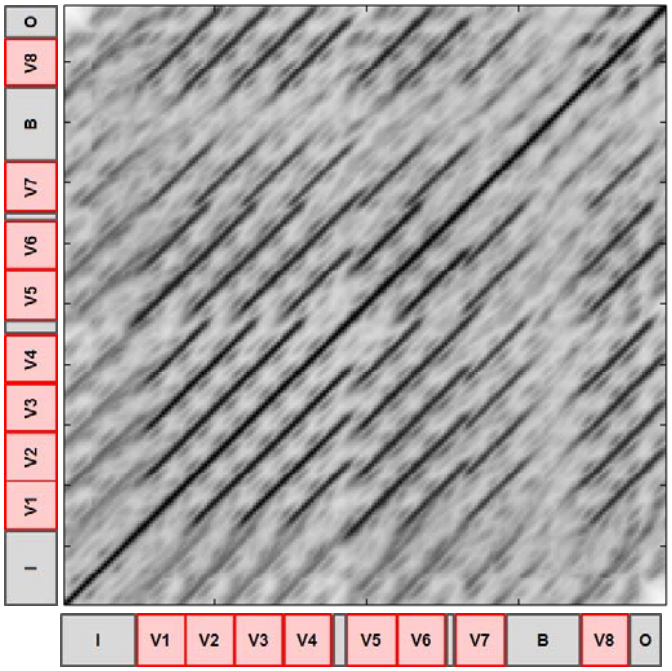
Example: Zager & Evans “In The Year 2525”

Note: Order of enhancement steps important!

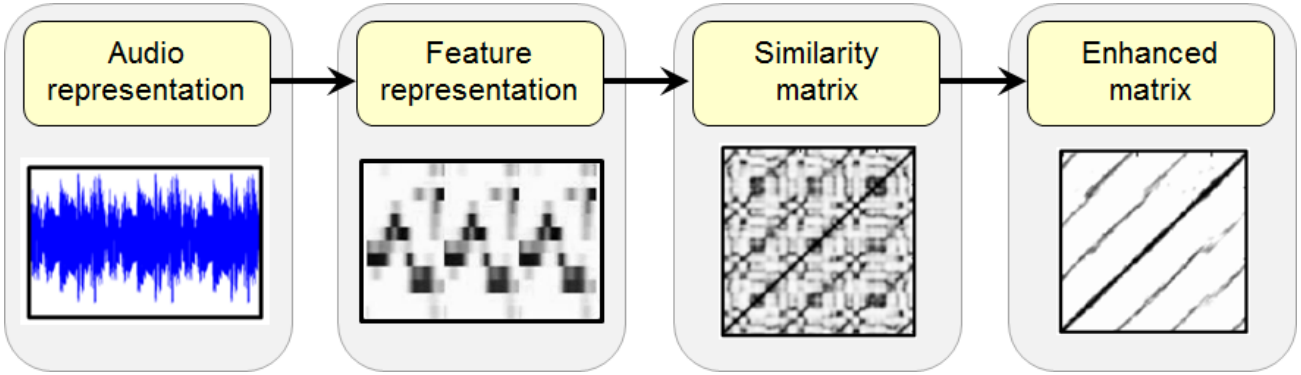
Maximization



Smoothing & Maximization



Similarity Matrix Toolbox



Meinard Müller, Nanzhu Jiang, Harald Grohganz
SM Toolbox: MATLAB Implementations for Computing and Enhancing Similarity Matrices

http://www.audiolabs-erlangen.de/resources/MIR/SMtoolbox/

Overview

- Introduction
- Feature Representations
- Self-Similarity Matrices
- Audio Thumbnailing
- Novelty-based Segmentation

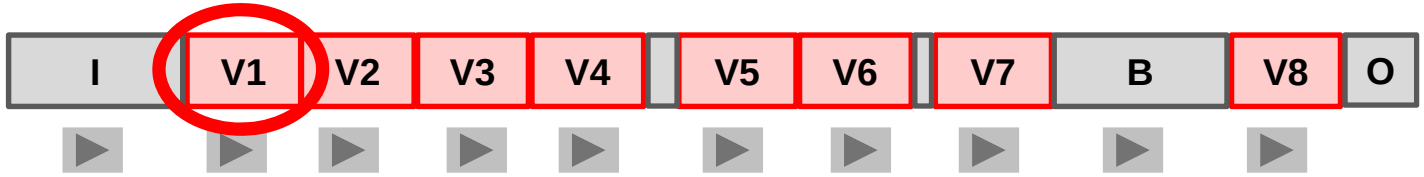
Thanks:

- Jiang, Grosche
- Peeters
- Cooper, Foote
- Goto
- Levy, Sandler
- Mauch
- Sapp

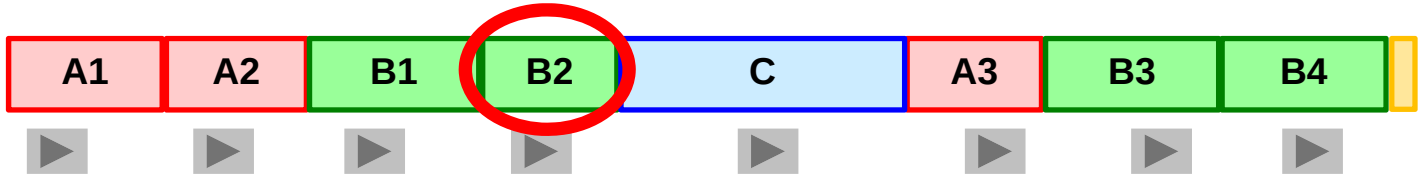
Audio Thumbnailing

General goal: Determine the most representative section ("Thumbnail") of a given music recording.

Example: Zager & Evans "In The Year 2525"



Example: Brahms Hungarian Dance No. 5 (Ormandy)



Thumbnail is often assumed to be the most repetitive segment

Audio Thumbnailing

Two steps

1. Path extraction

2. Grouping

Both steps are problematic!

- Paths of poor quality (fragmented, gaps)
- Block-like structures
- Curved paths

- Noisy relations
  (missing, distorted, overlapping)
- Transitivity computation difficult

Main idea: Do both, path extraction and grouping, jointly

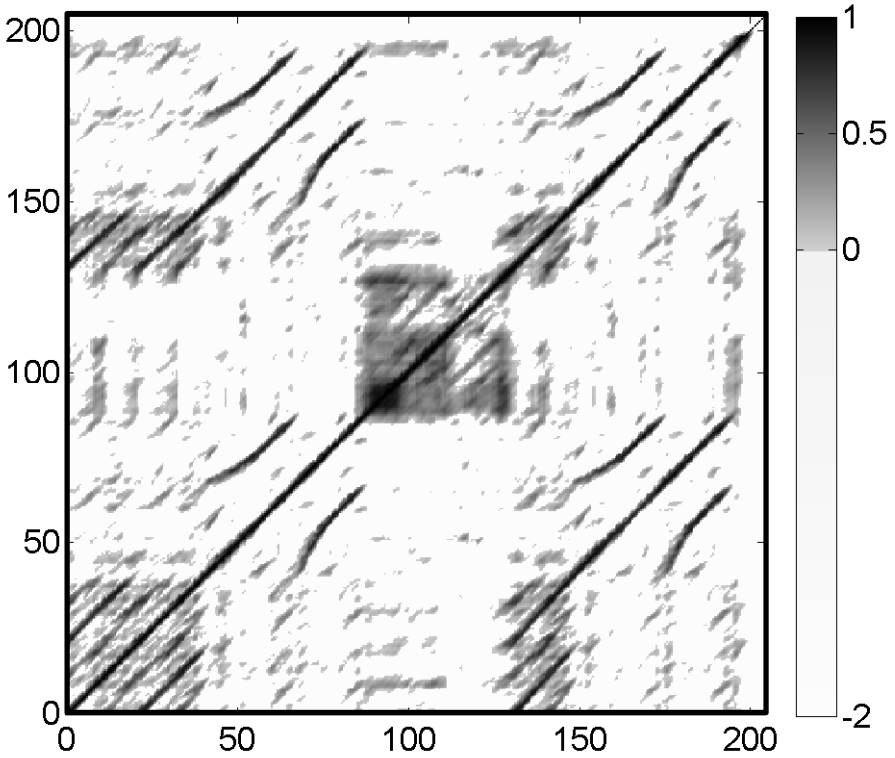
- One optimization scheme for both steps
- Stabilizing effect
- Efficient

Audio Thumbnailing

Main idea: Do both path extraction and grouping jointly

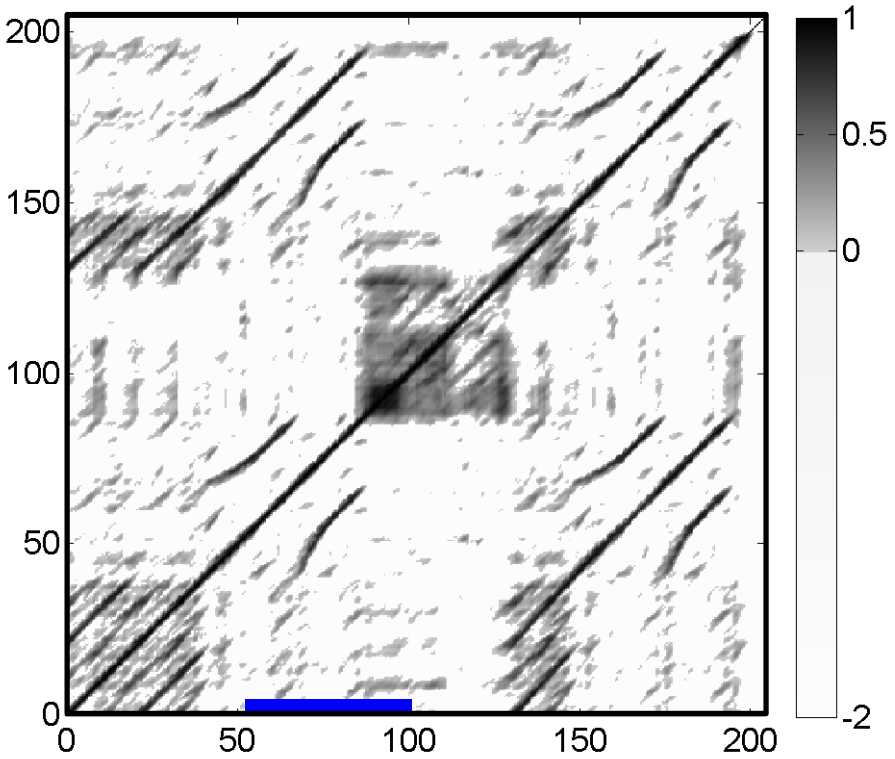
- For each audio segment we define a fitness value
- This fitness value expresses “how well” the segment explains the entire audio recording
- The segment with the highest fitness value is considered to be the thumbnail
- As main technical concept we introduce the notion of a path family

Fitness Measure



Enhanced SSM

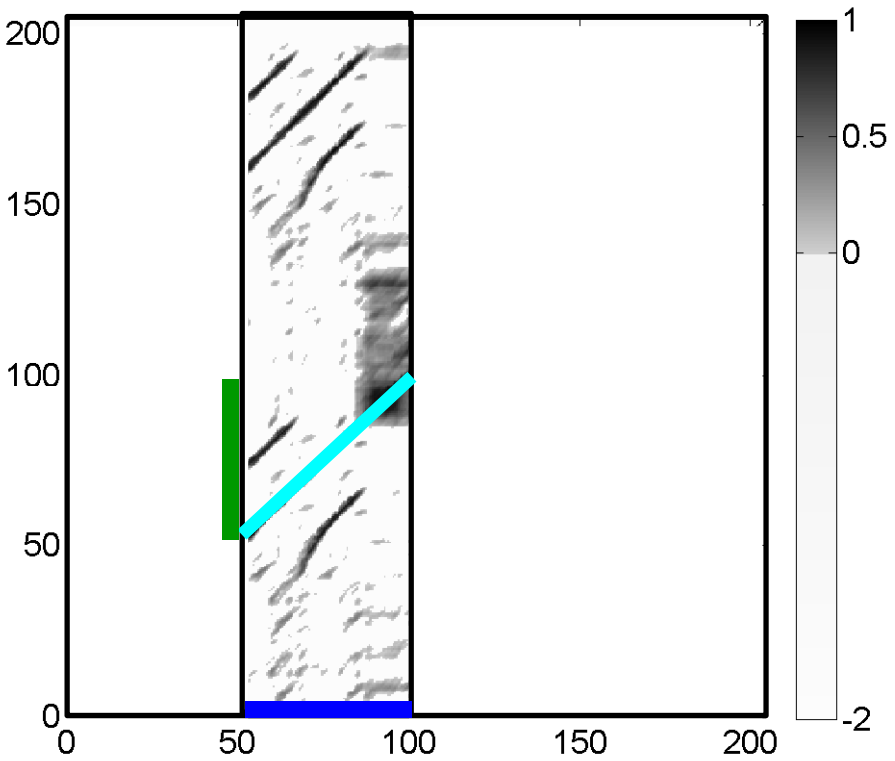
Fitness Measure



Path over segment

- Consider a fixed segment

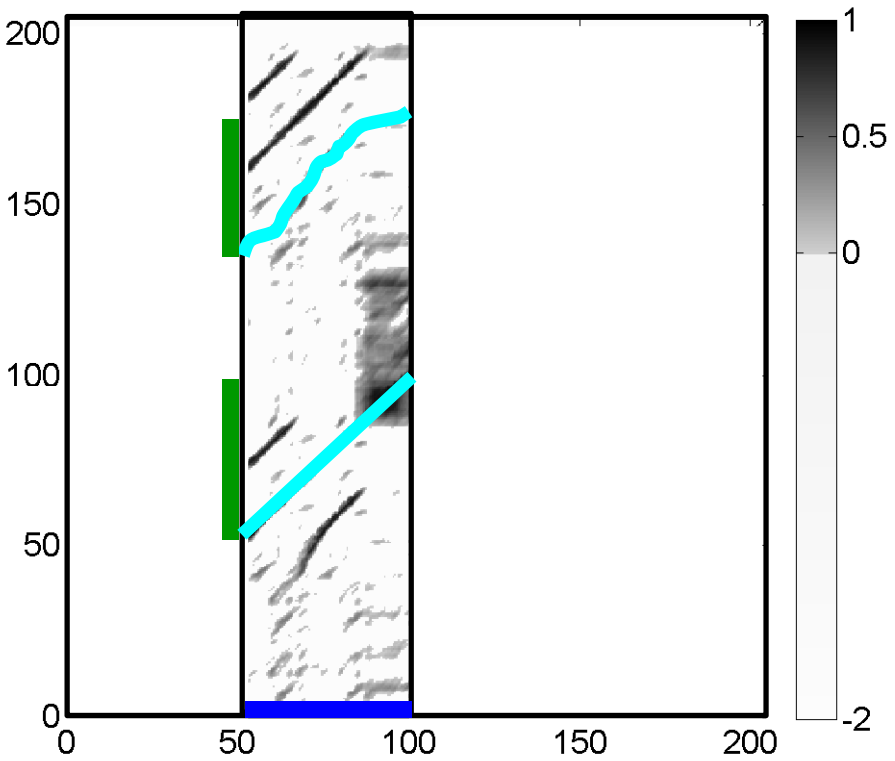
Fitness Measure



Path over segment

- Consider a fixed segment
- Path over segment
- Induced segment
- Score is high

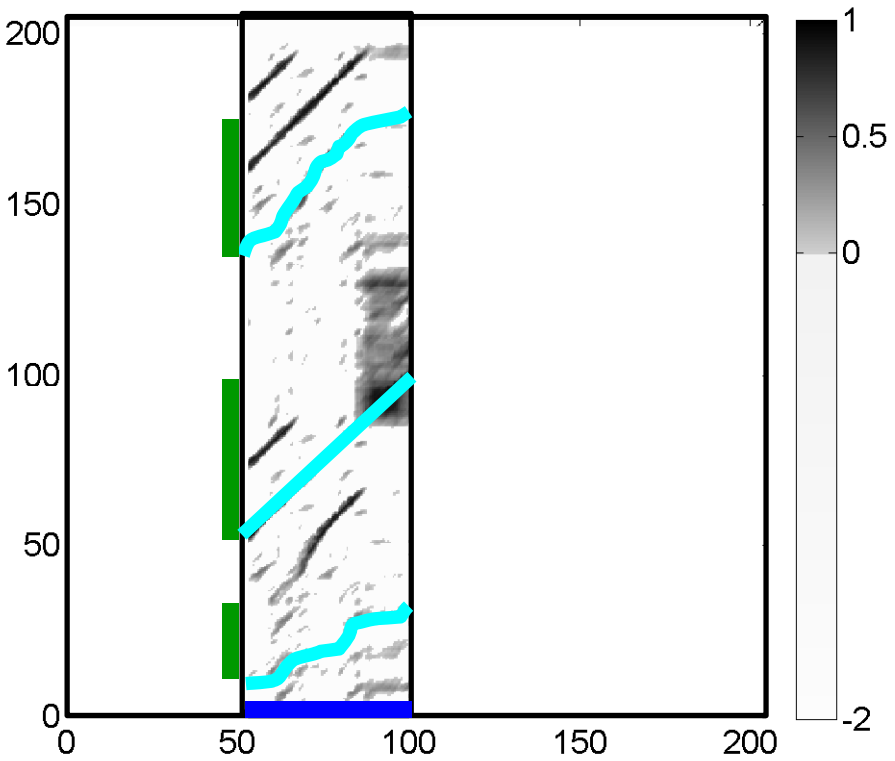
Fitness Measure



Path over segment

- Consider a fixed segment
- Path over segment
- Induced segment
- Score is high
- A second path over segment
- Induced segment
- Score is not so high

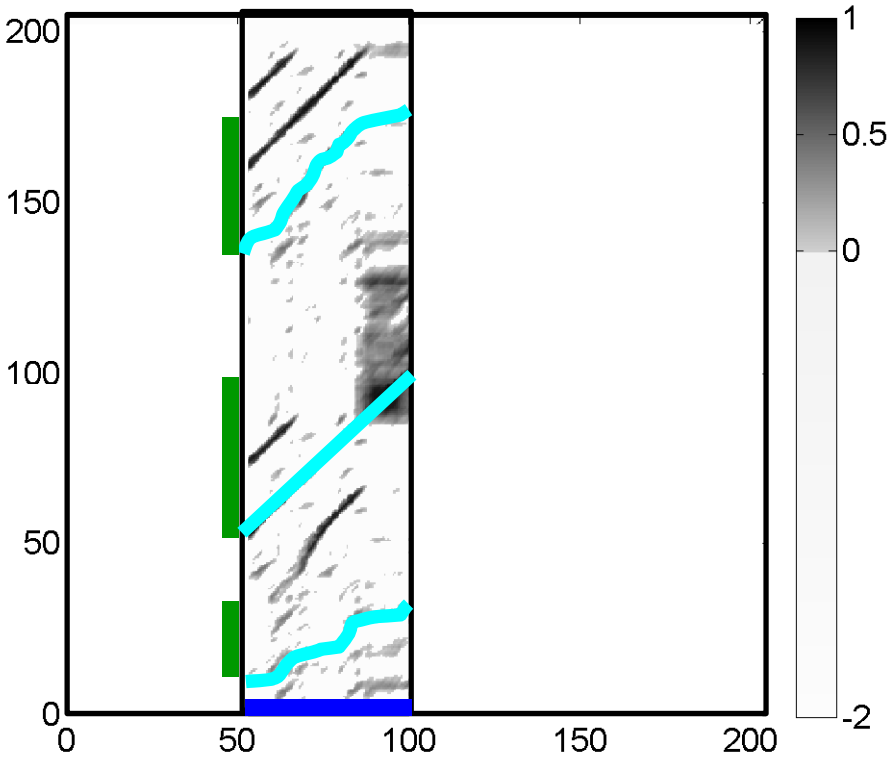
Fitness Measure



Path over segment

- Consider a fixed segment
- Path over segment
- Induced segment
- Score is high
- A second path over segment
- Induced segment
- Score is not so high
- A third path over segment
- Induced segment
- Score is very low

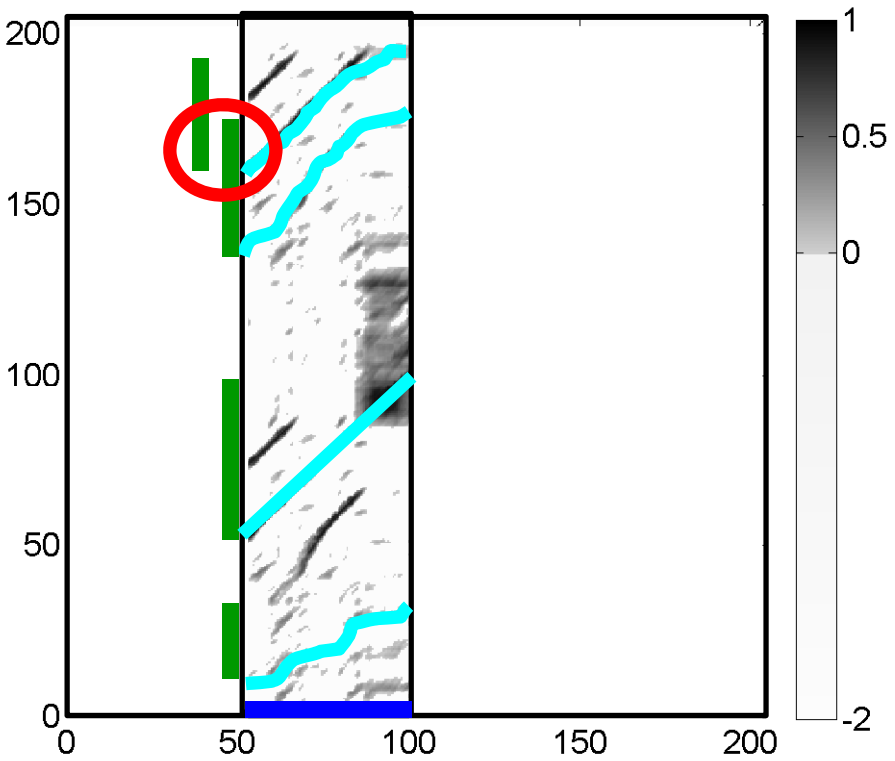
Fitness Measure



Path family

- Consider a fixed segment
- A path family over a segment is a family of paths such that the induced segments do not overlap.

Fitness Measure

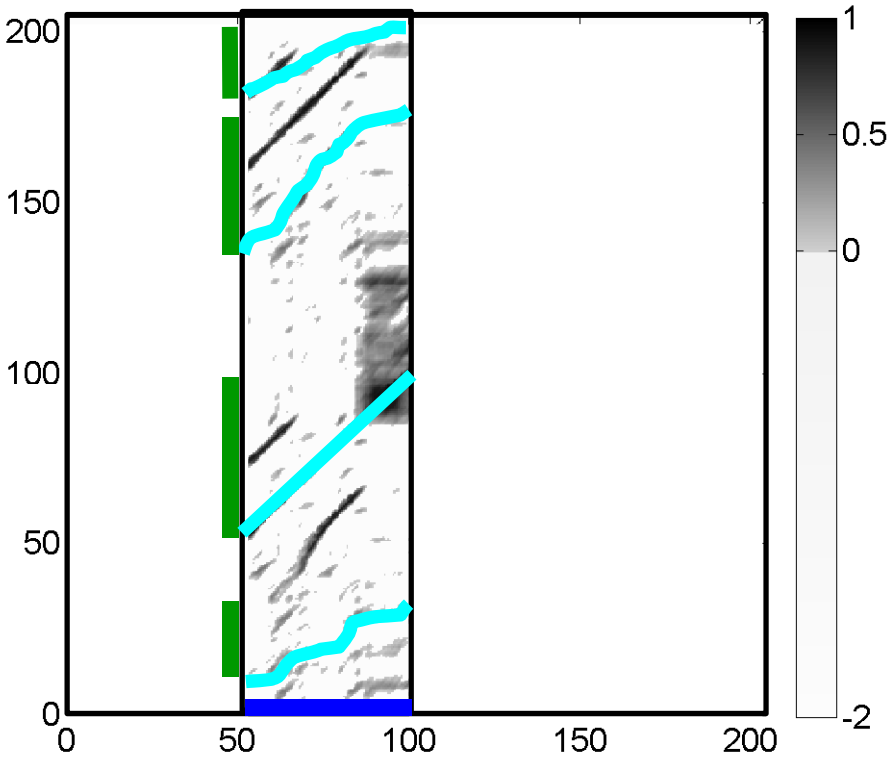


Path family

- Consider a fixed segment
- A path family over a segment is a family of paths such that the induced segments do not overlap.

This is not a path family!

Fitness Measure



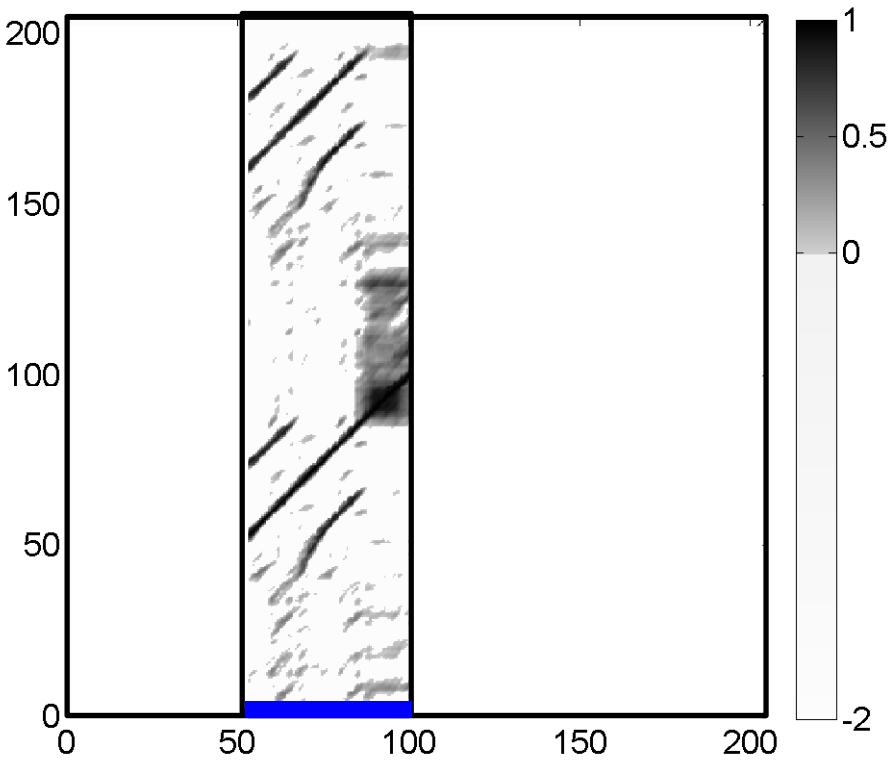
Path family

- Consider a fixed segment
- A path family over a segment is a family of paths such that the induced segments do not overlap.

This is a path family!

(Even though not a good one)

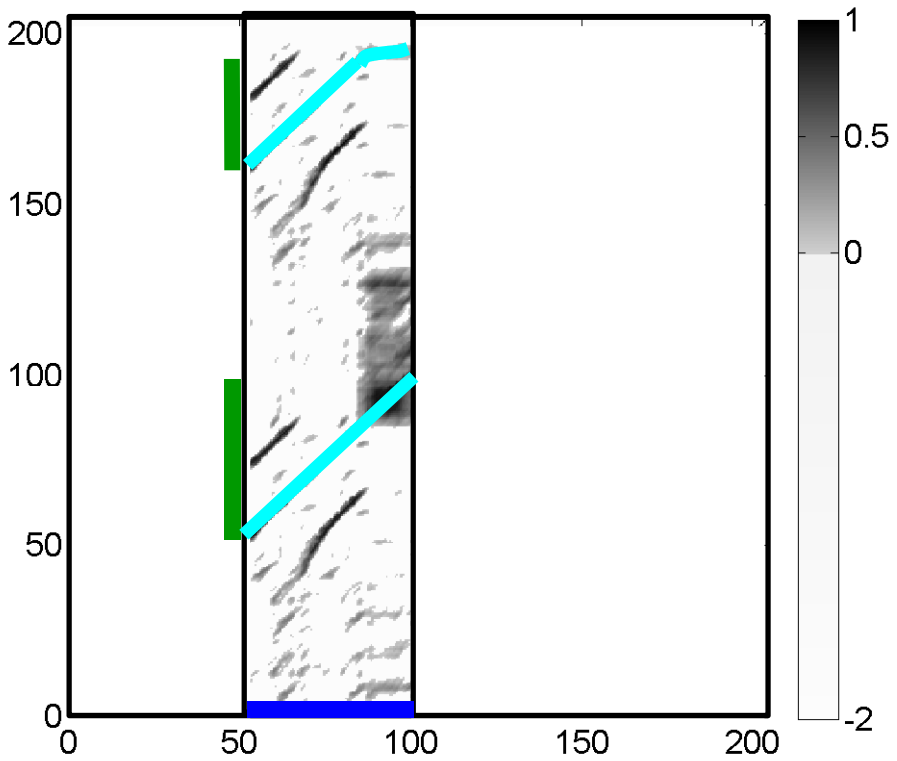
Fitness Measure



Optimal path family

- Consider a fixed segment

Fitness Measure



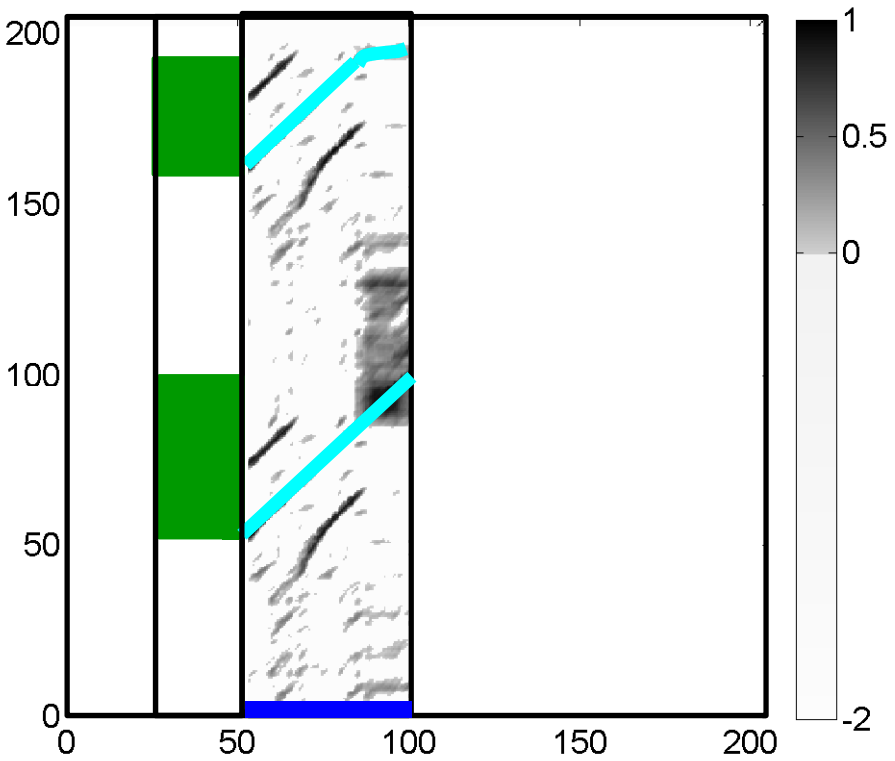
Optimal path family

- Consider a fixed segment
- Consider over the segment the optimal path family, i.e., the path family having maximal overall score.
- Call this value:

Score(segment)

Note: This optimal path family can be computed using dynamic programming.

Fitness Measure



Optimal path family

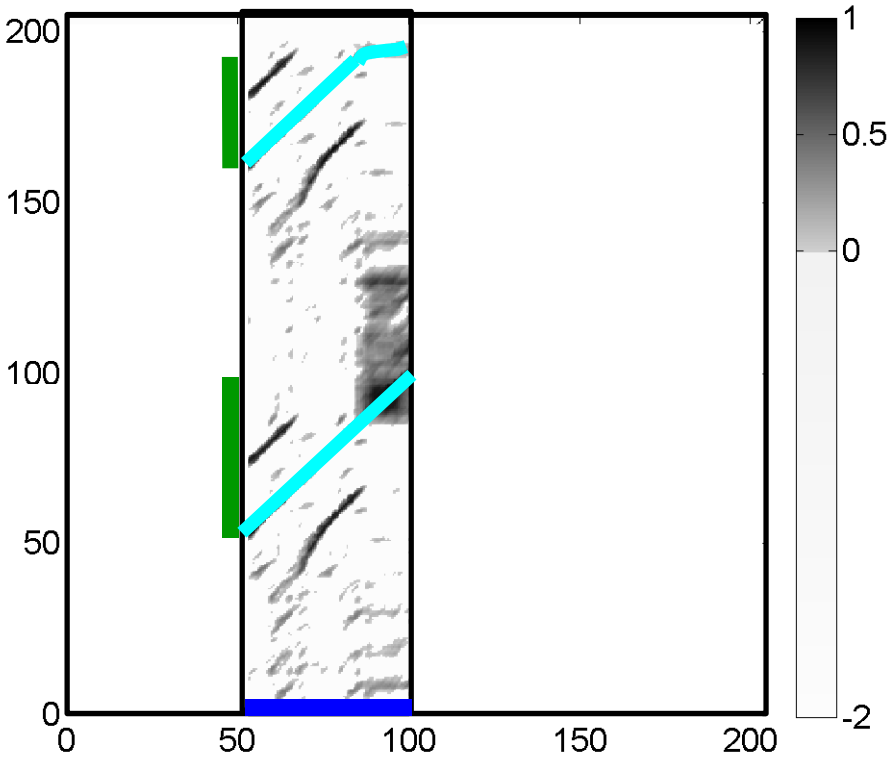
- Consider a fixed segment
- Consider over the segment the optimal path family, i.e., the path family having maximal overall score.
- Call this value:

  Score(segment)

- Furthermore consider the amount covered by the induced segments.
- Call this value:

  Coverage(segment)

Fitness Measure



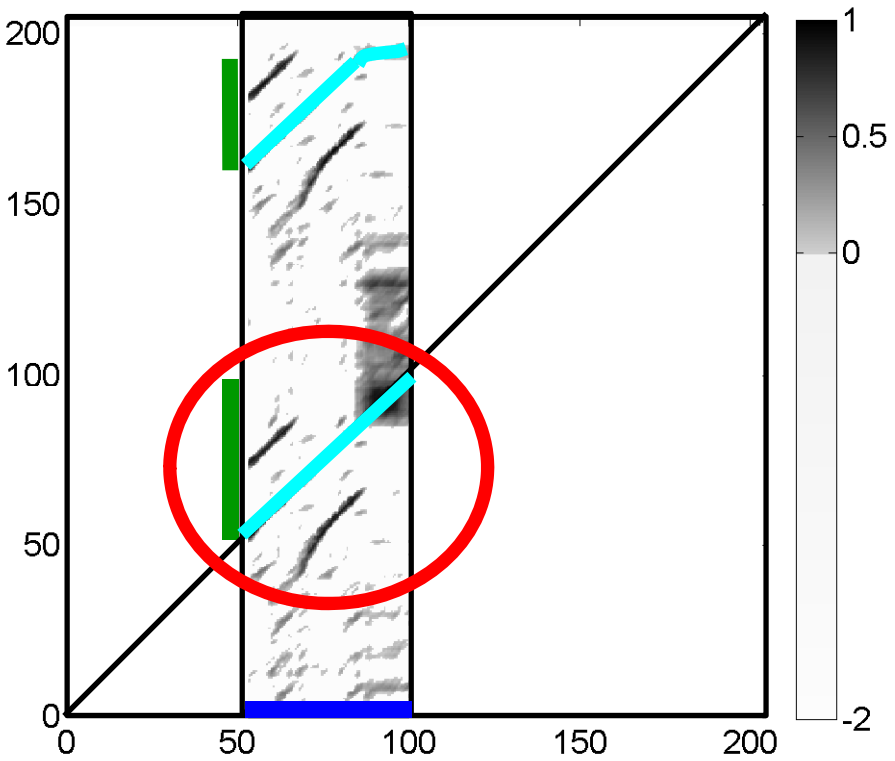
P := Score(segment)

R := Coverage(segment)

Fitness

- Consider a fixed segment

Fitness Measure



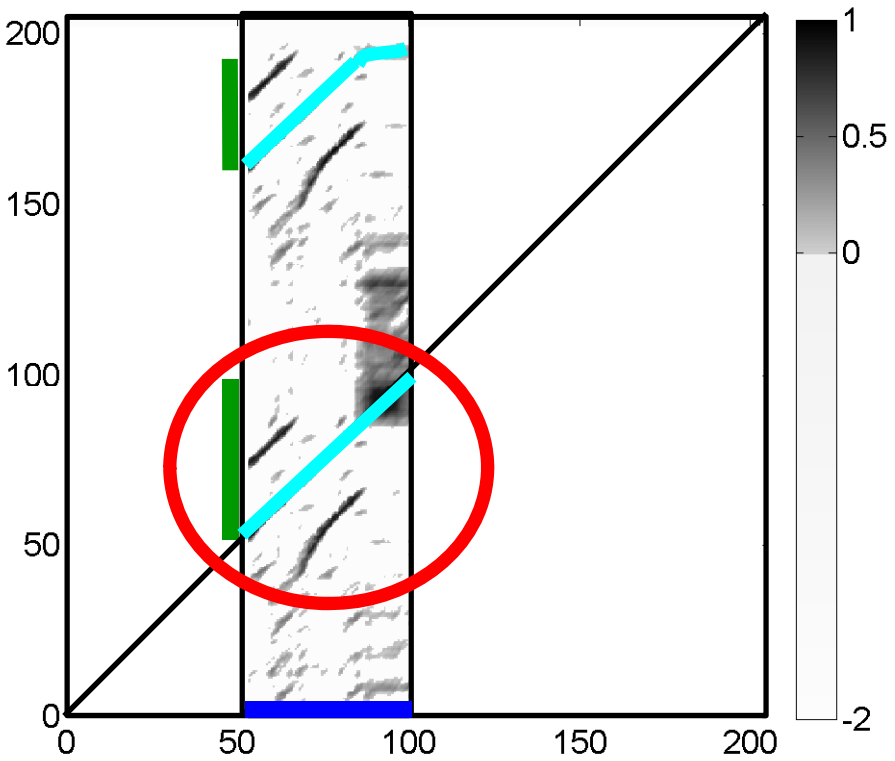
P := Score(segment)

R := Coverage(segment)

Fitness

- Consider a fixed segment
- Self-explanation are trivial!

Fitness Measure



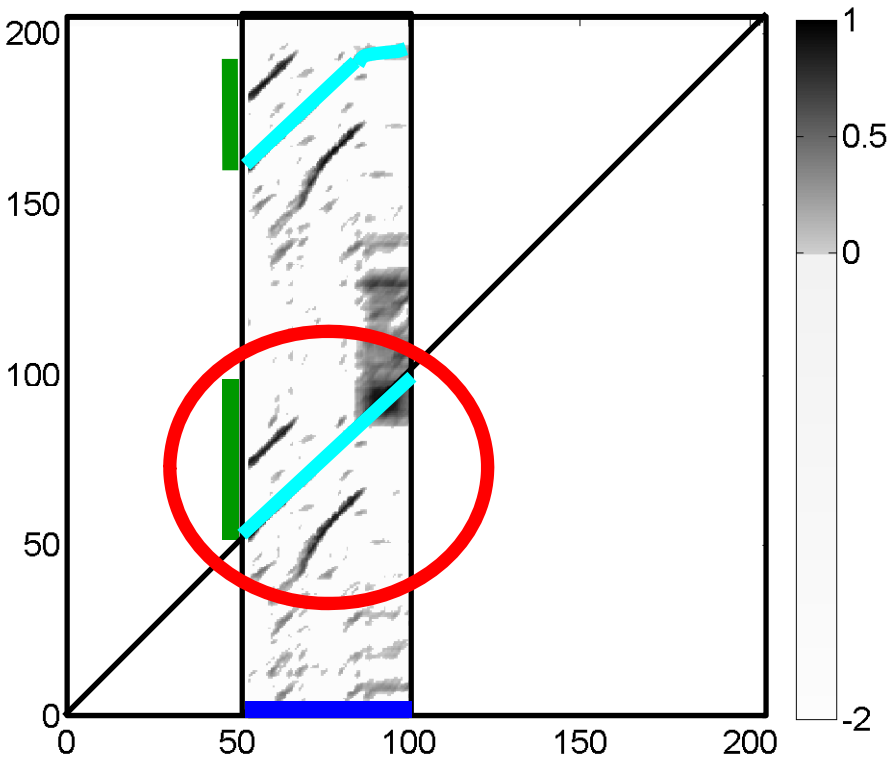
Fitness

- Consider a fixed segment
- Self-explanation are trivial!
- Subtract length of segment

P := Score(segment) - length(segment)

R := Coverage(segment) - length(segment)

Fitness Measure



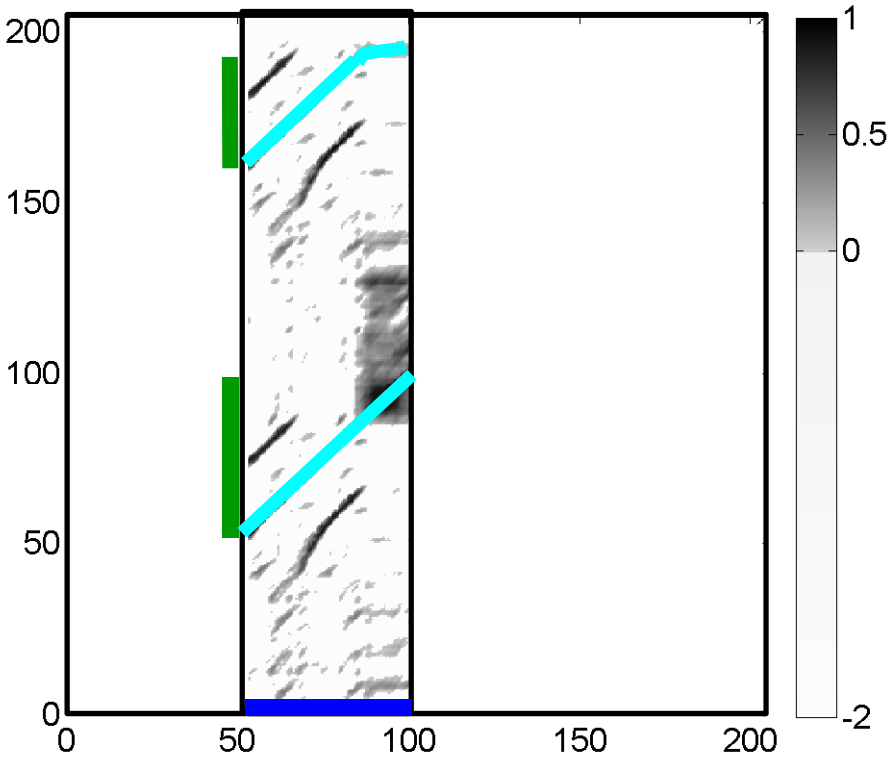
Fitness

- Consider a fixed segment
- Self-explanation are trivial!
- Subtract length of segment
- Normalization

P := Normalize(Score(segment) - length(segment)) $\in [0,1]$

R := Normalize(Coverage(segment) - length(segment)) $\in [0,1]$

Fitness Measure



Fitness

- Consider a fixed segment

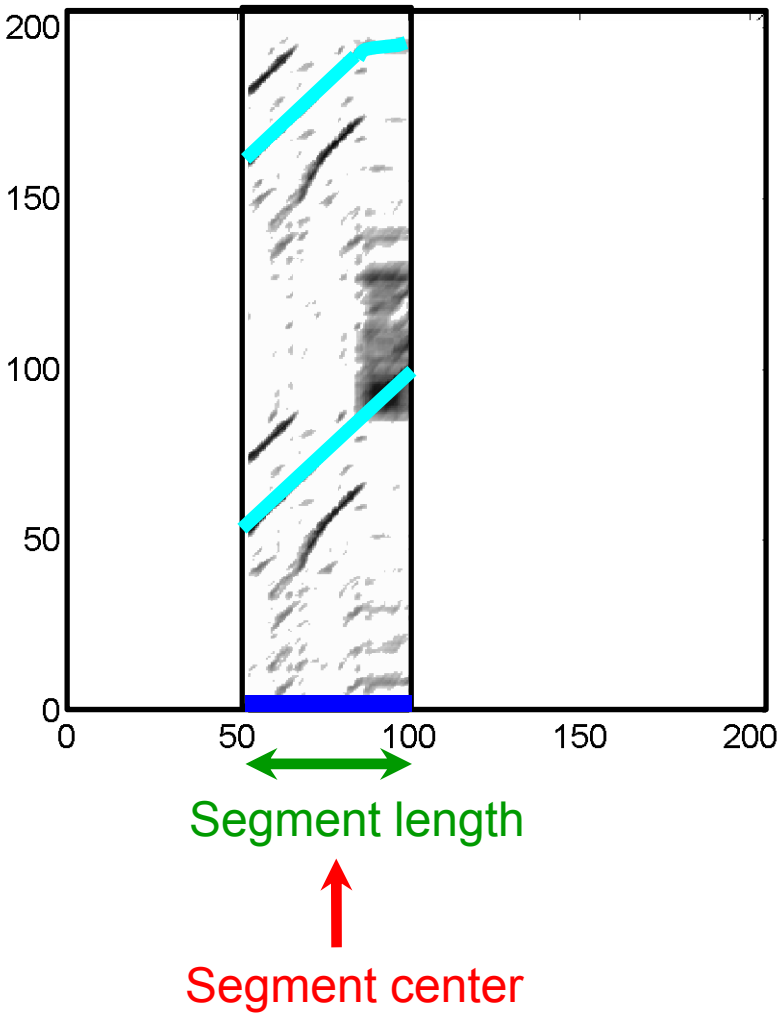
Fitness(segment)

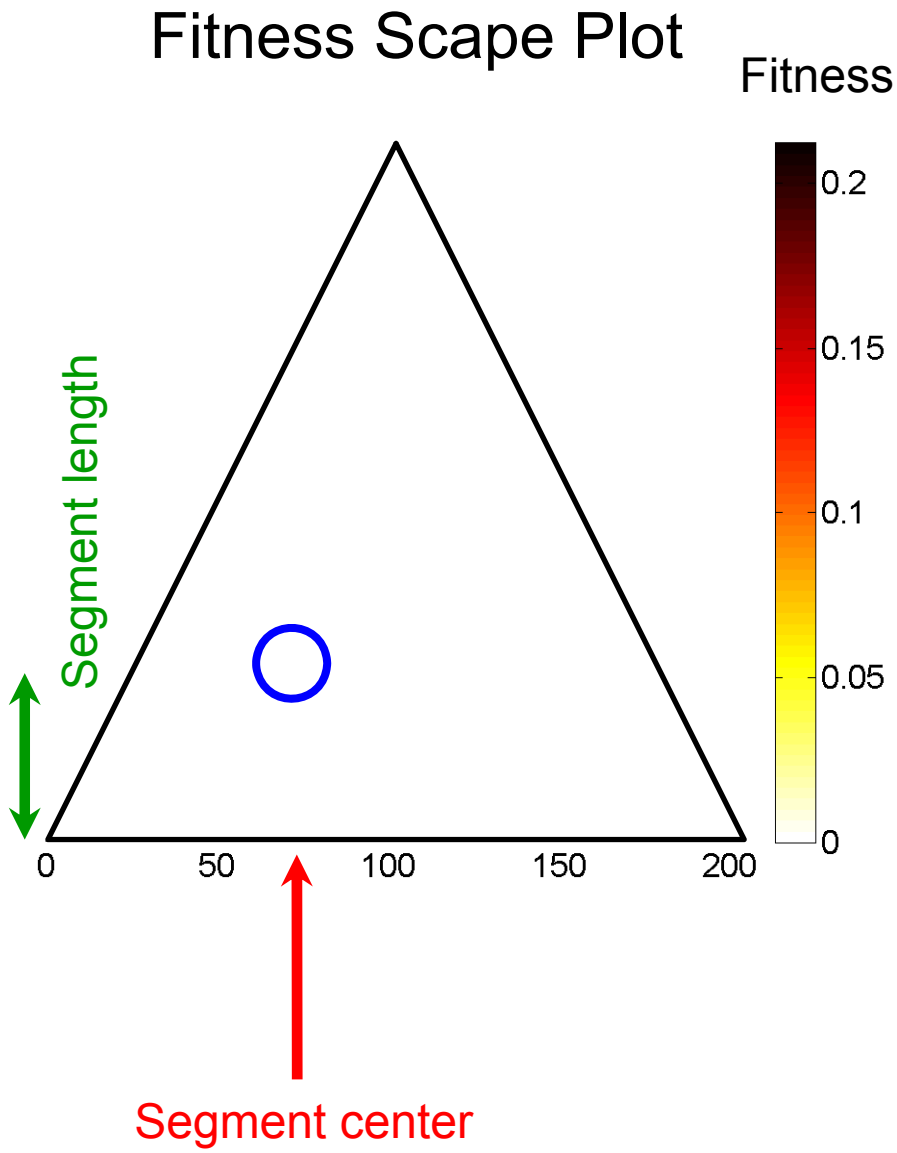
F := 2 • P • R / (P + R)

P := Normalize(Score(segment) - length(segment)) $\in [0,1]$

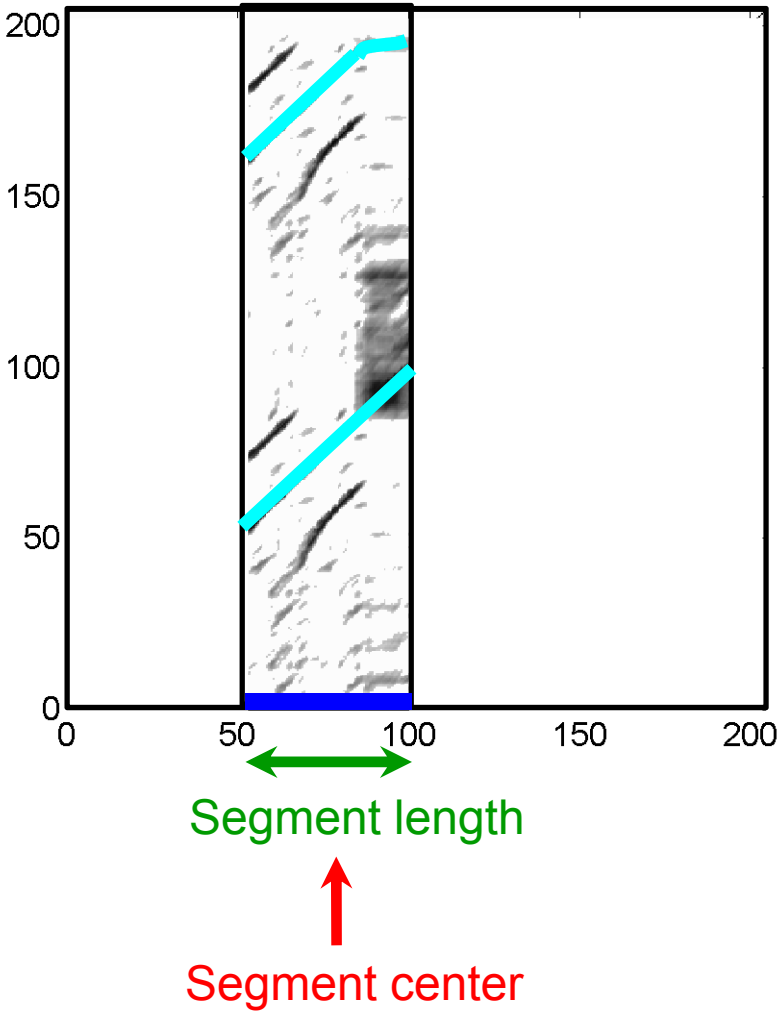
R := Normalize(Coverage(segment) - length(segment)) $\in [0,1]$

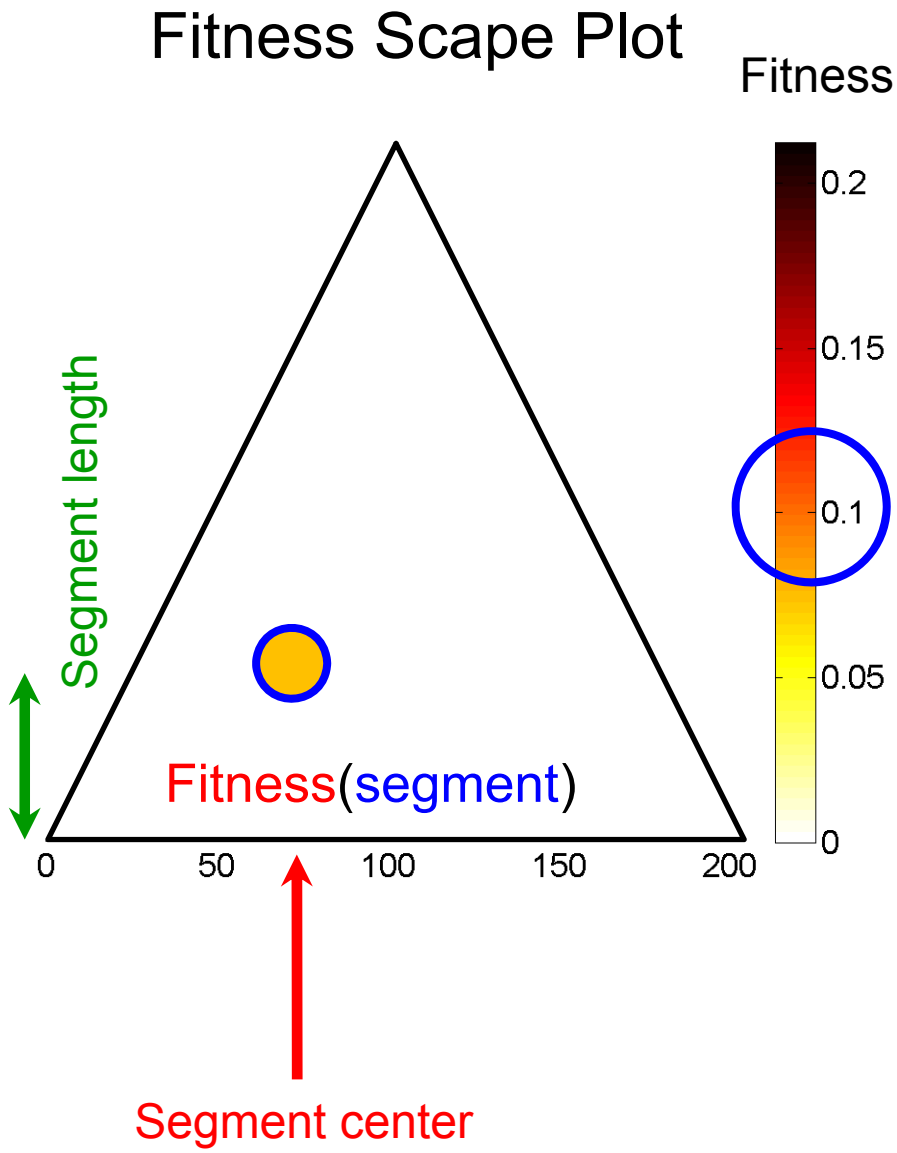
Thumbnail


200
150
100
50
0
0
50
100
150
200
Segment length
Segment center

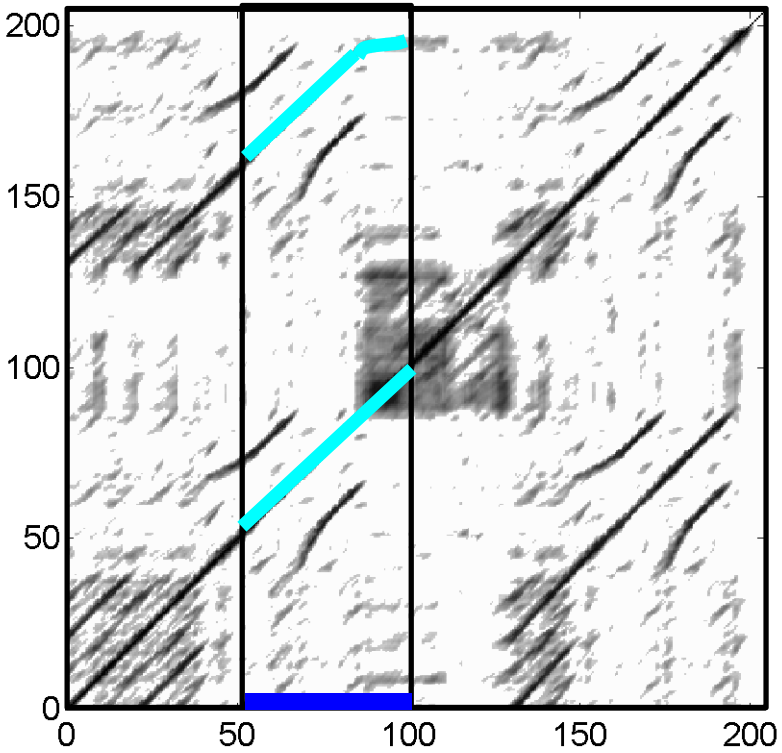

Fitness Scape Plot
Fitness
0.2
0.15
0.1
0.05
0
Segment length
0
50
100
150
200
Segment center

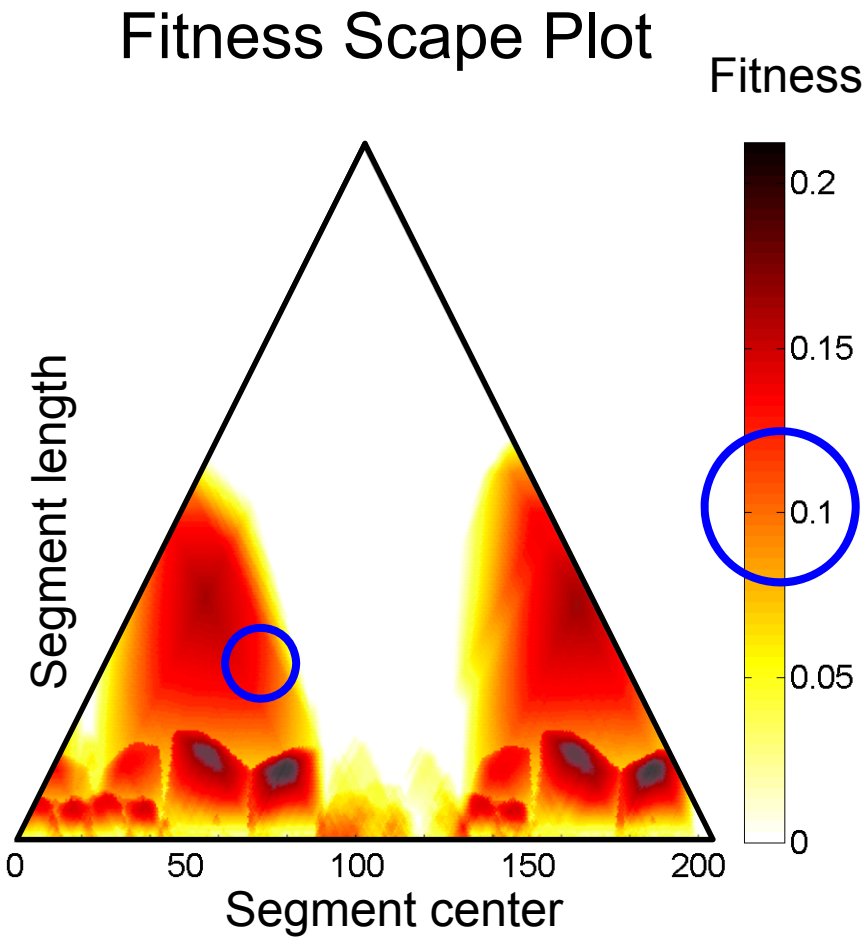
Thumbnail


200
150
100
50
0
0
50
100
150
200
Segment length
Segment center

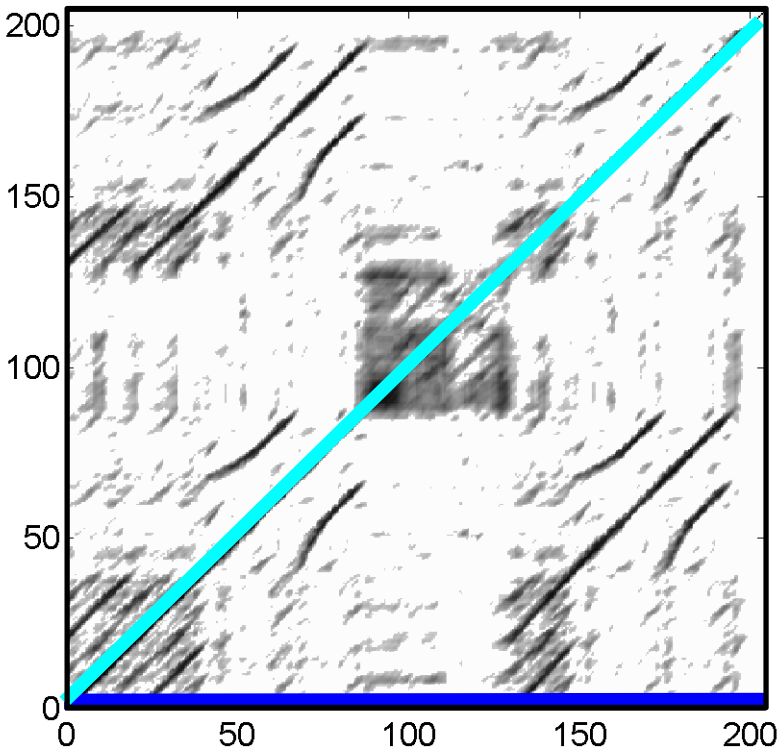

Fitness Scape Plot
Fitness
0.2
0.15
0.1
0.05
0
Segment length
Fitness(segment)
0
50
100
150
200
Segment center

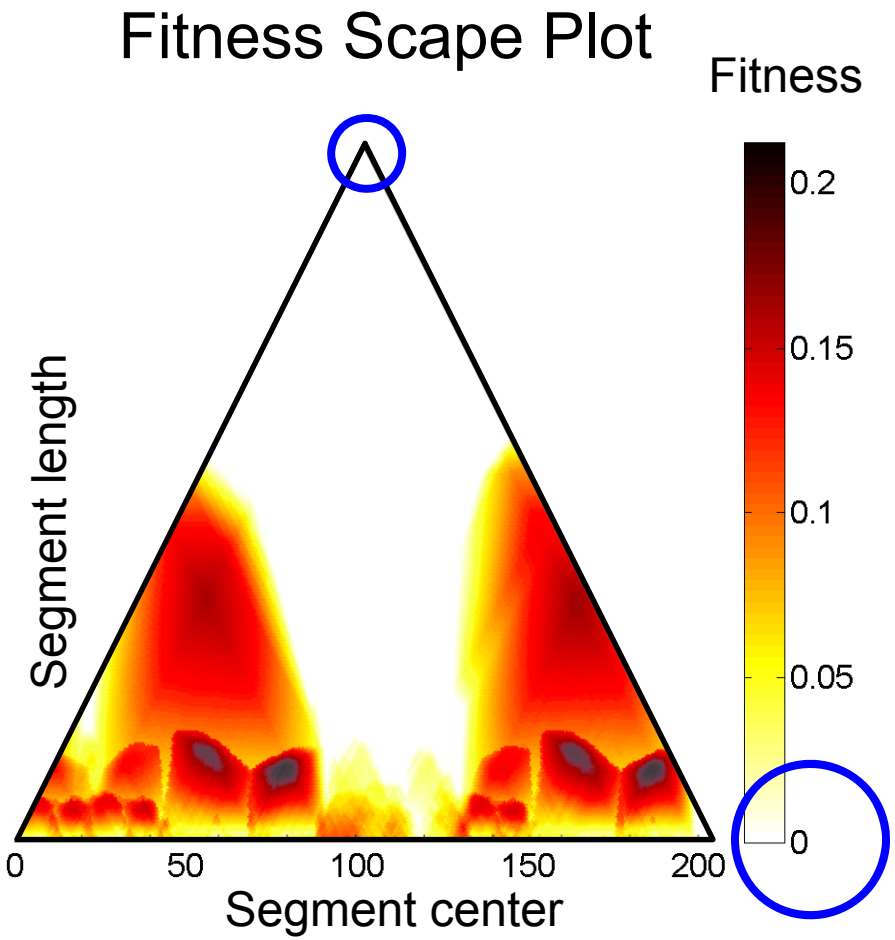
Thumbnail


200
150
100
50
0
0
50
100
150
200


Fitness Scape Plot
Fitness
0.2
0.15
0.1
0.05
0
Segment length
0
50
100
150
200
Segment center

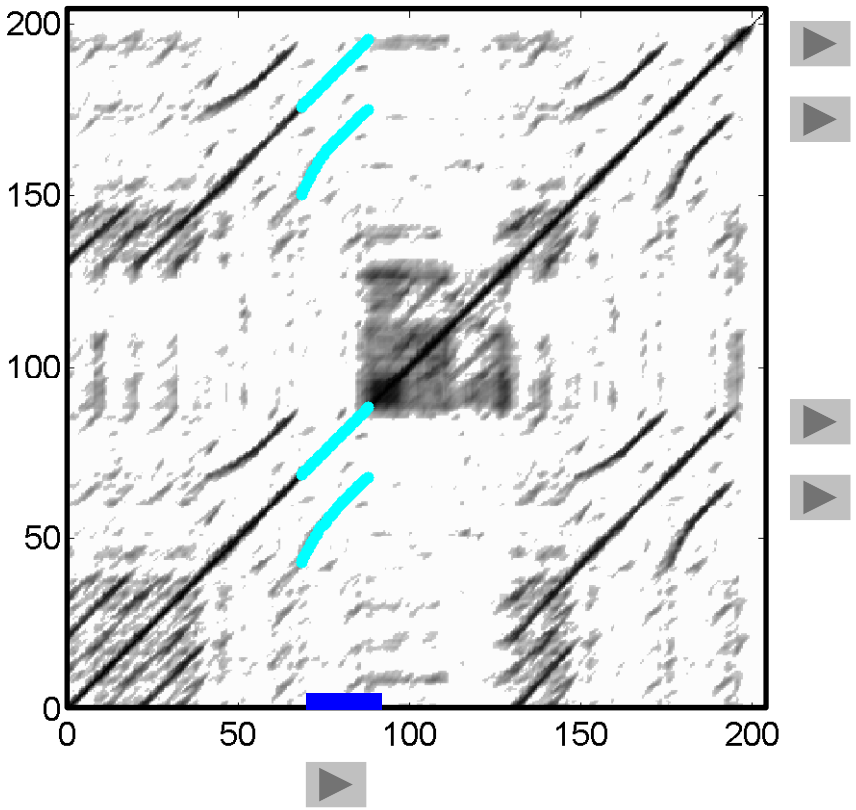
Thumbnail

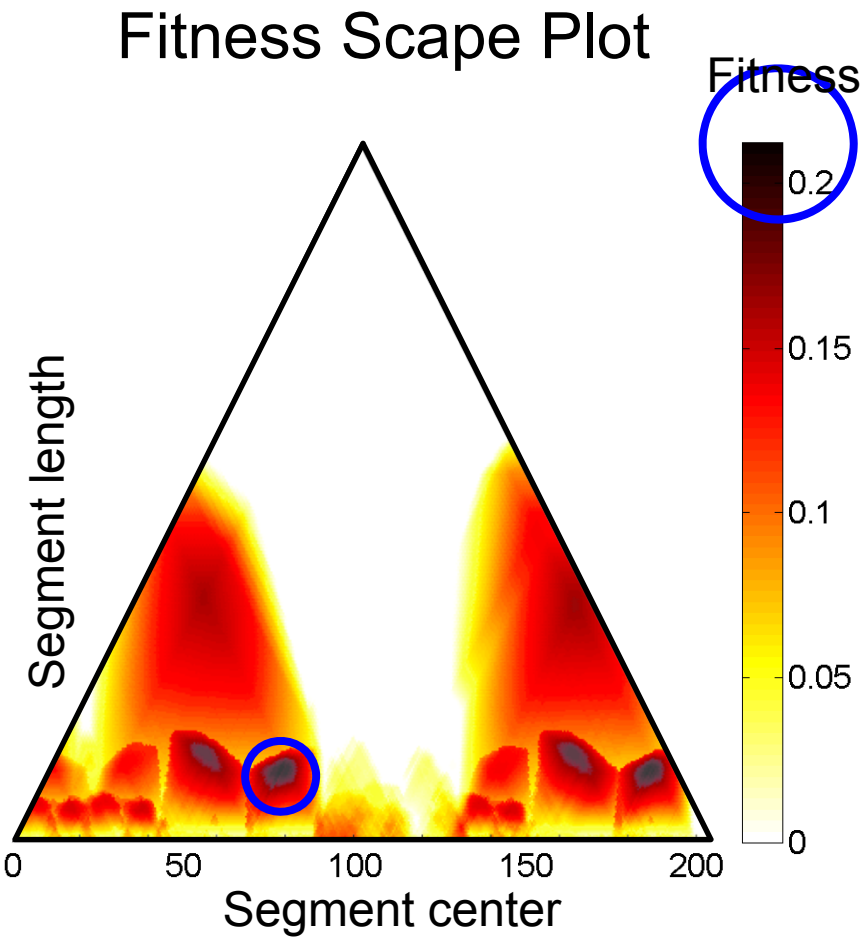




Note: Self-explanations are ignored → fitness is zero

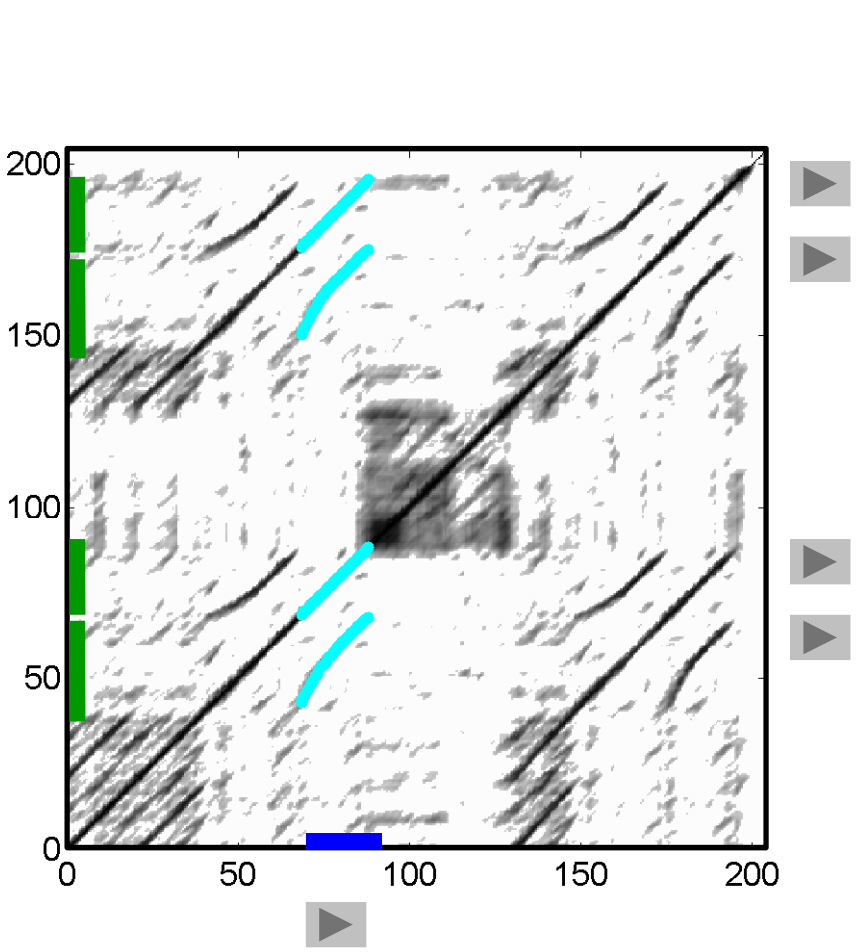
Thumbnail

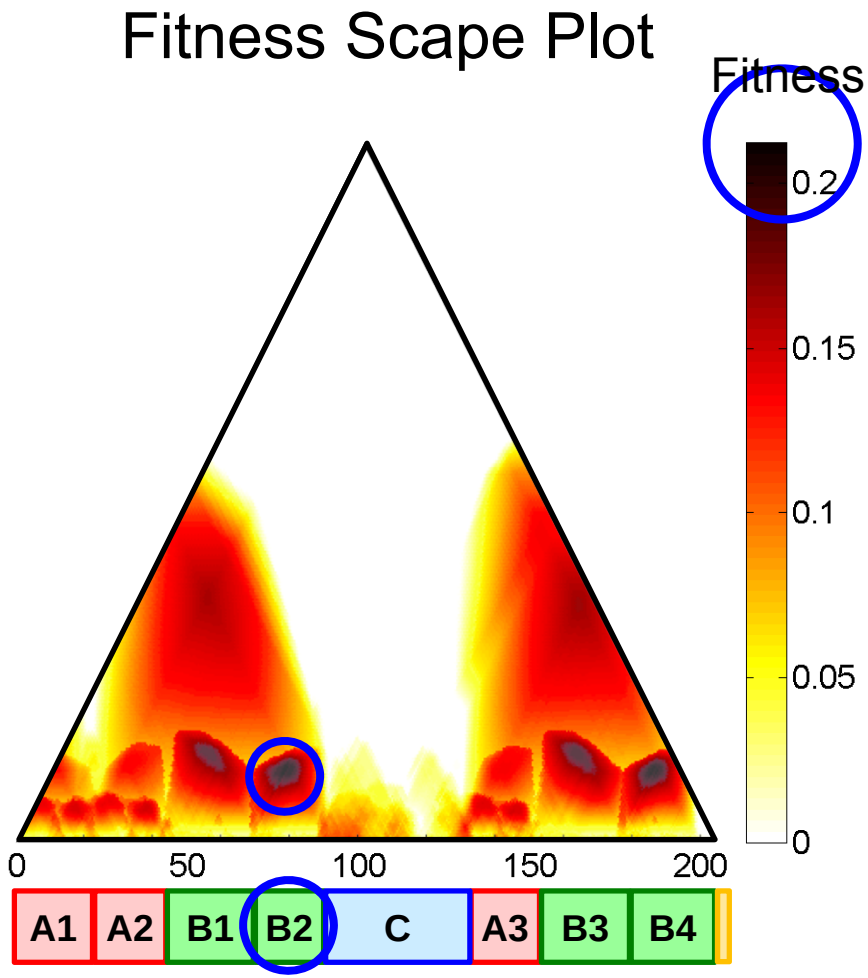




Thumbnail := segment having the highest fitness

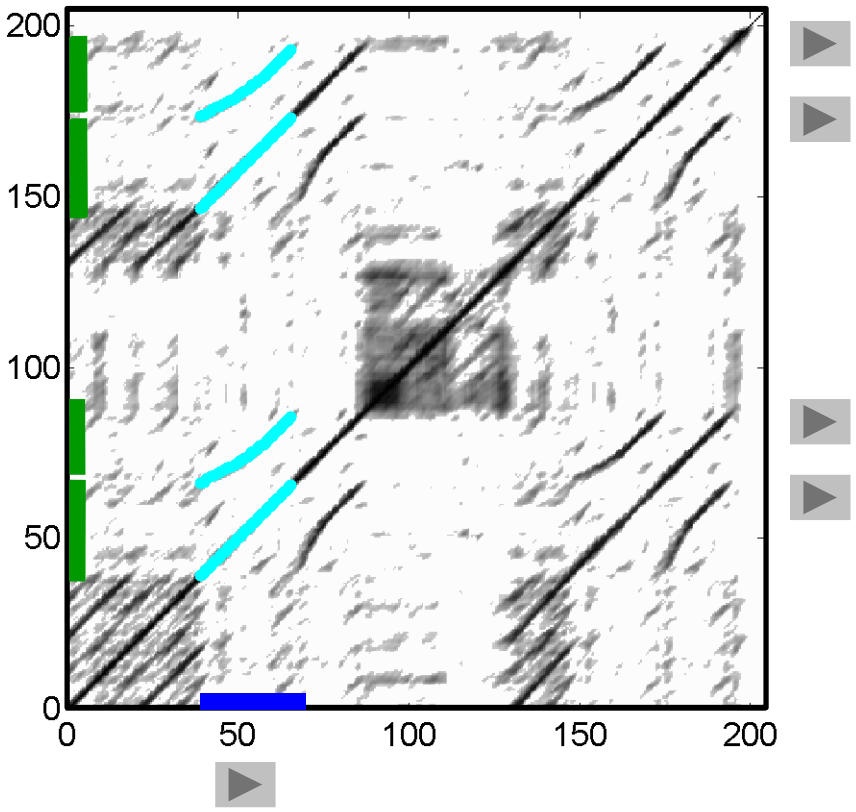
Thumbnail

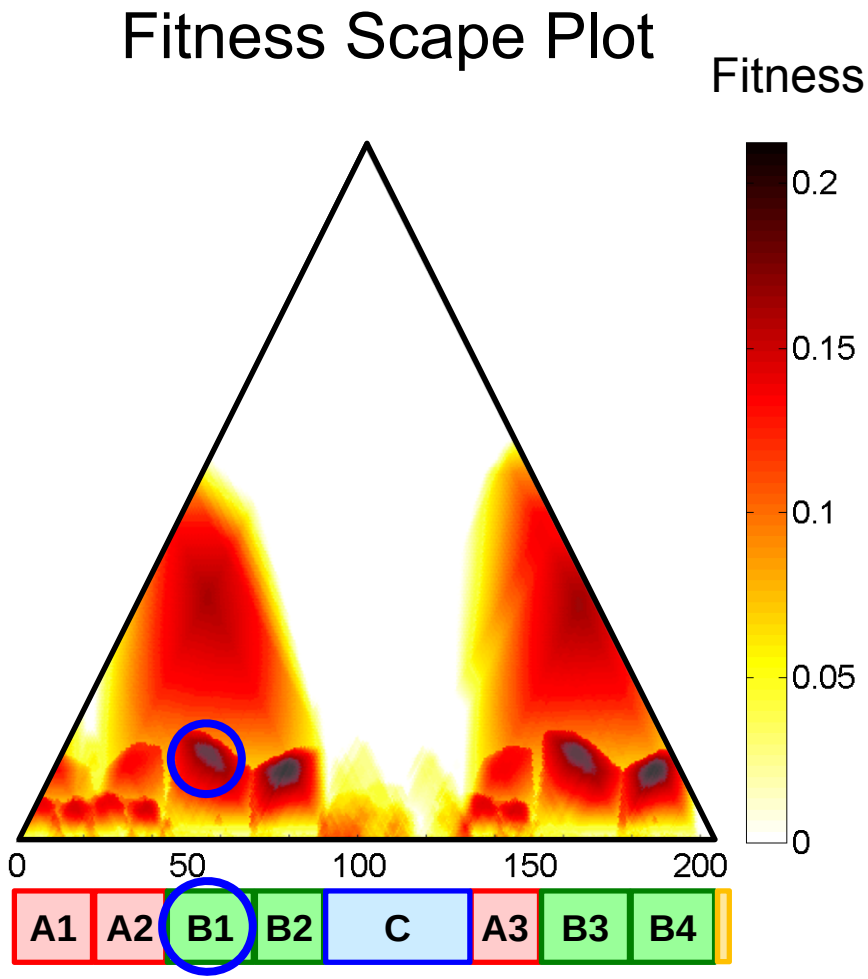




Example: Brahms Hungarian Dance No. 5 (Ormandy)

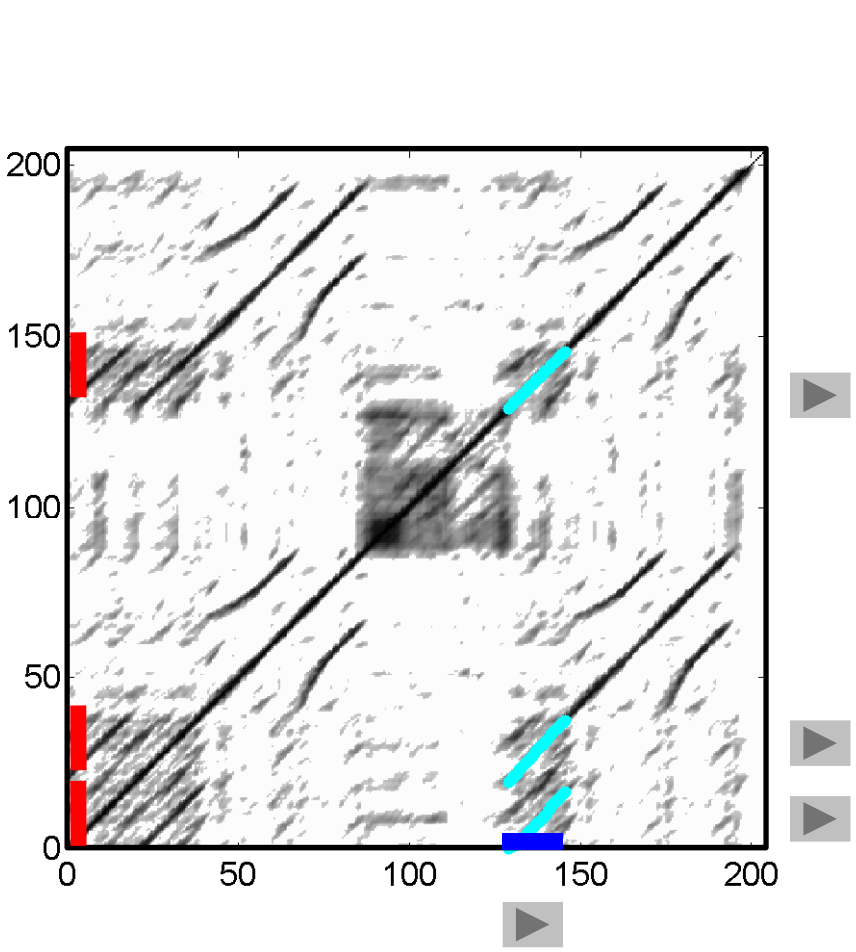
Thumbnail

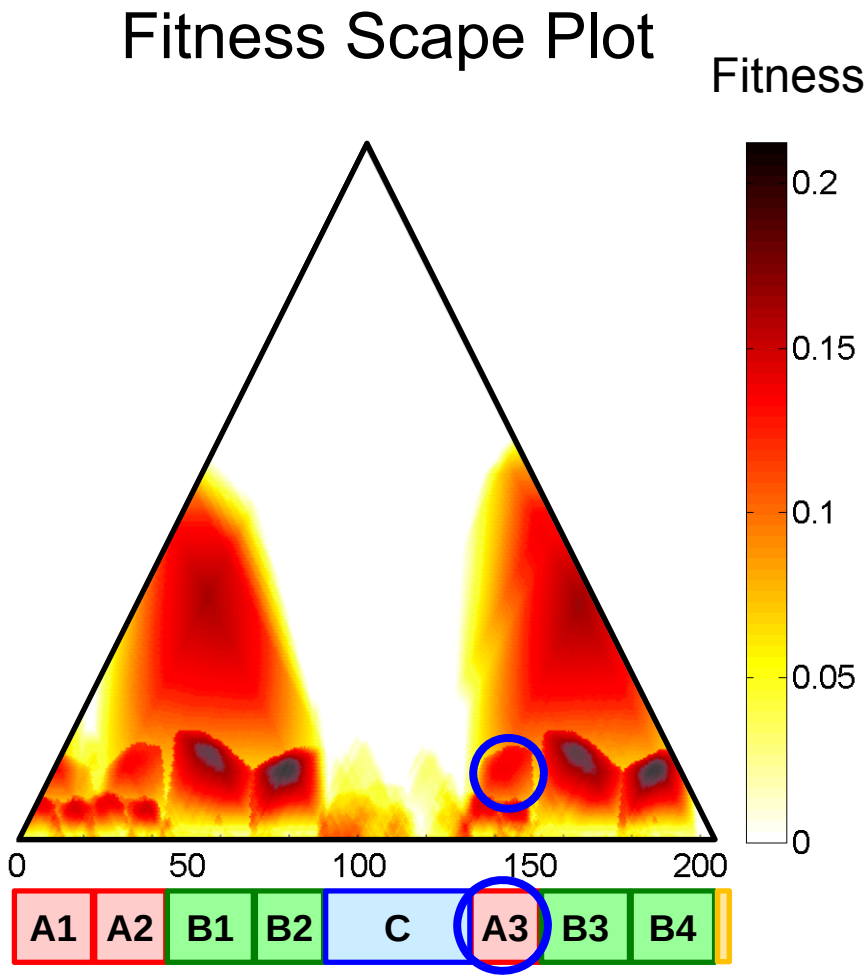




Example: Brahms Hungarian Dance No. 5 (Ormandy)

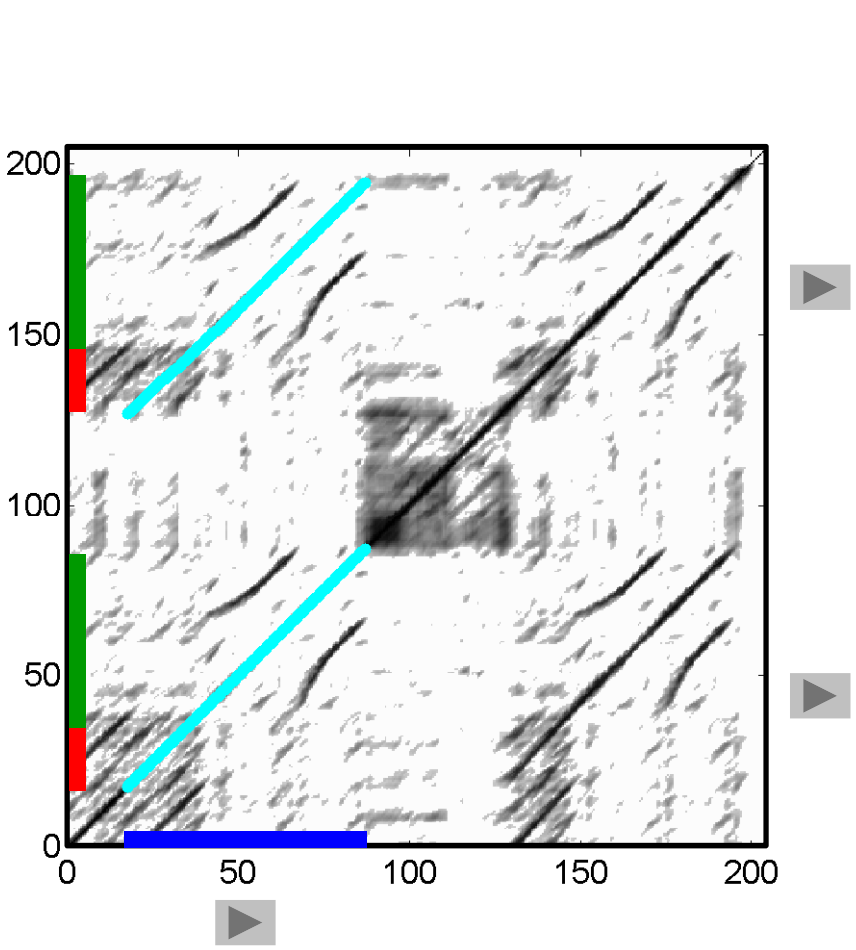
Thumbnail

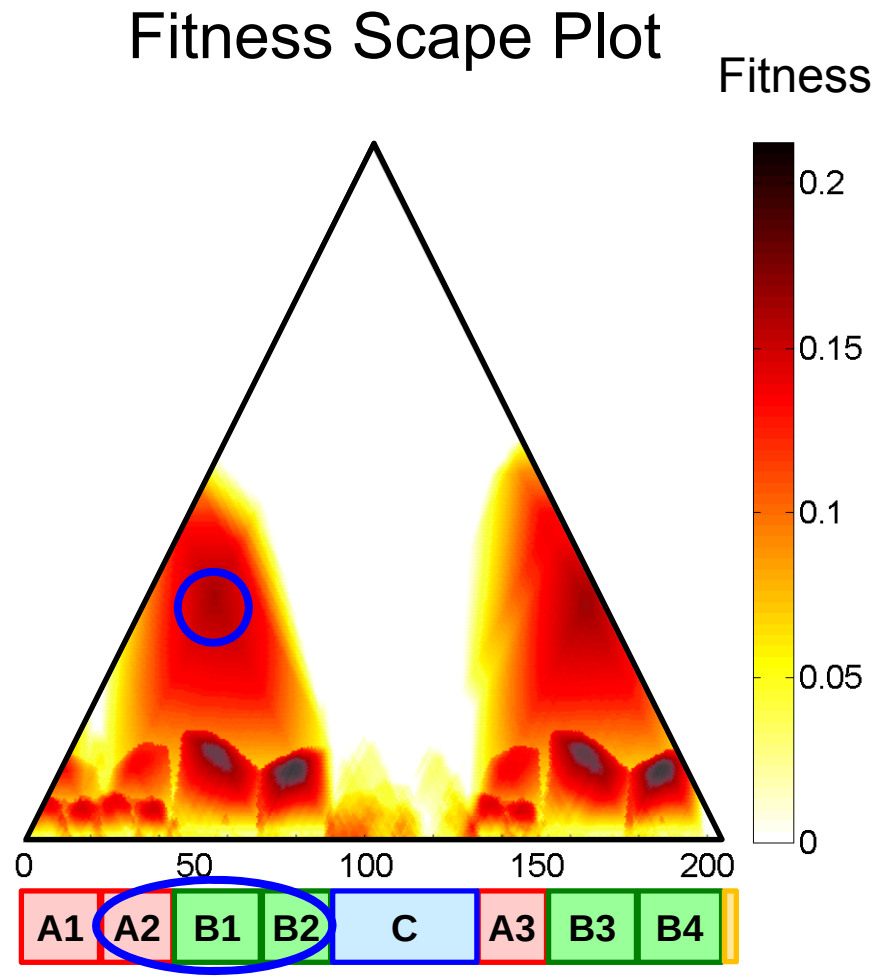




Example: Brahms Hungarian Dance No. 5 (Ormandy)

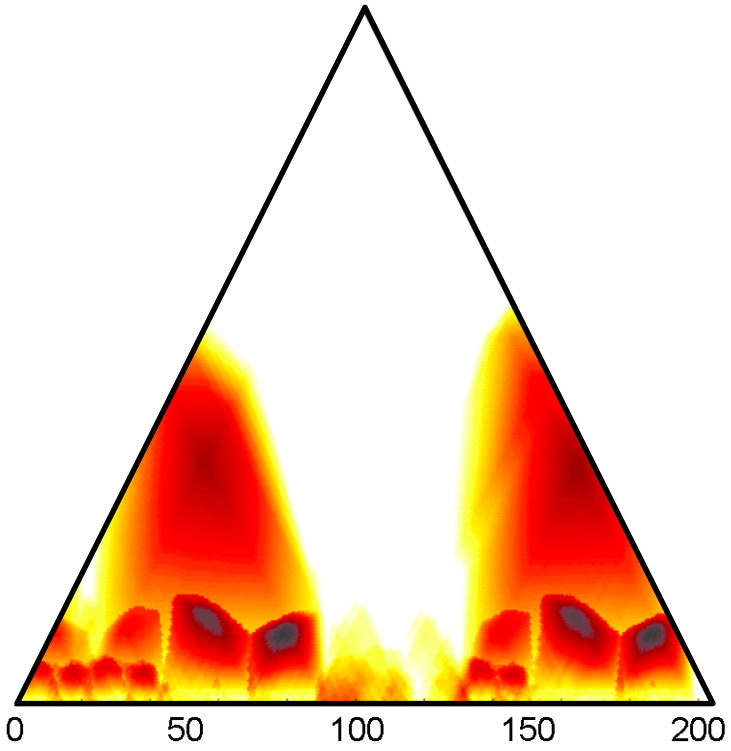
Thumbnail





Example: Brahms Hungarian Dance No. 5 (Ormandy)

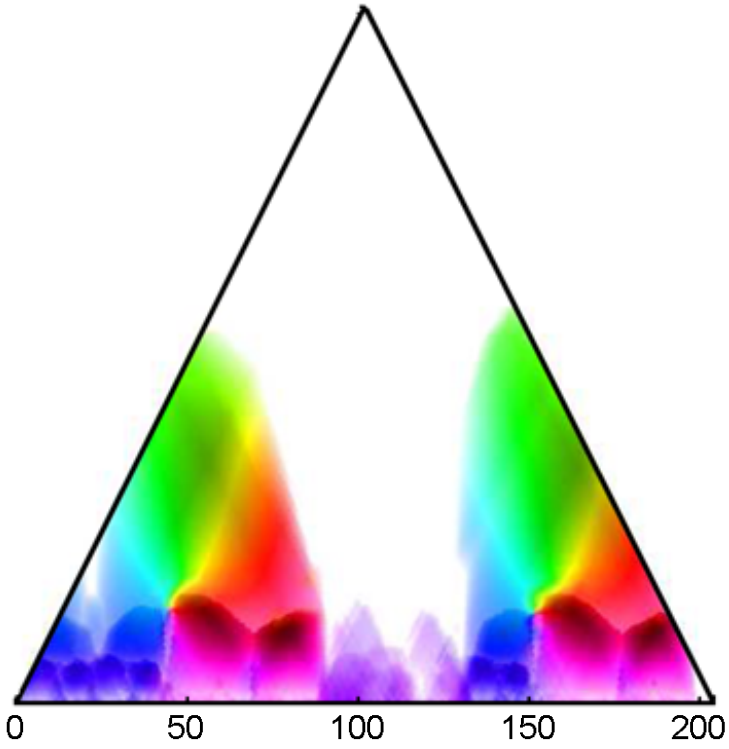
Scape Plot



Example: Brahms Hungarian Dance No. 5 (Ormandy)

Scape Plot

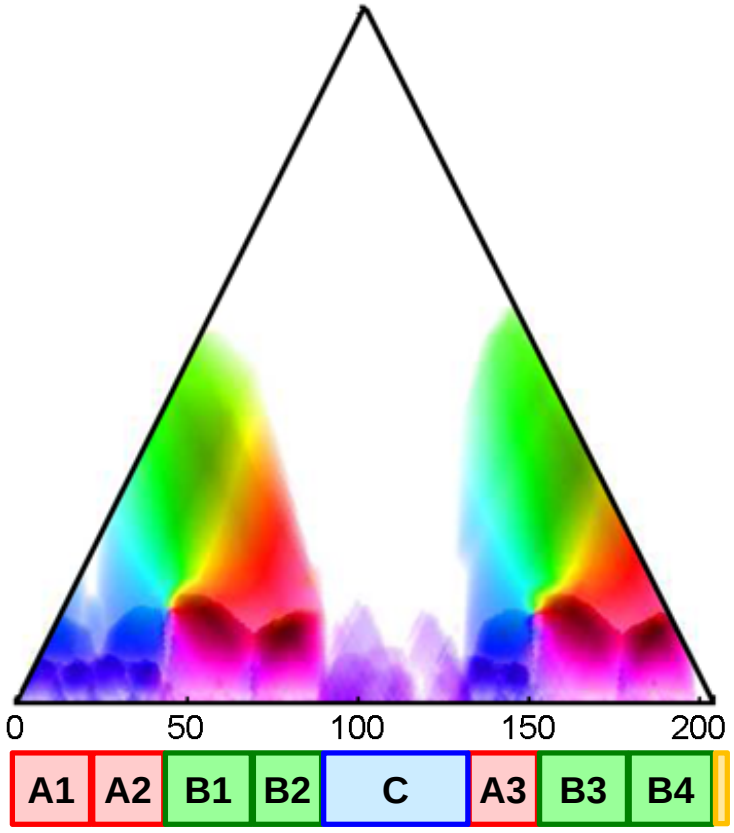
Coloring according to clustering result (grouping)



Example: Brahms Hungarian Dance No. 5 (Ormandy)

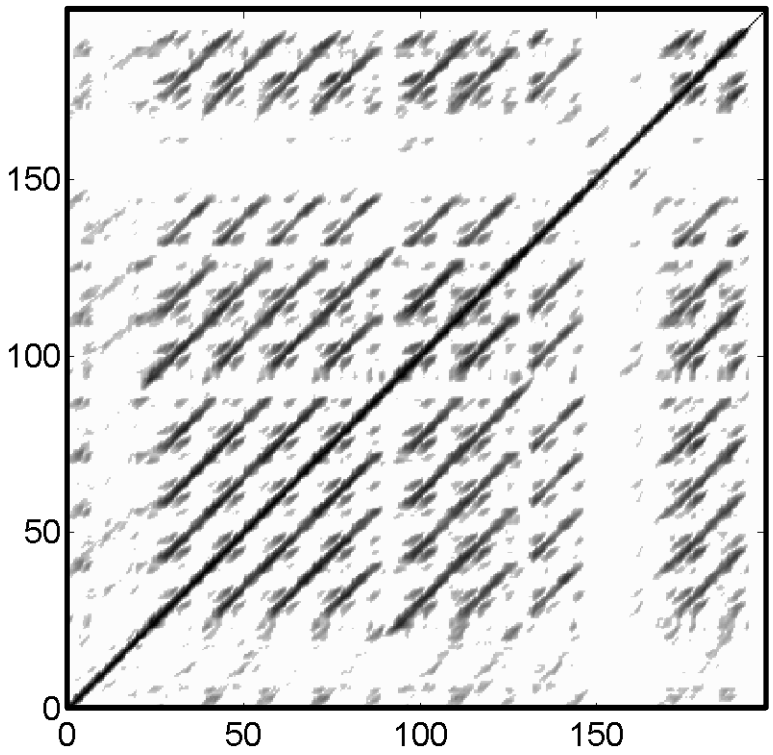
Scape Plot

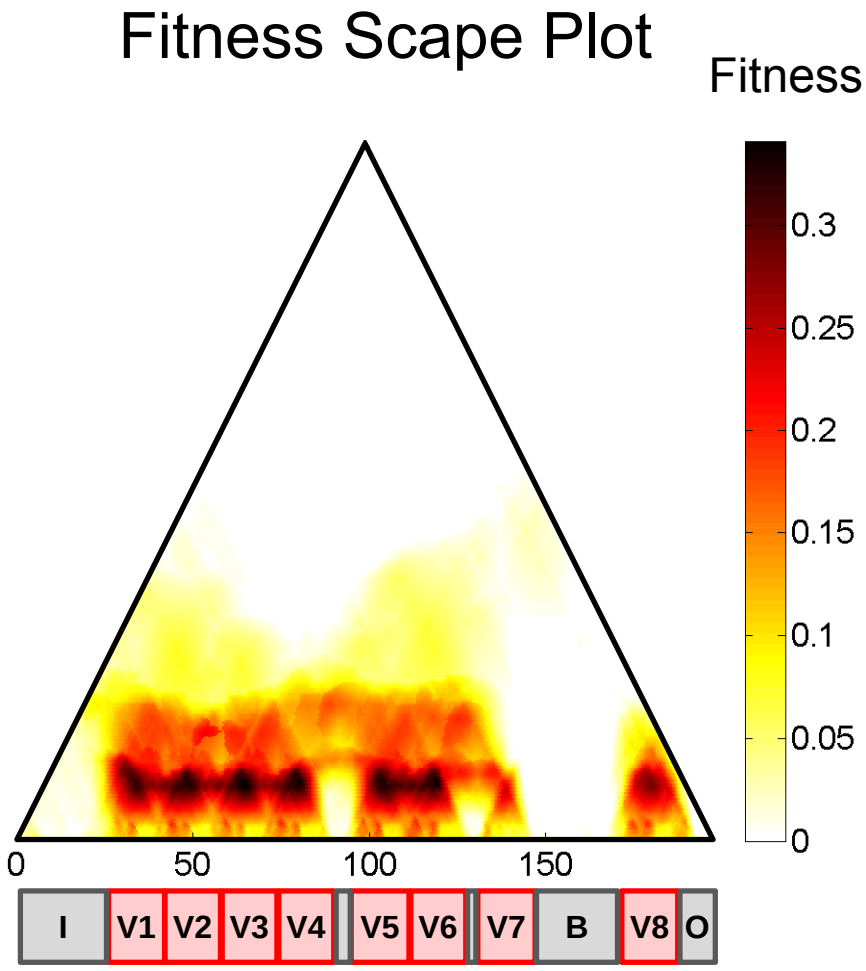
Coloring according to clustering result (grouping)



Example: Brahms Hungarian Dance No. 5 (Ormandy)

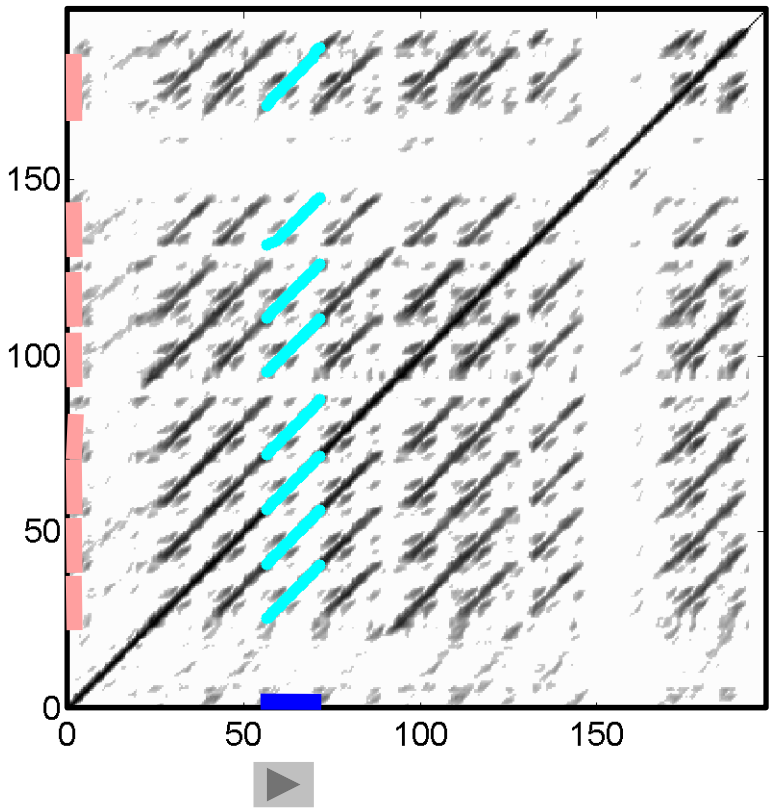
Thumbnail

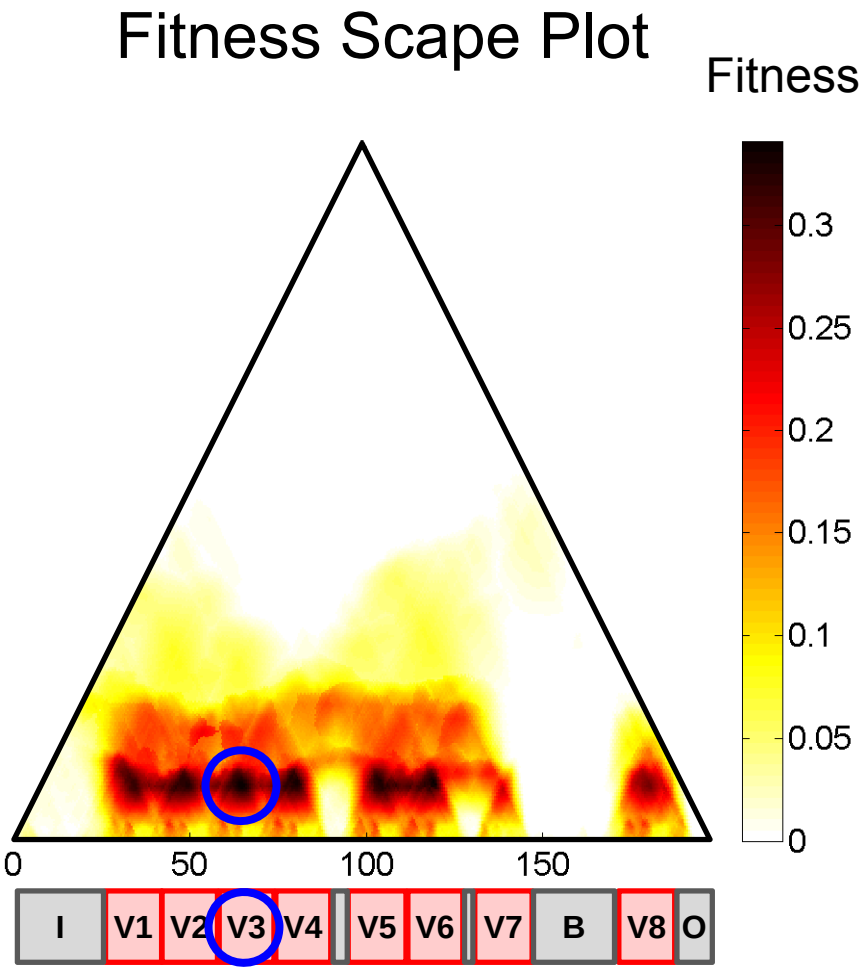




Example: Zager & Evans “In The Year 2525”

Thumbnail





Example: Zager & Evans “In The Year 2525”

Overview

- Introduction
- Feature Representations
- Self-Similarity Matrices
- Audio Thumbnailing
- Novelty-based Segmentation

Thanks:

- Foote
- Serra, Grosche, Arcos
- Goto
- Tzanetakis, Cook

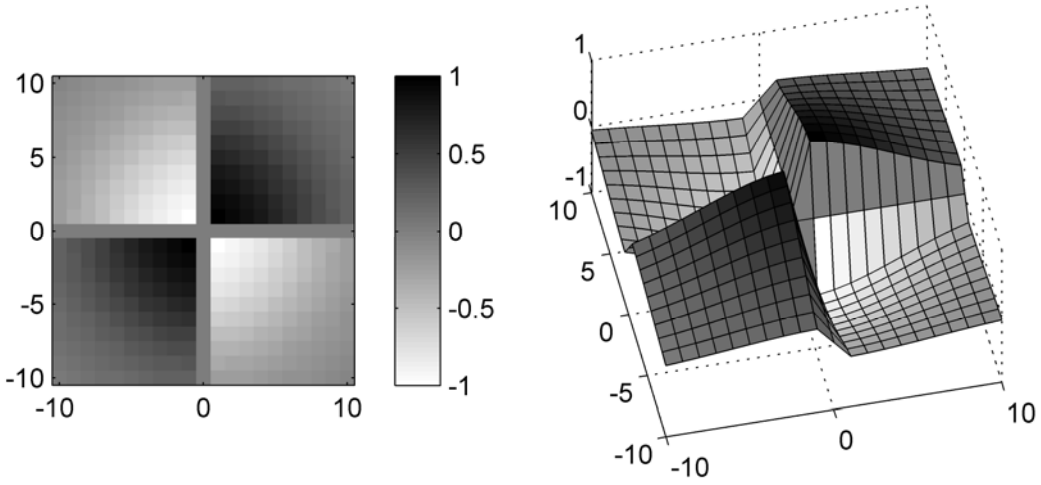
Novelty-based Segmentation

General goals:

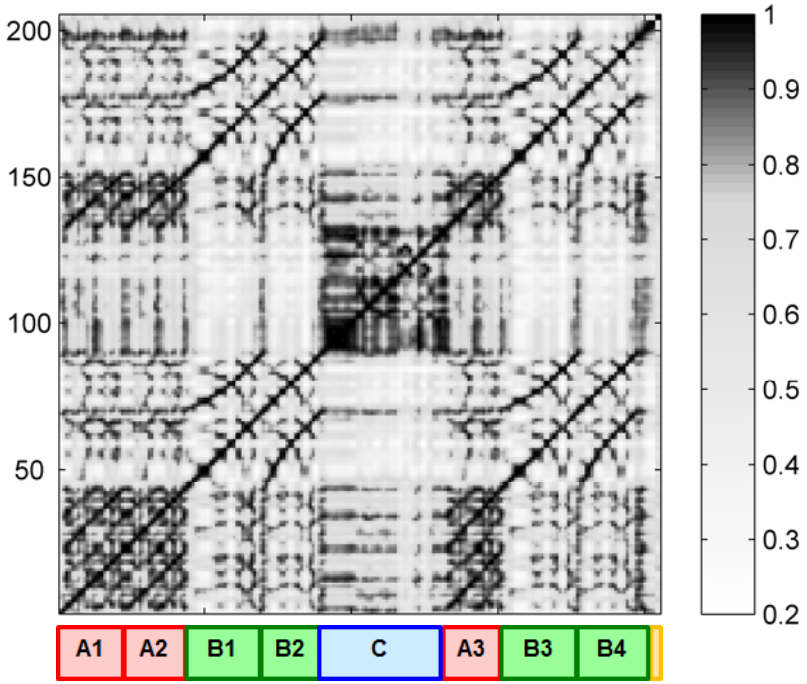
- Find instances where musical changes occur.
- Find transition between subsequent musical parts.

Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.



Novelty-based Segmentation



Idea (Foote):

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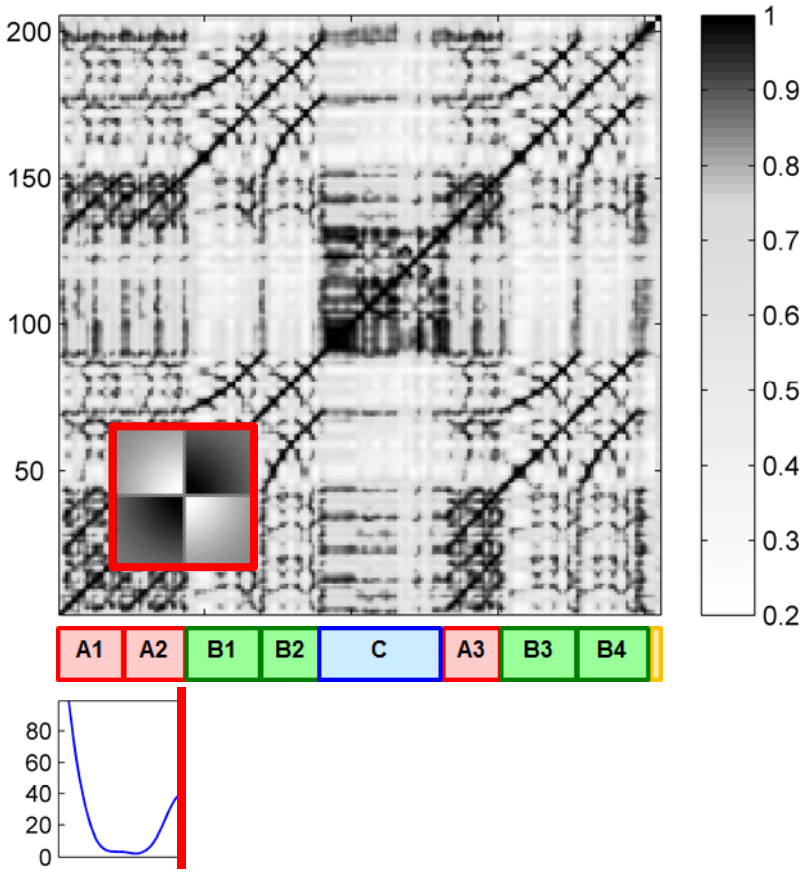
Novelty-based Segmentation



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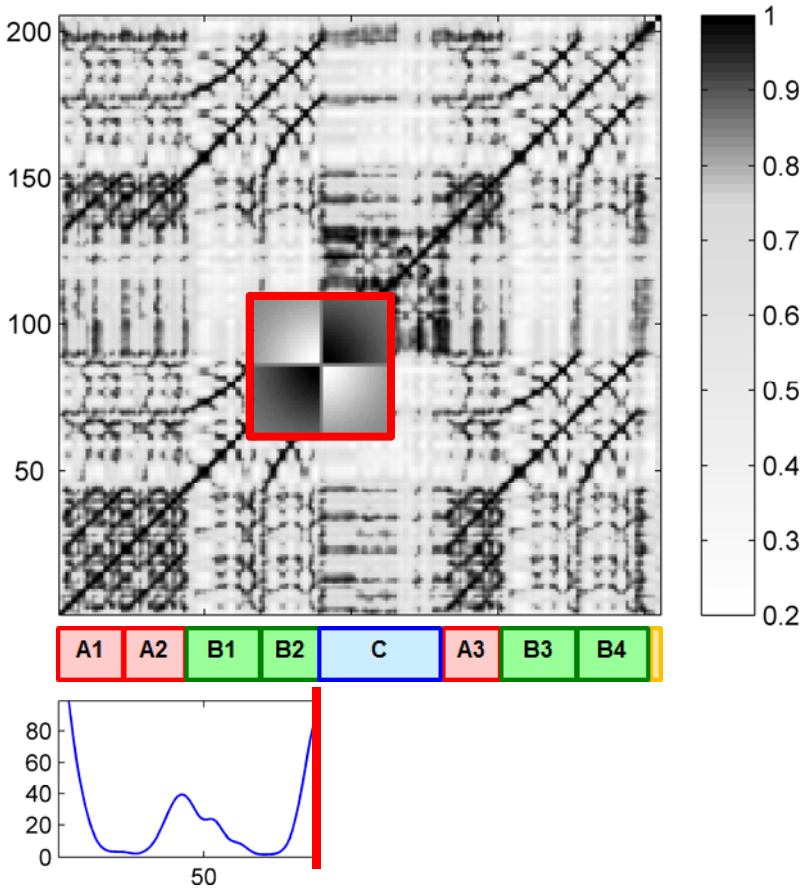
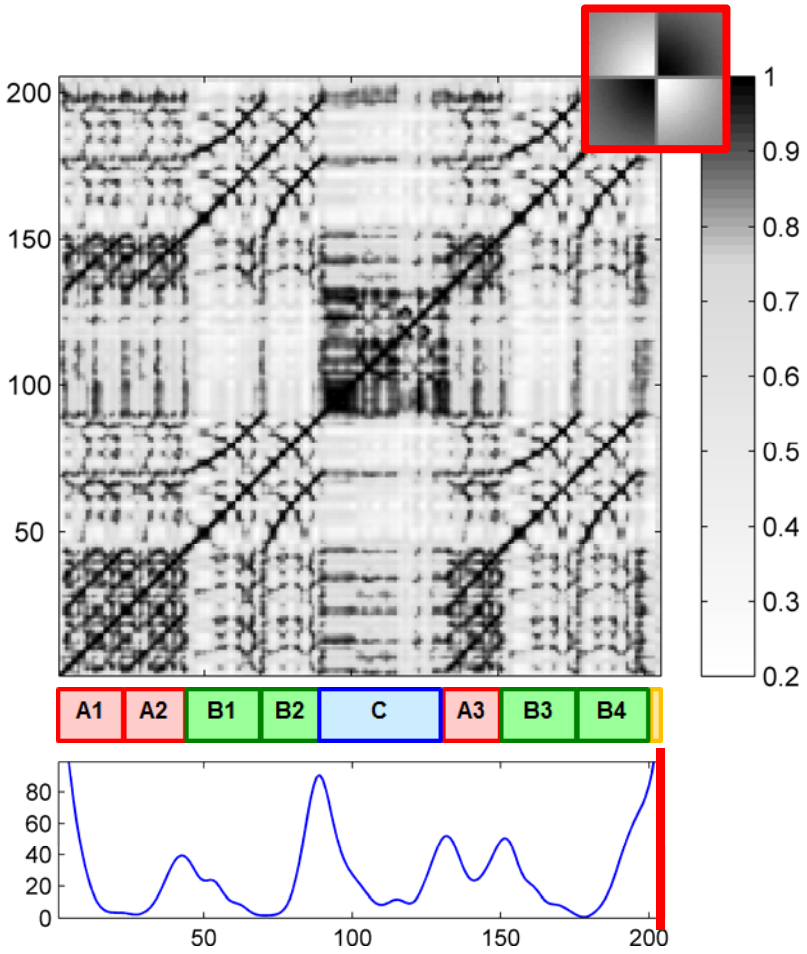
Novelty-based Segmentation



Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.

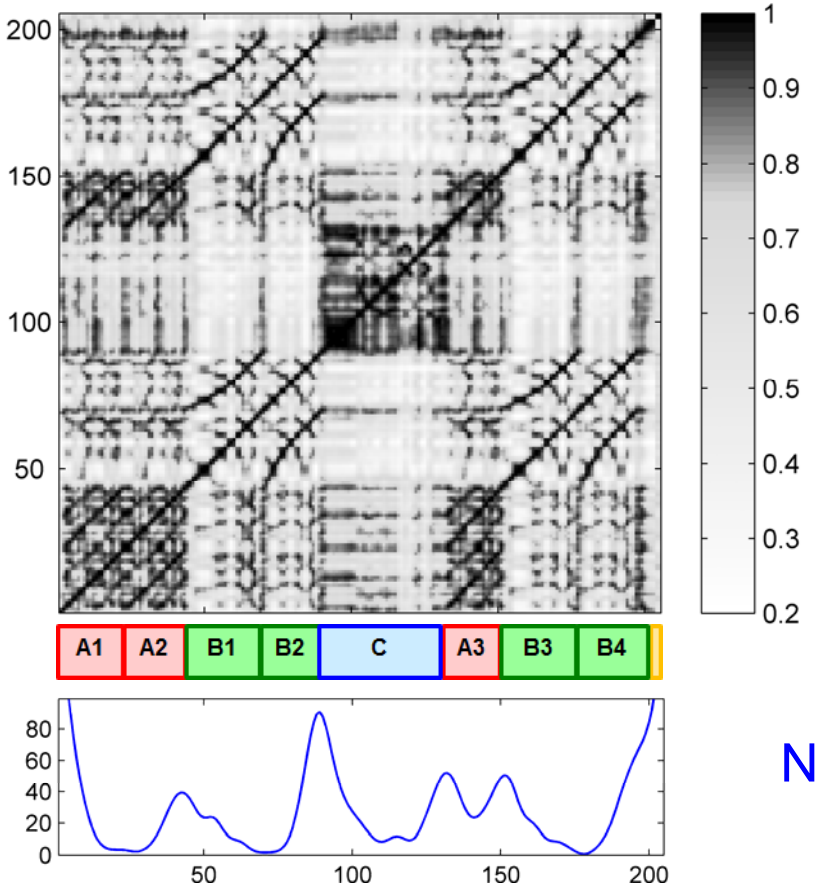
Novelty-based Segmentation



Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.

Novelty-based Segmentation

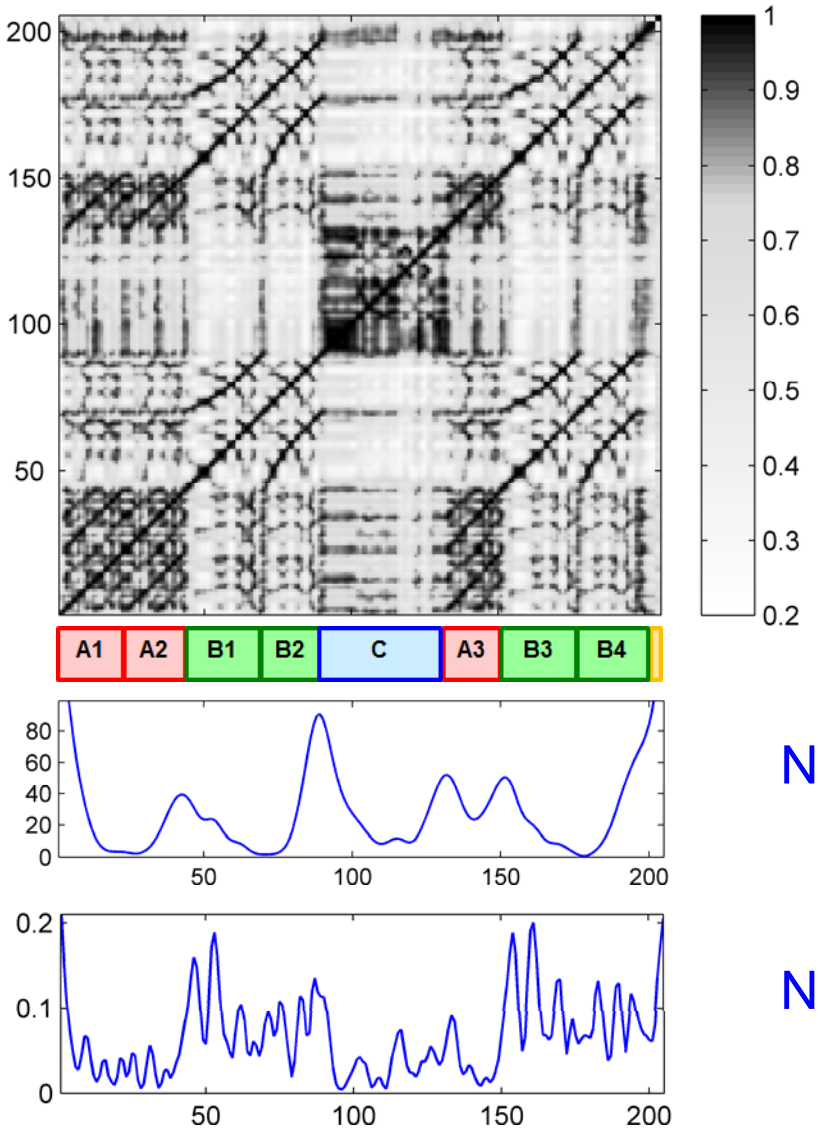


Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.

Novelty function using

Novelty-based Segmentation



Idea (Foote):

Use checkerboard-like kernel function to detect corner points on main diagonal of SSM.

Novelty function using 

Novelty function using 

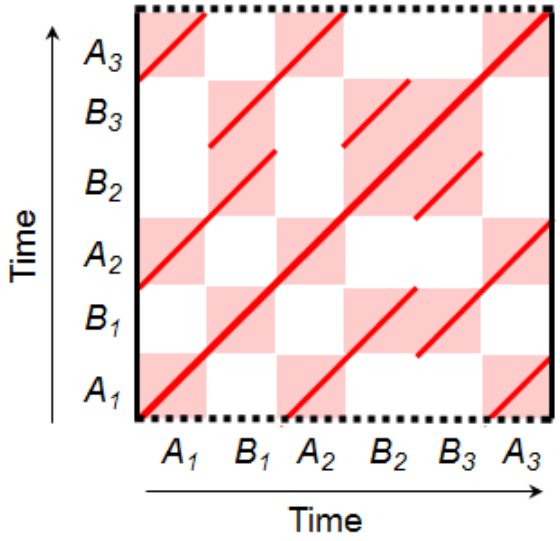
Novelty-based Segmentation

Idea:

- Find instances where structural changes occur.
- Combine global and local aspects within a unifying framework

Structure features

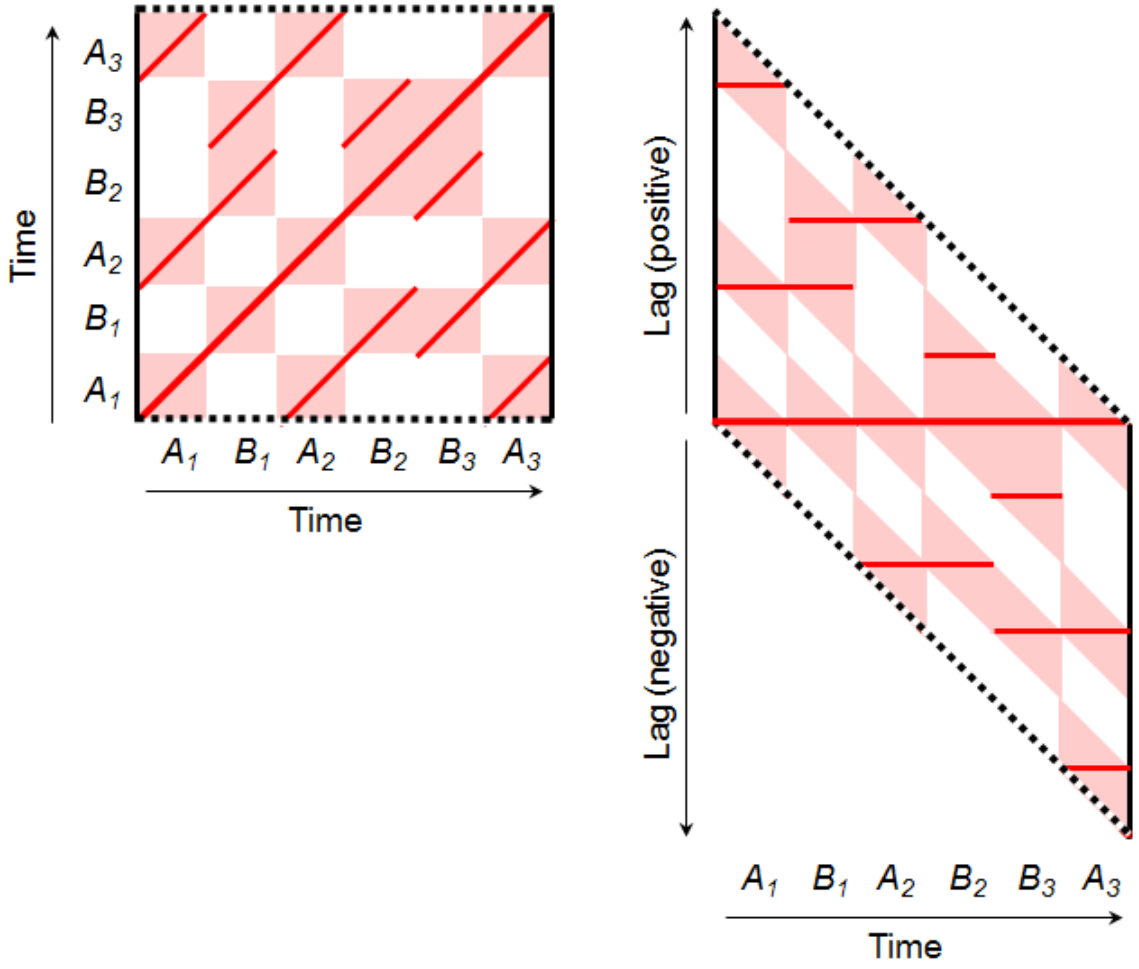
Novelty-based Segmentation



Structure features

- Enhanced SSM

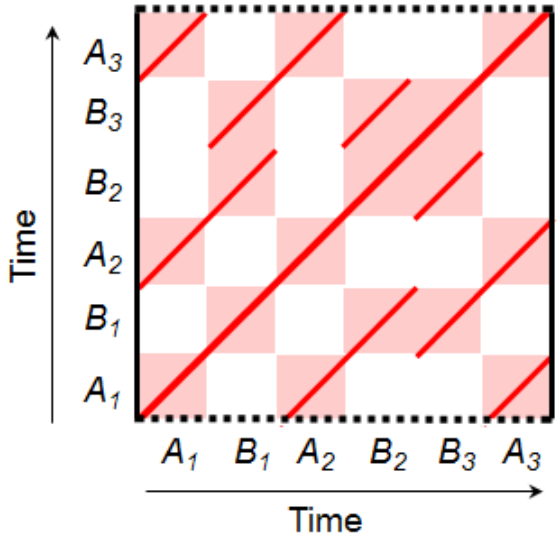
Novelty-based Segmentation

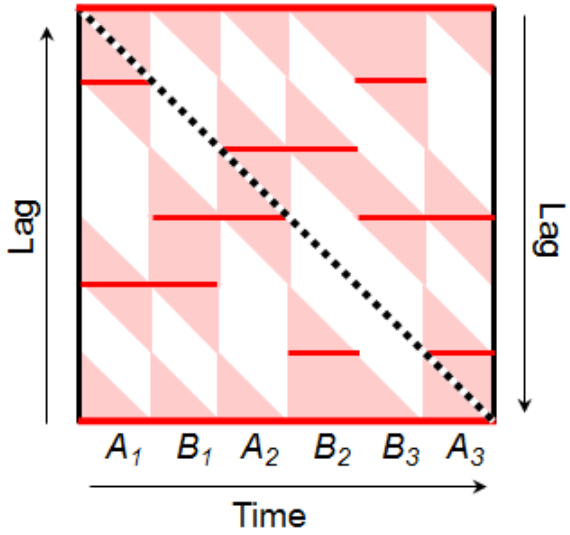


Structure features

- Enhanced SSM
- Time-lag SSM

Novelty-based Segmentation

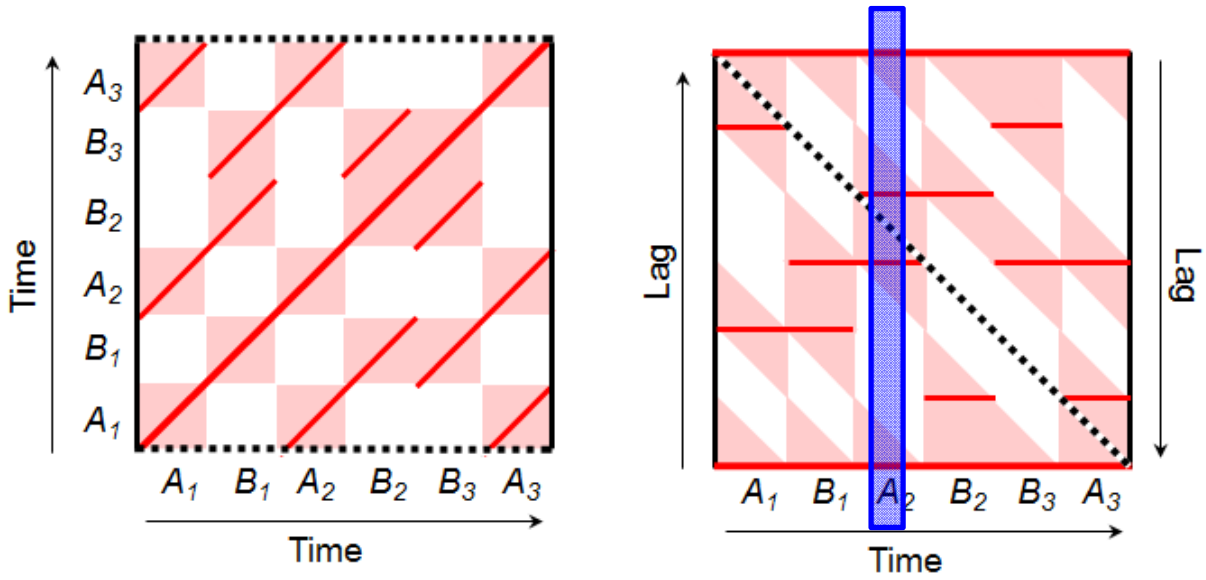




Structure features

- Enhanced SSM
- Time-lag SSM
- Cyclic time-lag SSM

Novelty-based Segmentation

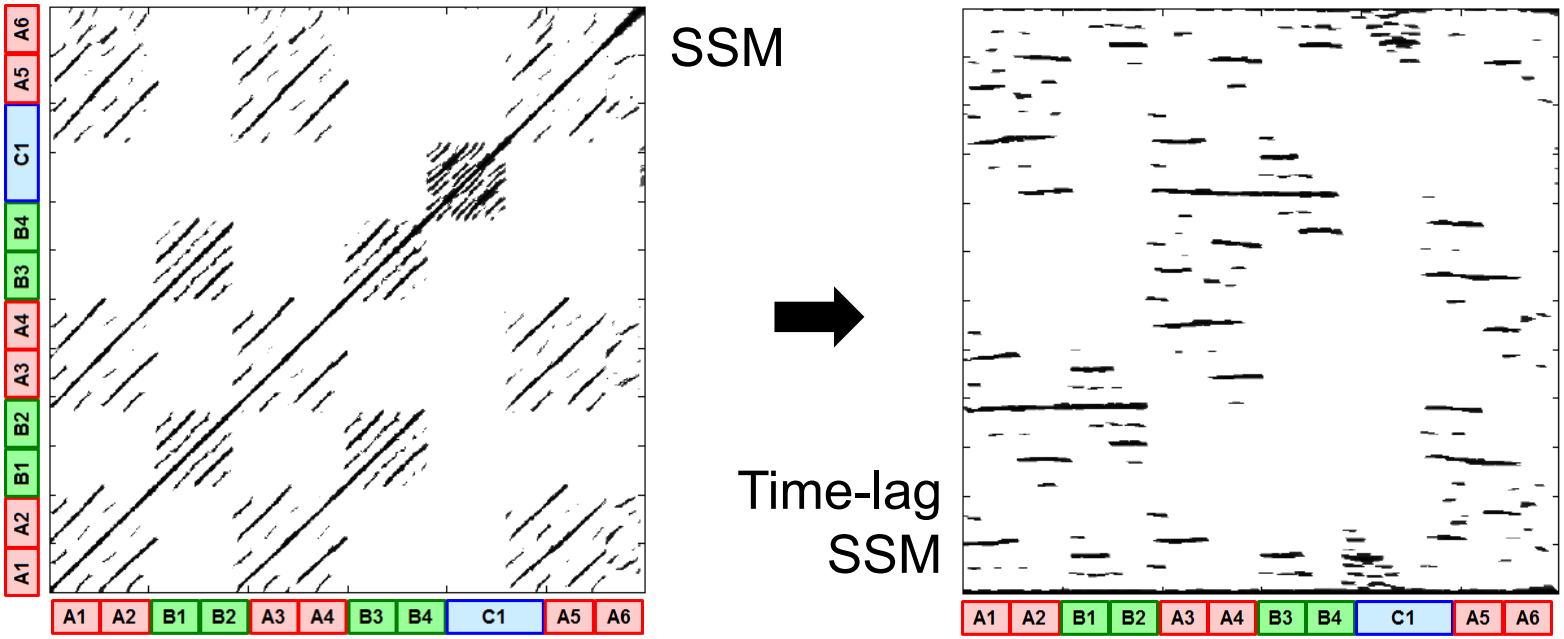


Structure features

- Enhanced SSM
- Time-lag SSM
- Cyclic time-lag SSM
- Columns as features

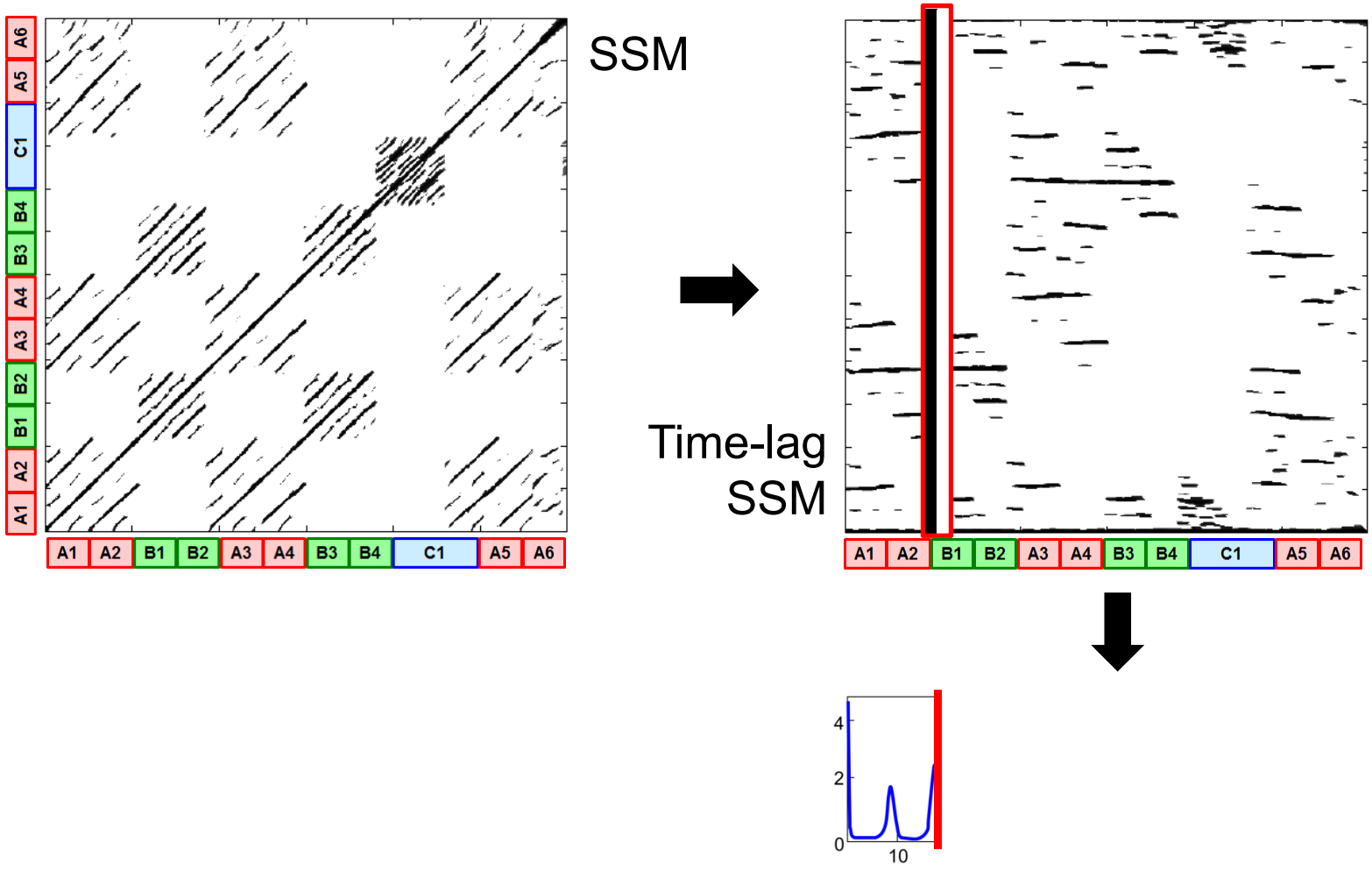
Novelty-based Segmentation

Example: Chopin Mazurka Op. 24, No. 1



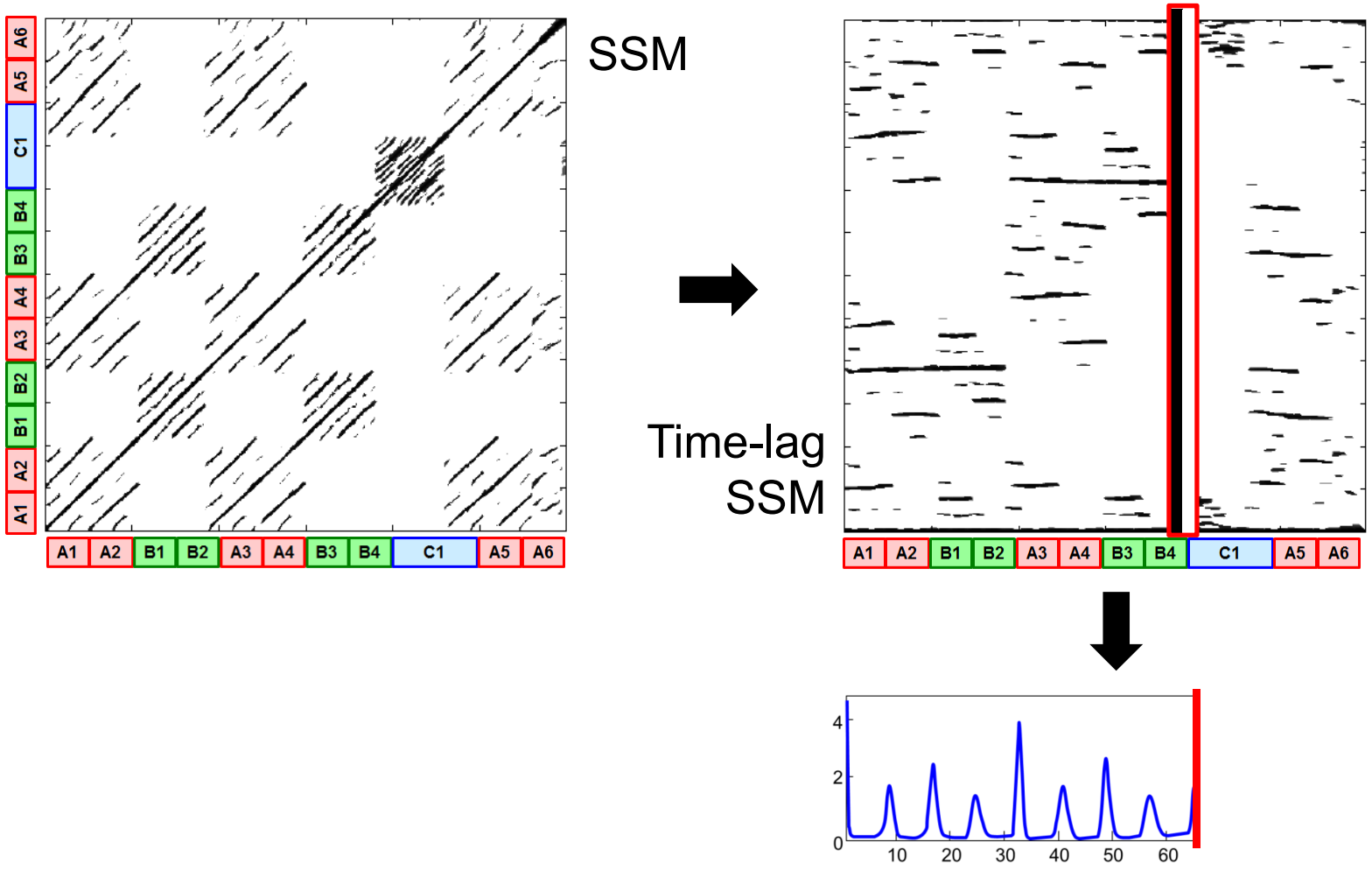
Novelty-based Segmentation

Example: Chopin Mazurka Op. 24, No. 1



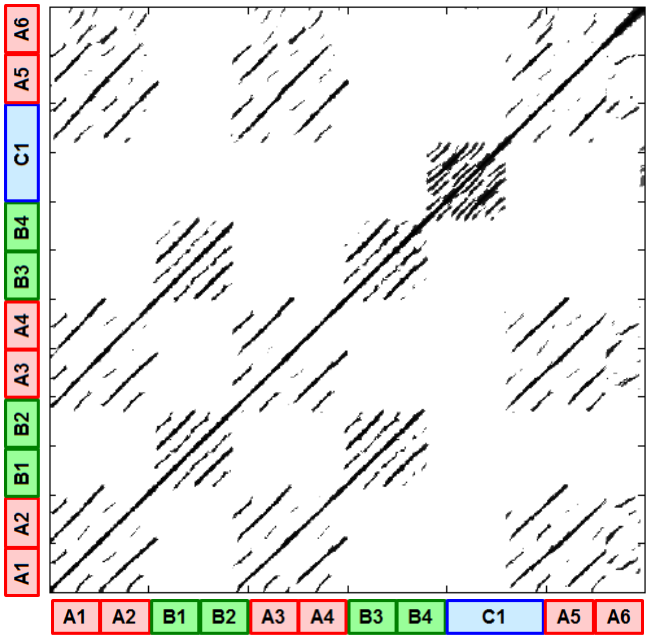
Novelty-based Segmentation

Example: Chopin Mazurka Op. 24, No. 1



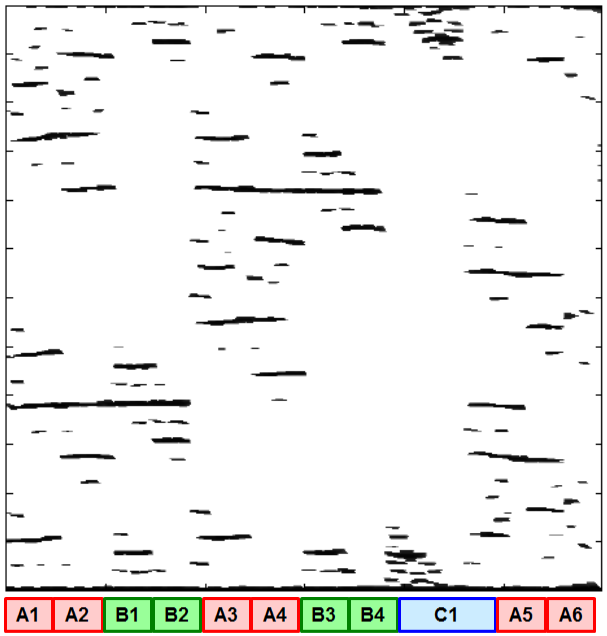
Novelty-based Segmentation

Example: Chopin Mazurka Op. 24, No. 1

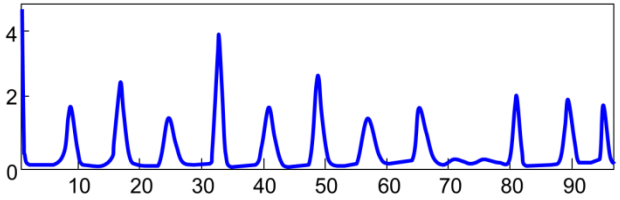


SSM

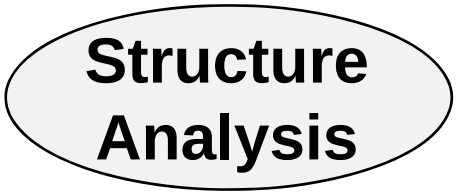
Time-lag SSM



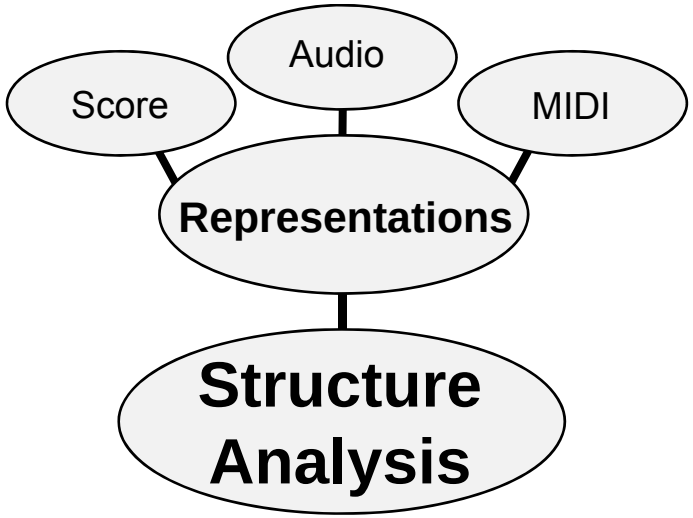
Structure-based novelty function



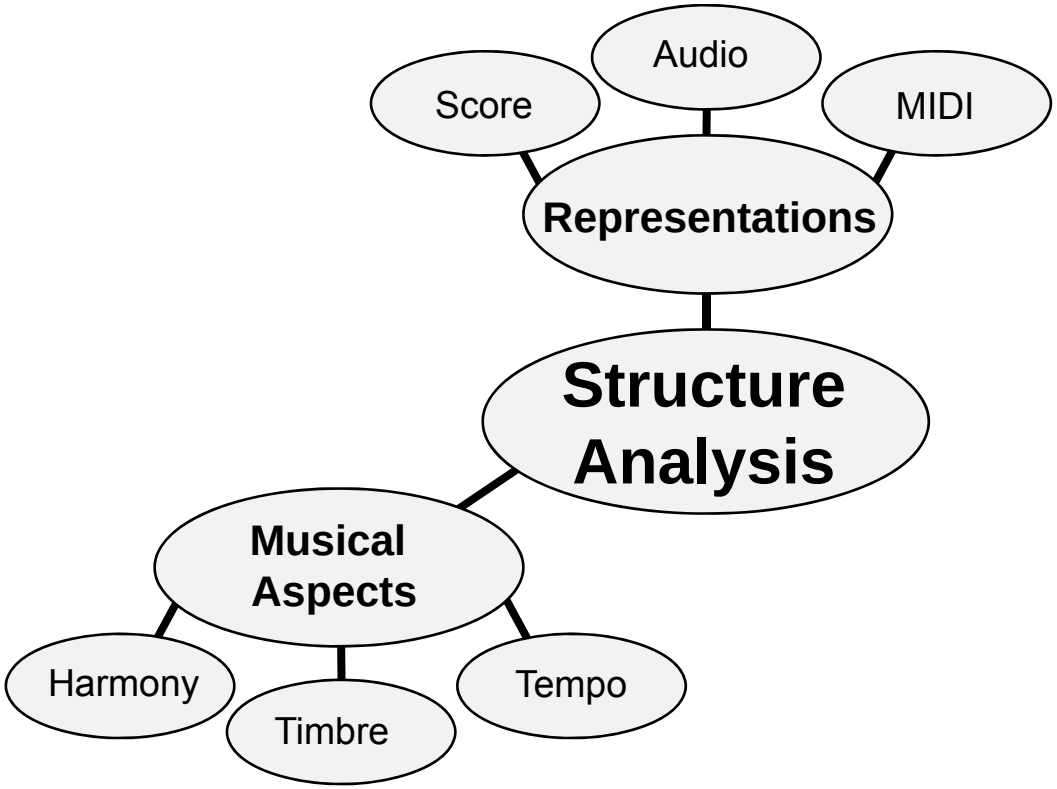
Conclusions



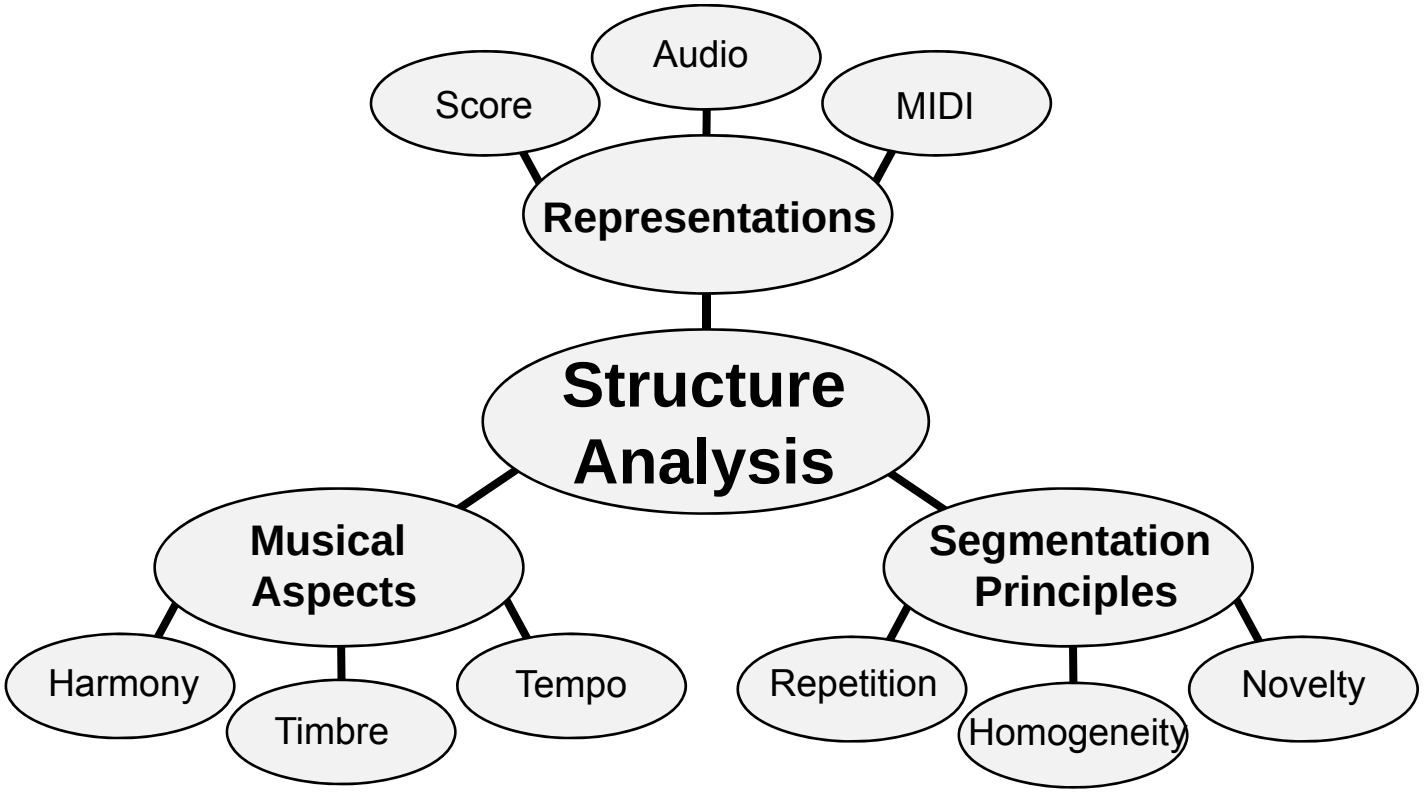
Conclusions



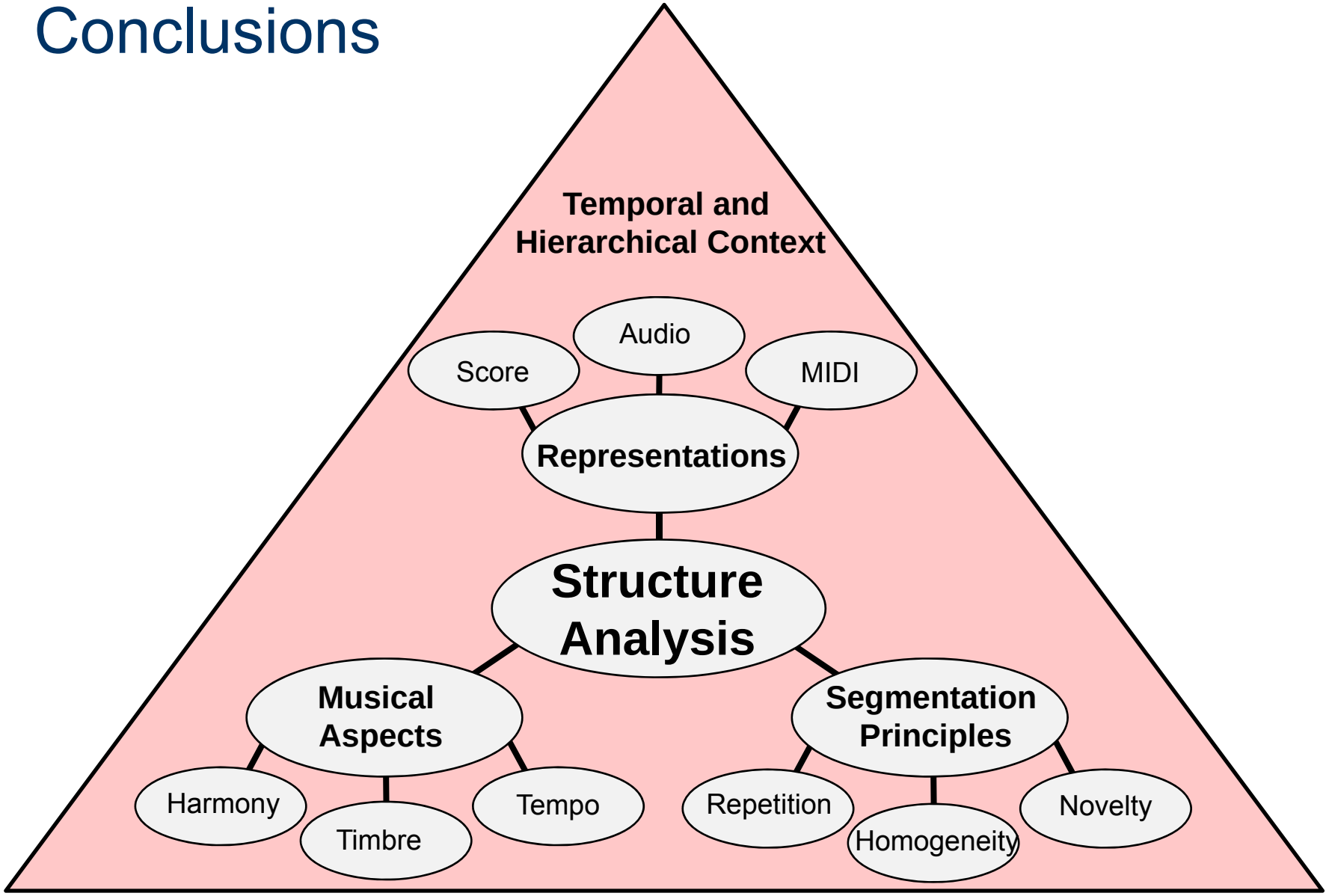
Conclusions



Conclusions

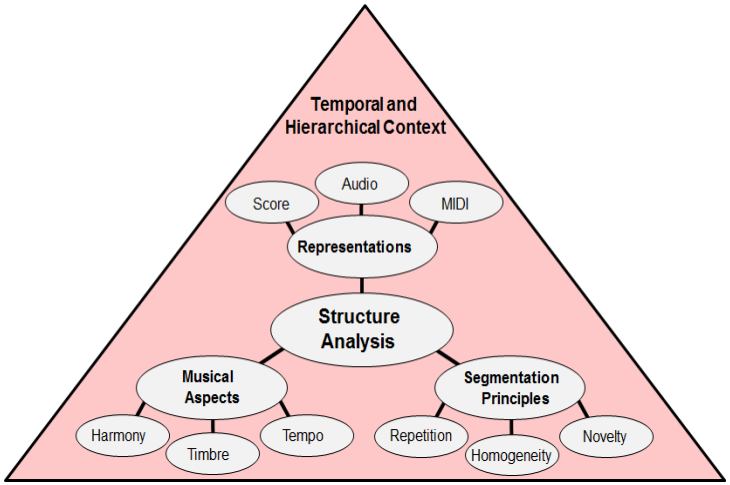


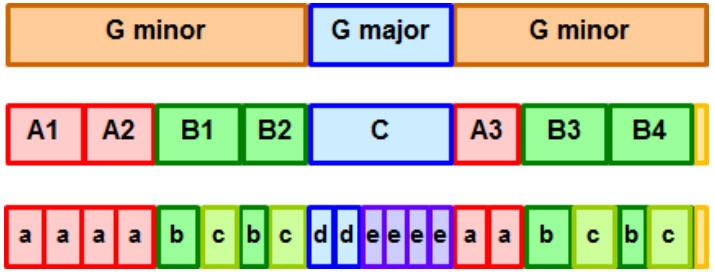
Conclusions



Conclusions

- Combined Approaches
- Hierarchical Approaches
- Evaluation
- Explaining Structure





- MIREX
- SALAMI-Project
- Smith, Chew

Links

- SM Toolbox (MATLAB)
  http://www.audiolabs-erlangen.de/resources/MIR/SMtoolbox/
- MSAF: Music Structure Analysis Framework (Python)
  https://github.com/urinieto/msaf
- SALAMI Annotation Data
  http://ddmal.music.mcgill.ca/research/salami/annotations
- LibROSA (Python)
  https://librosa.github.io/librosa/
- Evaluation: mir_eval (Python)
  https://craffel.github.io/mir_eval/
- Deep Learning: Boundary Detection
  Jan Schlüter (PhD thesis)