Lecture

Music Processing

Tempo and Beat Tracking

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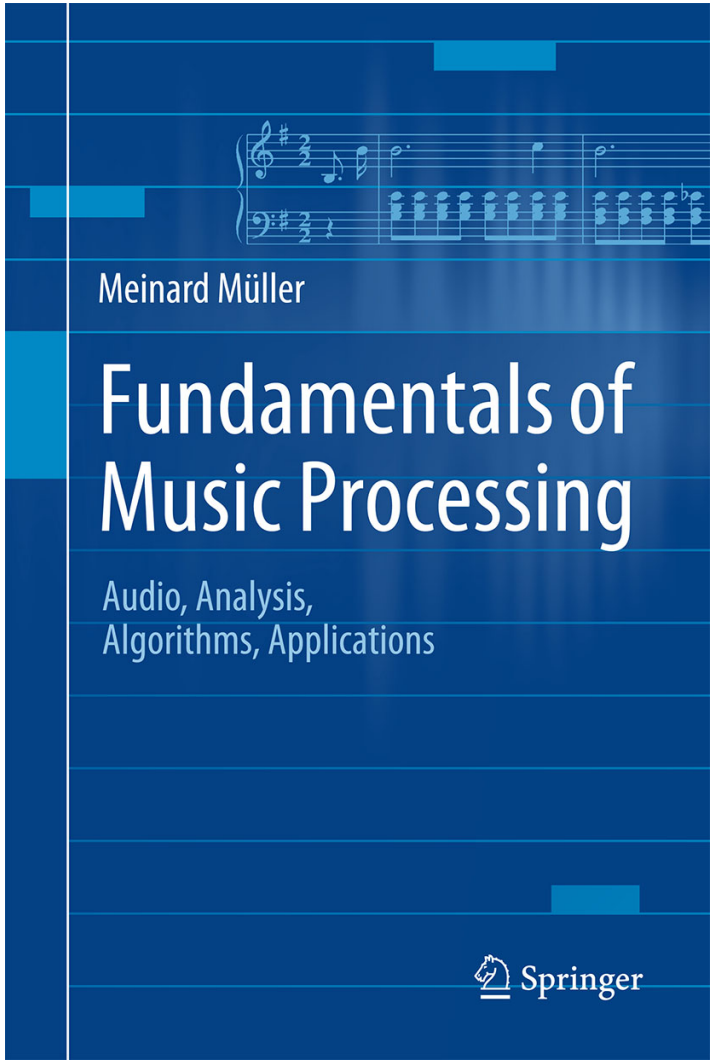
Book: Fundamentals of Music Processing



Meinard Müller
Fundamentals of Music Processing
Audio, Analysis, Algorithms, Applications
483 p., 249 illus., hardcover
ISBN: 978-3-319-21944-8
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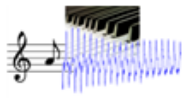
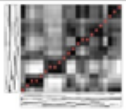
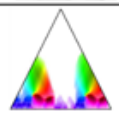
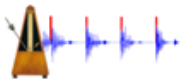
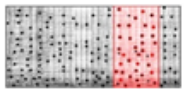
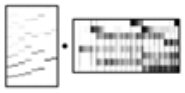
Accompanying website:
www.music-processing.de

Book: Fundamentals of Music Processing

Chapter		Music Processing Scenario
1		Music Represenations
2		Fourier Analysis of Signals
3		Music Synchronization
4		Music Structure Analysis
5		Chord Recognition
6		Tempo and Beat Tracking
7		Content-Based Audio Retrieval
8		Musically Informed Audio Decomposition

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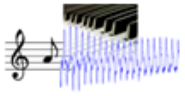
1		Music Represenations
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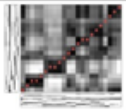
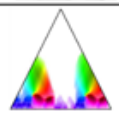
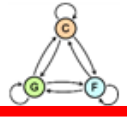
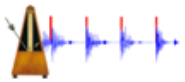
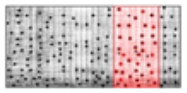
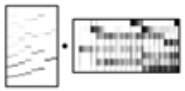
3		Music Synchronization
4		Music Structure Analysis
5		Chord Recognition
6		Tempo and Beat Tracking
7		Content-Based Audio Retrieval
8		Musically Informed Audio Decomposition

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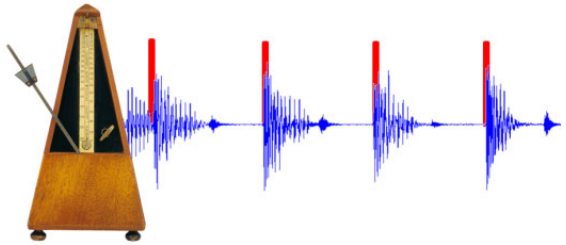
Chapter 6: Tempo and Beat Tracking



Tempo and beat are further fundamental properties of music. In Chapter 6, we introduce the basic ideas on how to extract tempo-related information from audio recordings. In this scenario, a first challenge is to locate note onset information—a task that requires methods for detecting changes in energy and spectral content. To derive tempo and beat information, note onset candidates are then analyzed with regard to quasiperiodic patterns. This leads us to the study of general methods for local periodicity analysis of time series.

Introduction

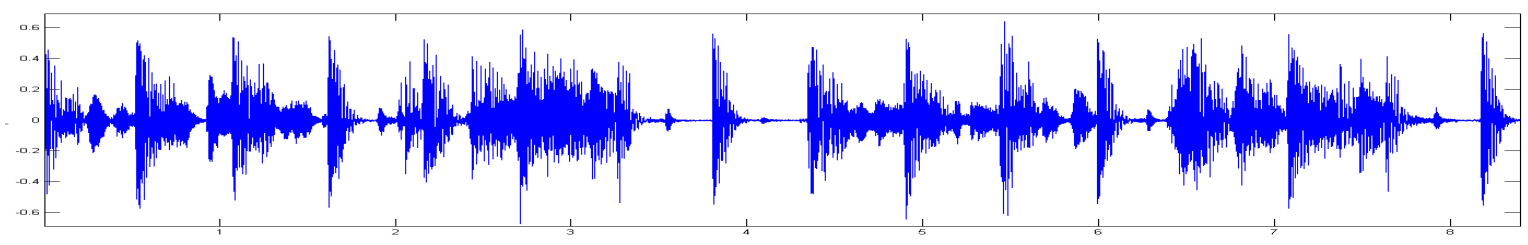
Basic beat tracking task:

Given an audio recording of a piece of music,
determine the periodic sequence of beat positions.

“Tapping the foot when listening to music”

Introduction

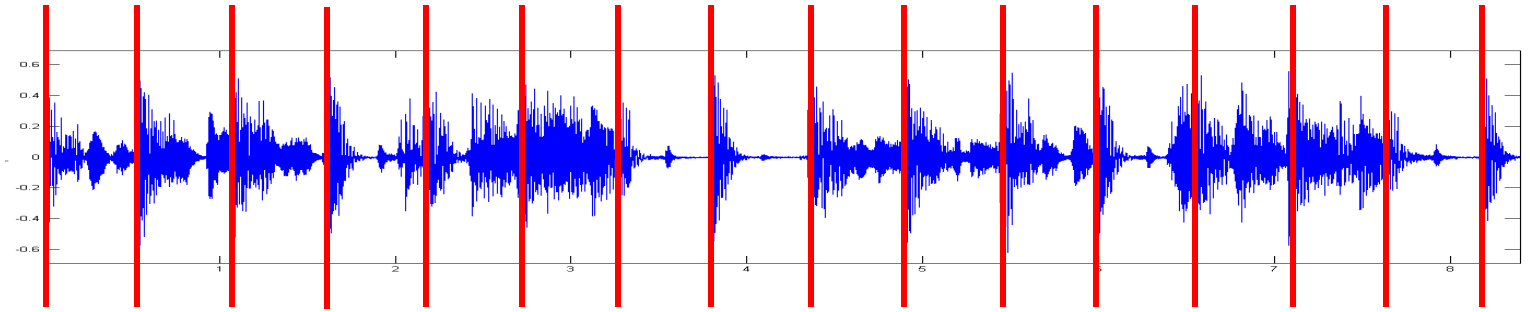
Example: Queen – Another One Bites The Dust



Time (seconds)

Introduction

Example: Queen – Another One Bites The Dust

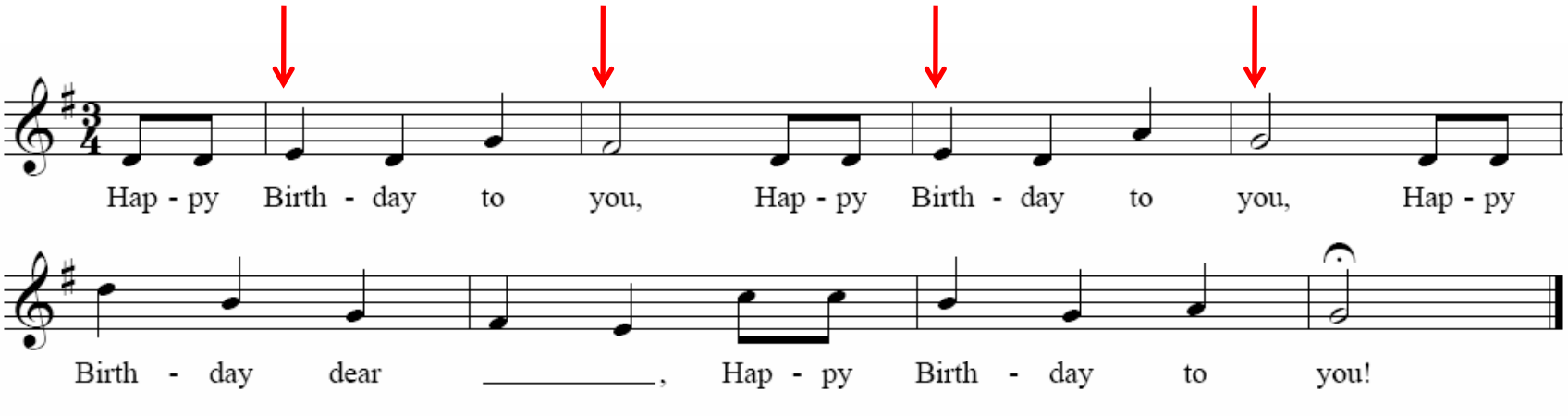


Time (seconds)

Introduction

Example: Happy Birthday to you

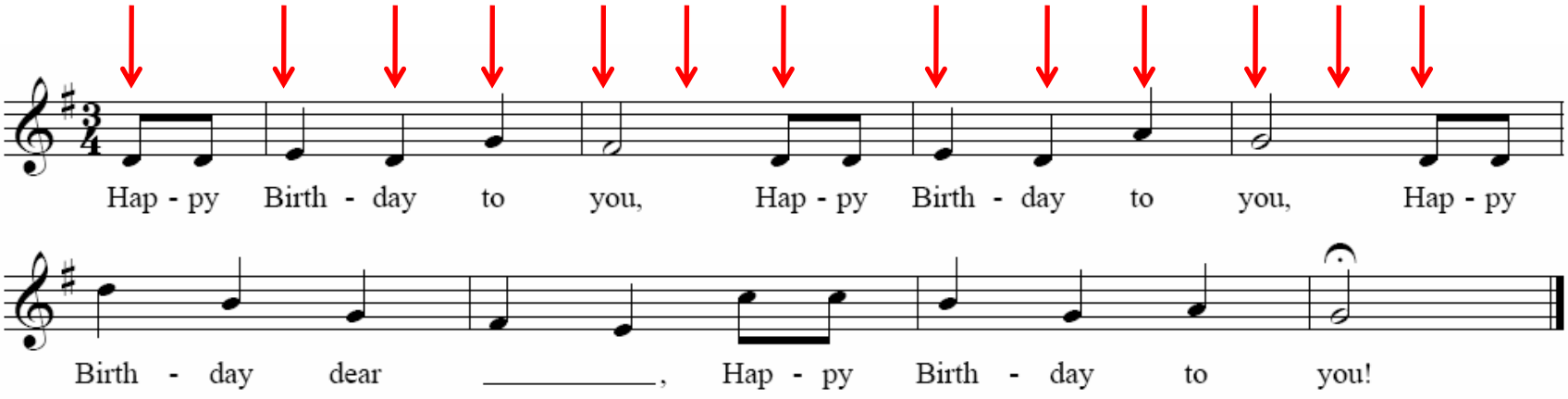
Pulse level: **Measure**



Introduction

Example: Happy Birthday to you

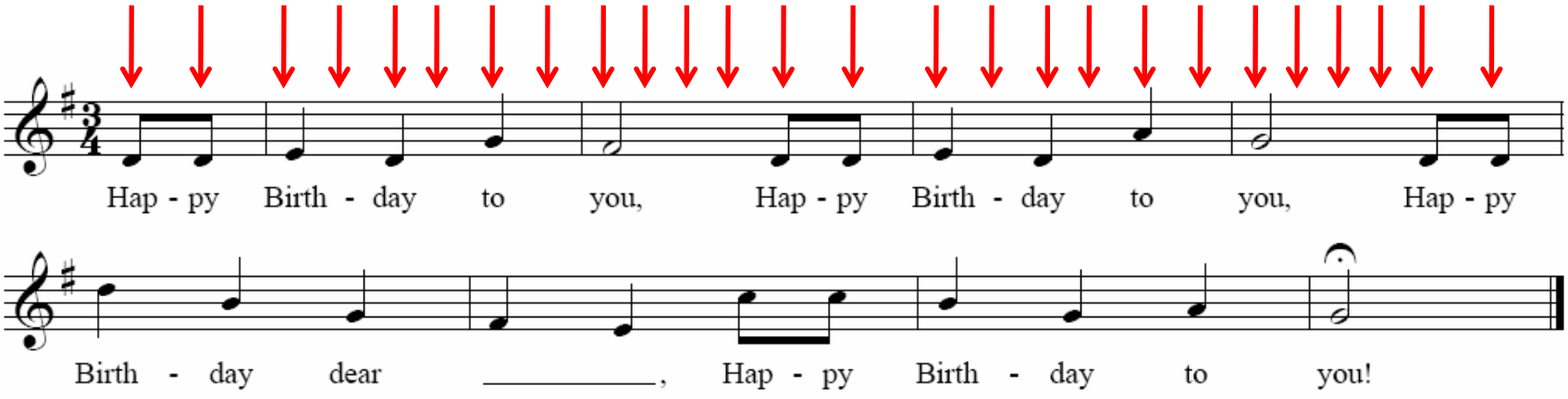
Pulse level: **Tactus (beat)**



Introduction

Example: Happy Birthday to you

Pulse level: **Tatum (temporal atom)**



Introduction

Example: Chopin – Mazurka Op. 68-3

Pulse level: Quarter note

Tempo: ???

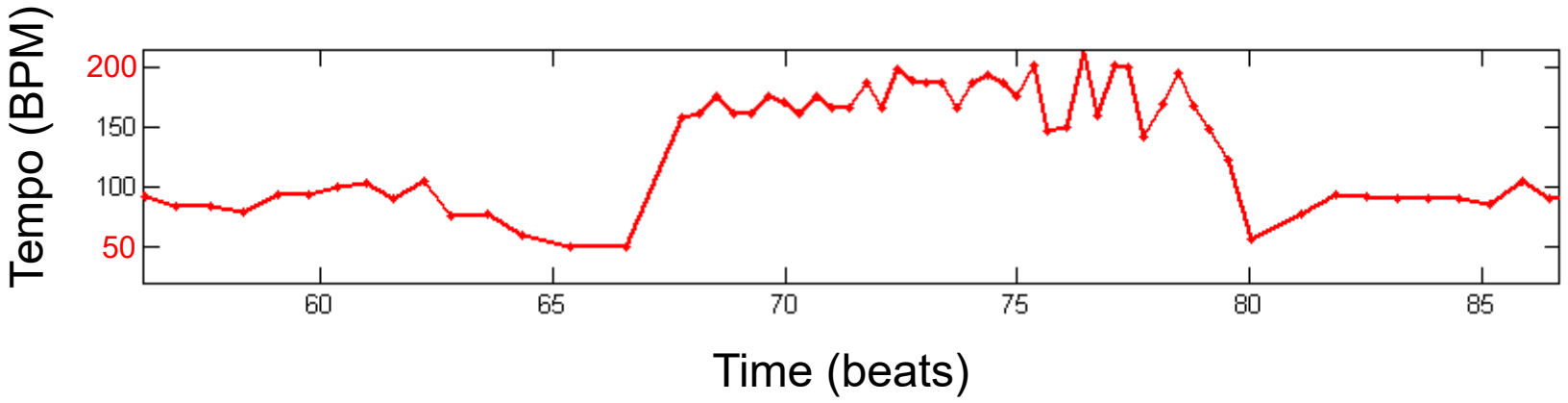
Introduction

Example: Chopin – Mazurka Op. 68-3

Pulse level: Quarter note

Tempo: 50-200 BPM

Tempo curve



Introduction

Example: Borodin – String Quartet No. 2

Pulse level: Quarter note

Tempo: 120-140 BPM (roughly)

Beat tracker without any prior knowledge 

Beat tracker with prior knowledge on rough tempo range 

Introduction

Challenges in beat tracking

- Pulse level often unclear
- Local/sudden tempo changes (e.g. rubato)
- Vague information

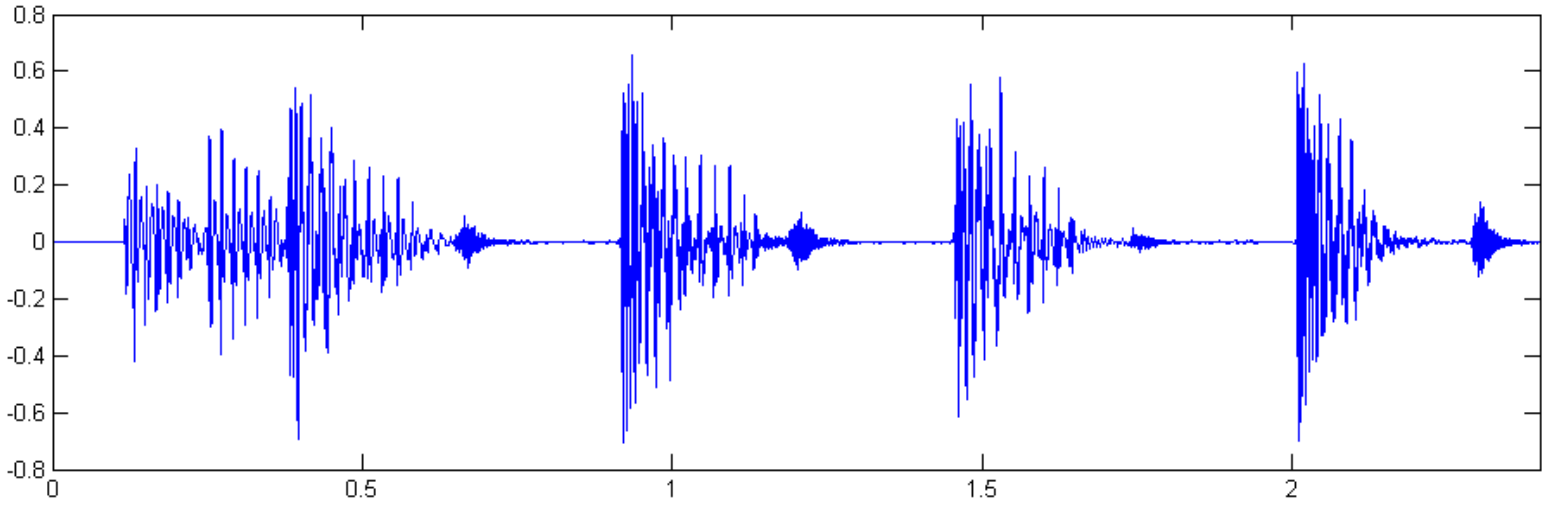
  (e.g., soft onsets, extracted onsets corrupt)
- Sparse information

  (often only note onsets are used)

Introduction

Tasks

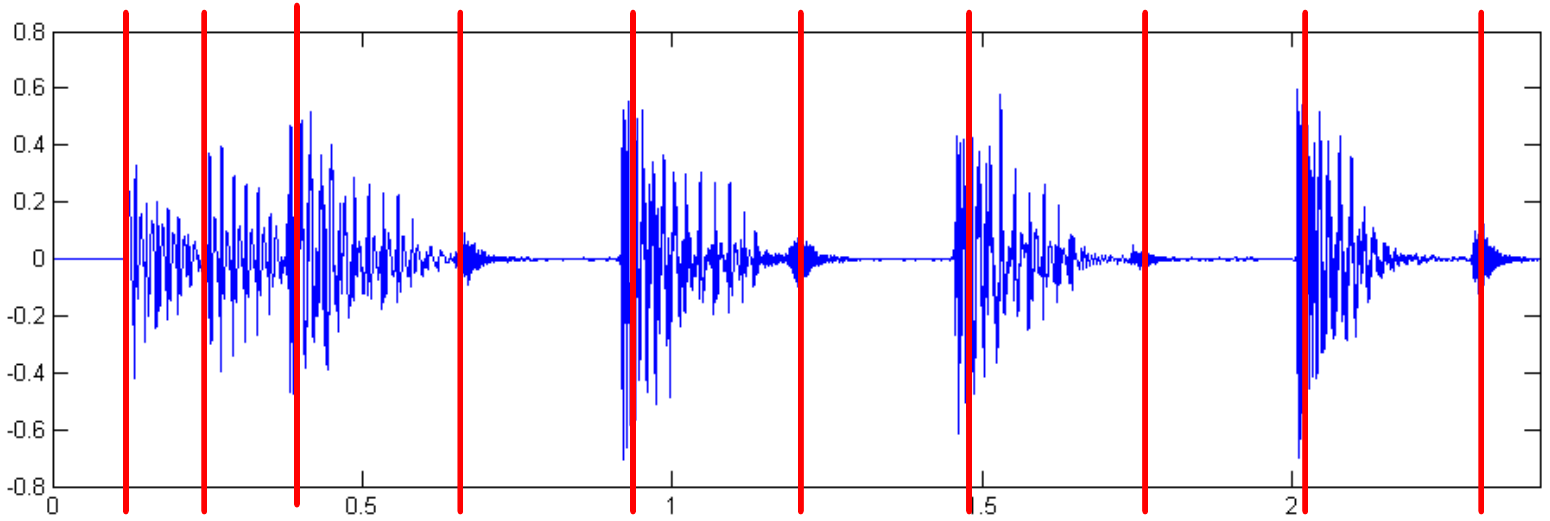
- Onset detection
- Beat tracking
- Tempo estimation



Introduction

Tasks

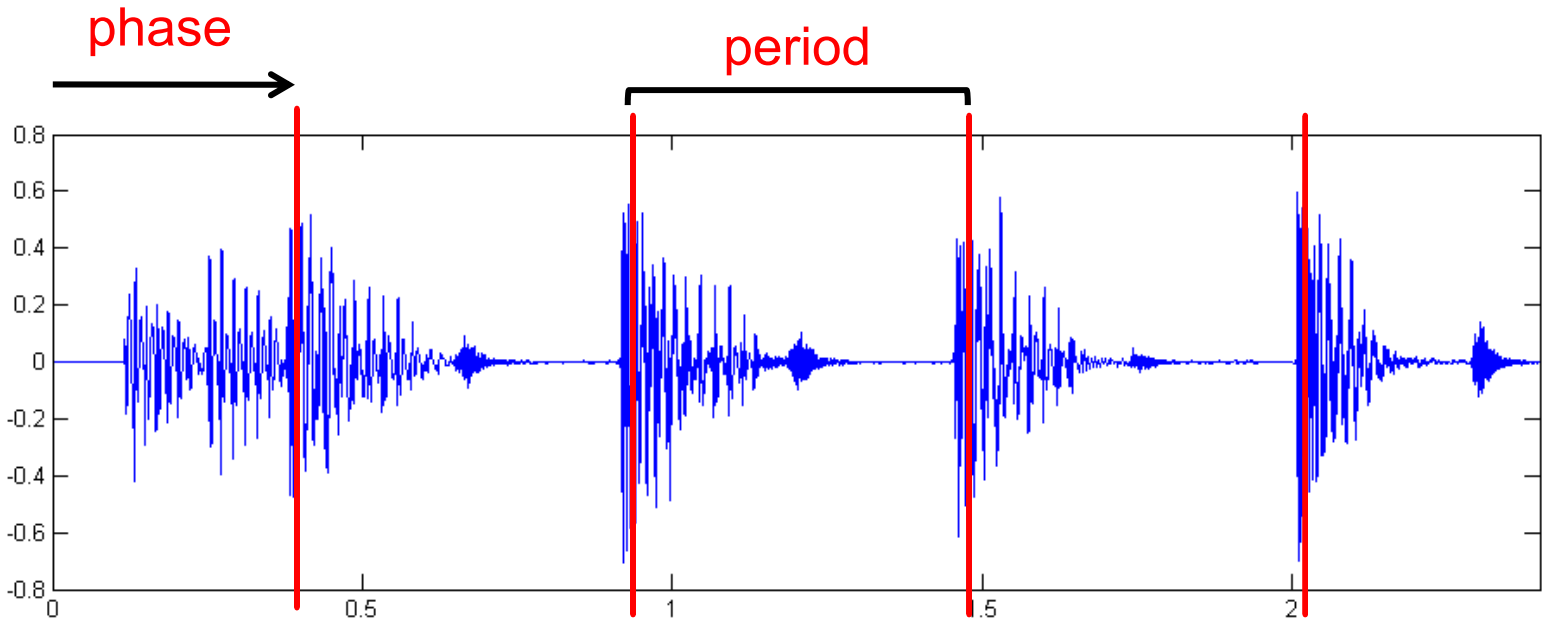
- Onset detection
- Beat tracking
- Tempo estimation



Introduction

Tasks

- Onset detection
- Beat tracking
- Tempo estimation



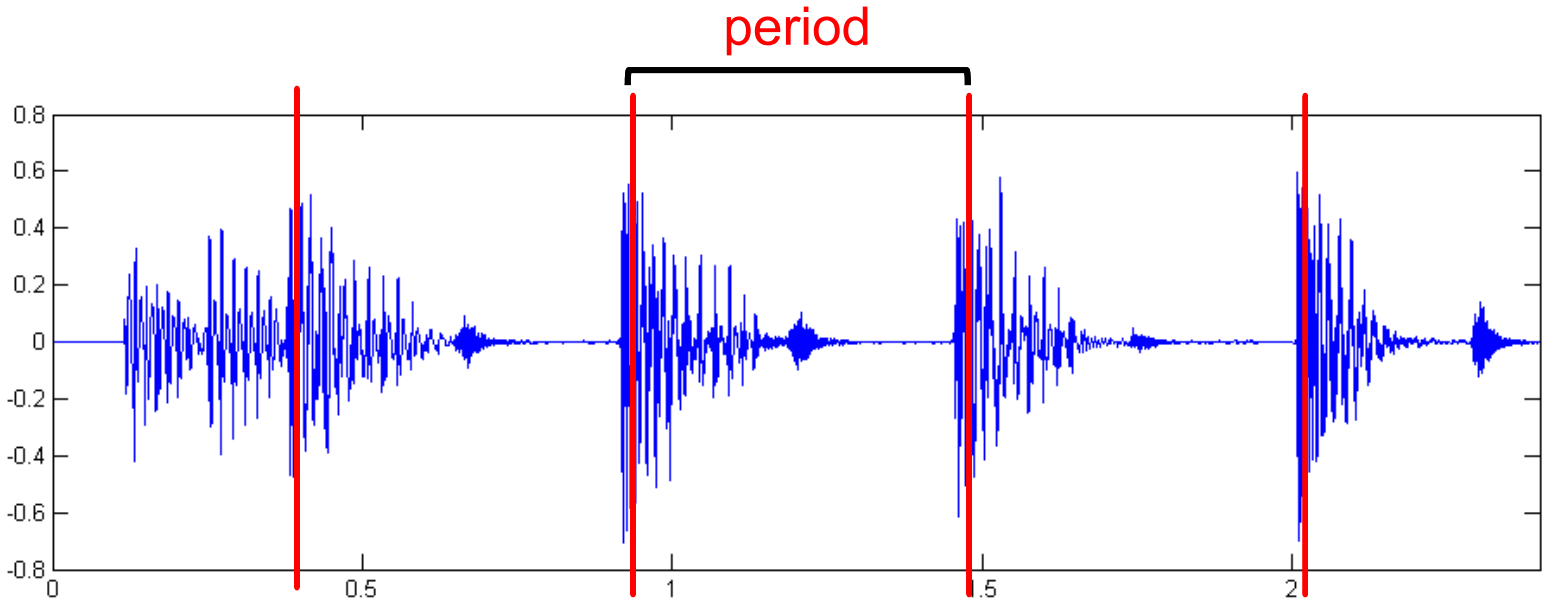
Introduction

Tasks

- Onset detection
- Beat tracking
- Tempo estimation

Tempo := 60 / period

Beats per minute (BPM)

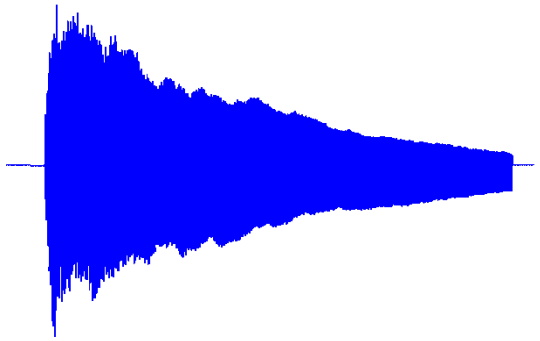


Onset Detection

- Finding start times of perceptually relevant acoustic events in music signal
- Onset is the time position where a note is played
- Onset typically goes along with a change of the signal's properties:
  - energy or loudness
  - pitch or harmony
  - timbre

Onset Detection

- Finding start times of perceptually relevant acoustic events in music signal



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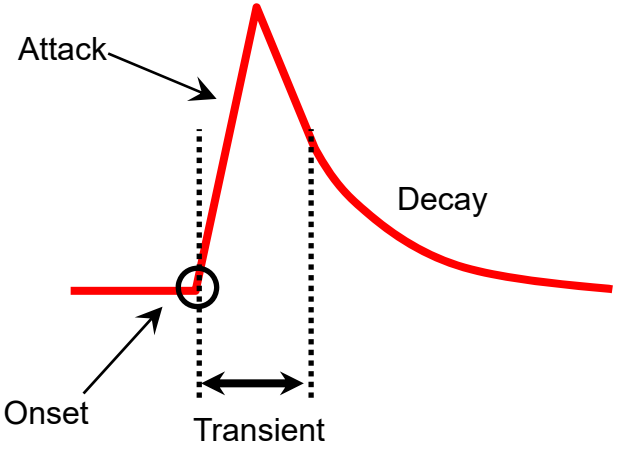
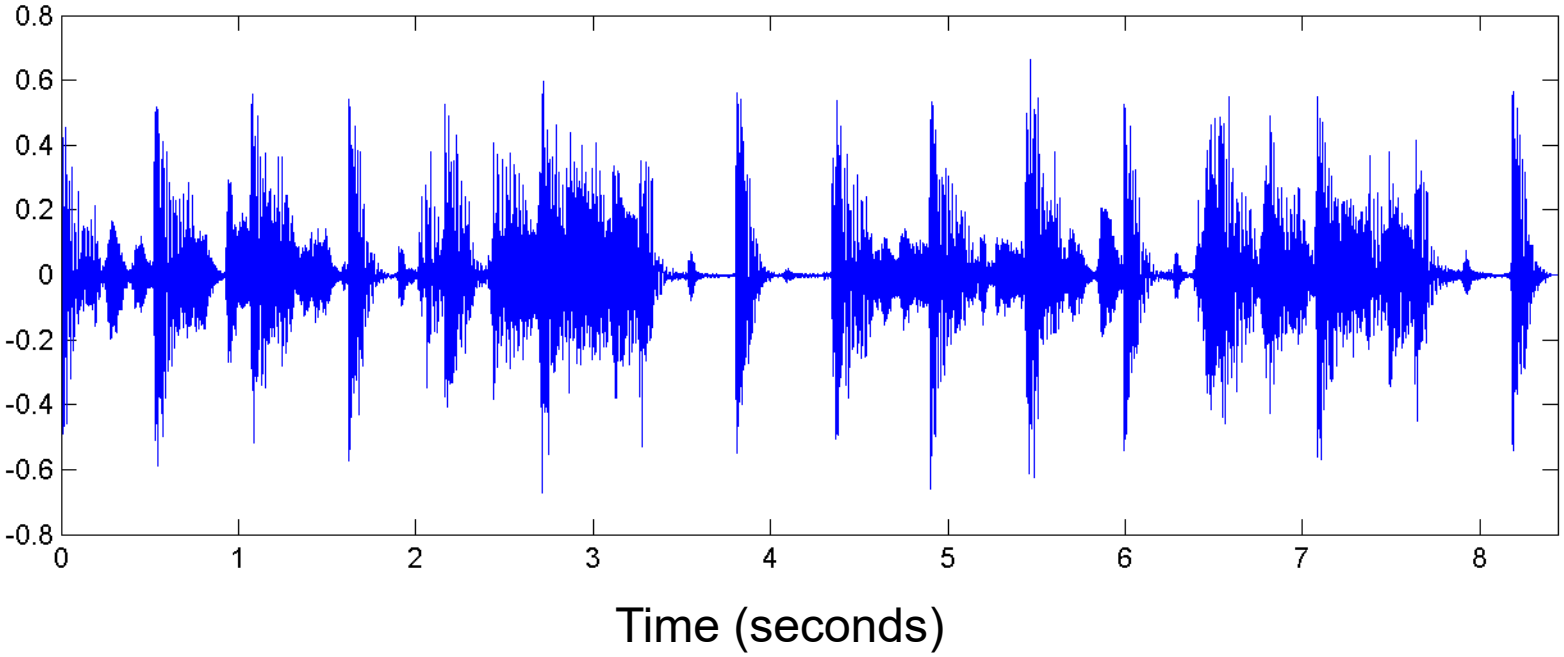


Onset Detection (Energy-Based)

Steps

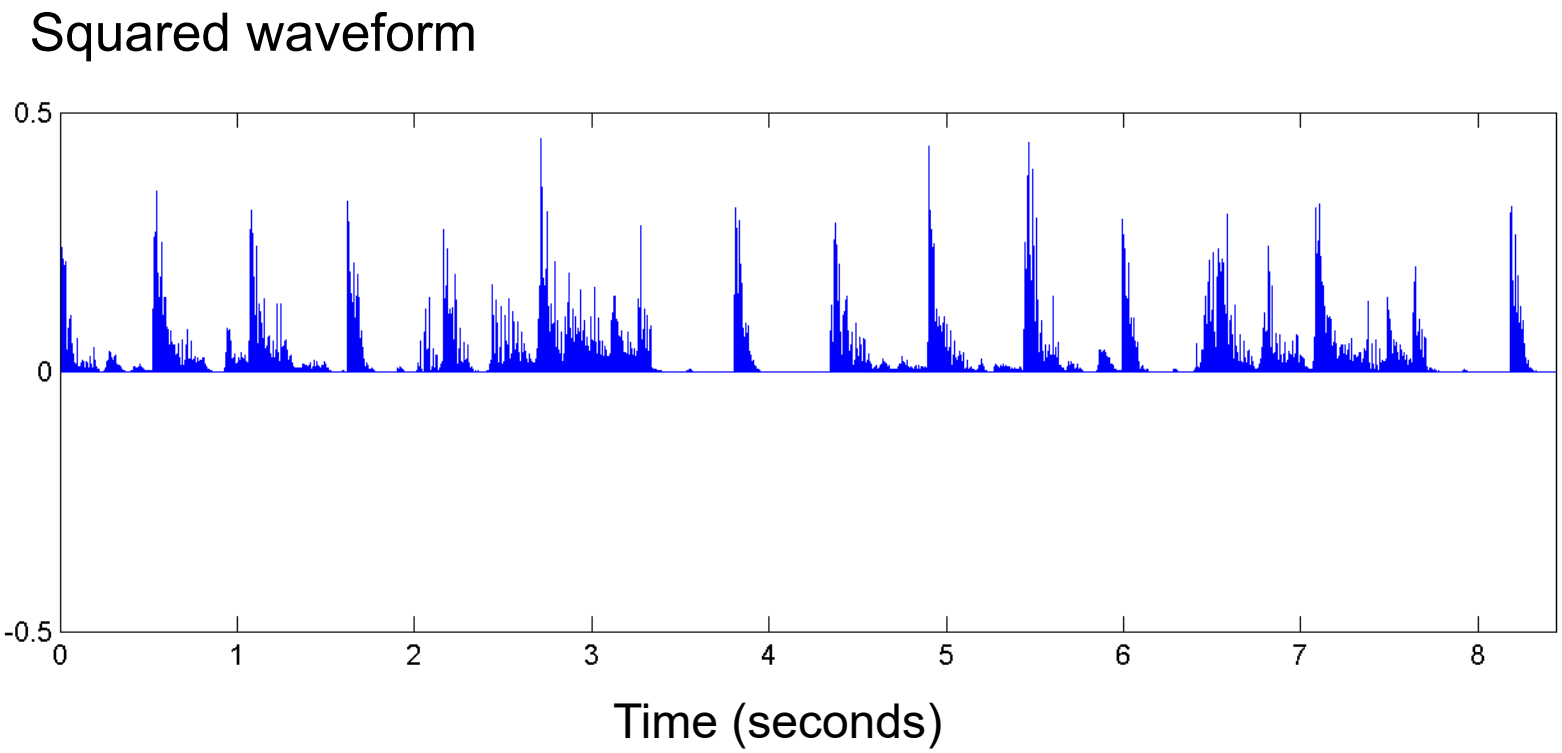
Waveform



Onset Detection (Energy-Based)

Steps

1. Amplitude squaring

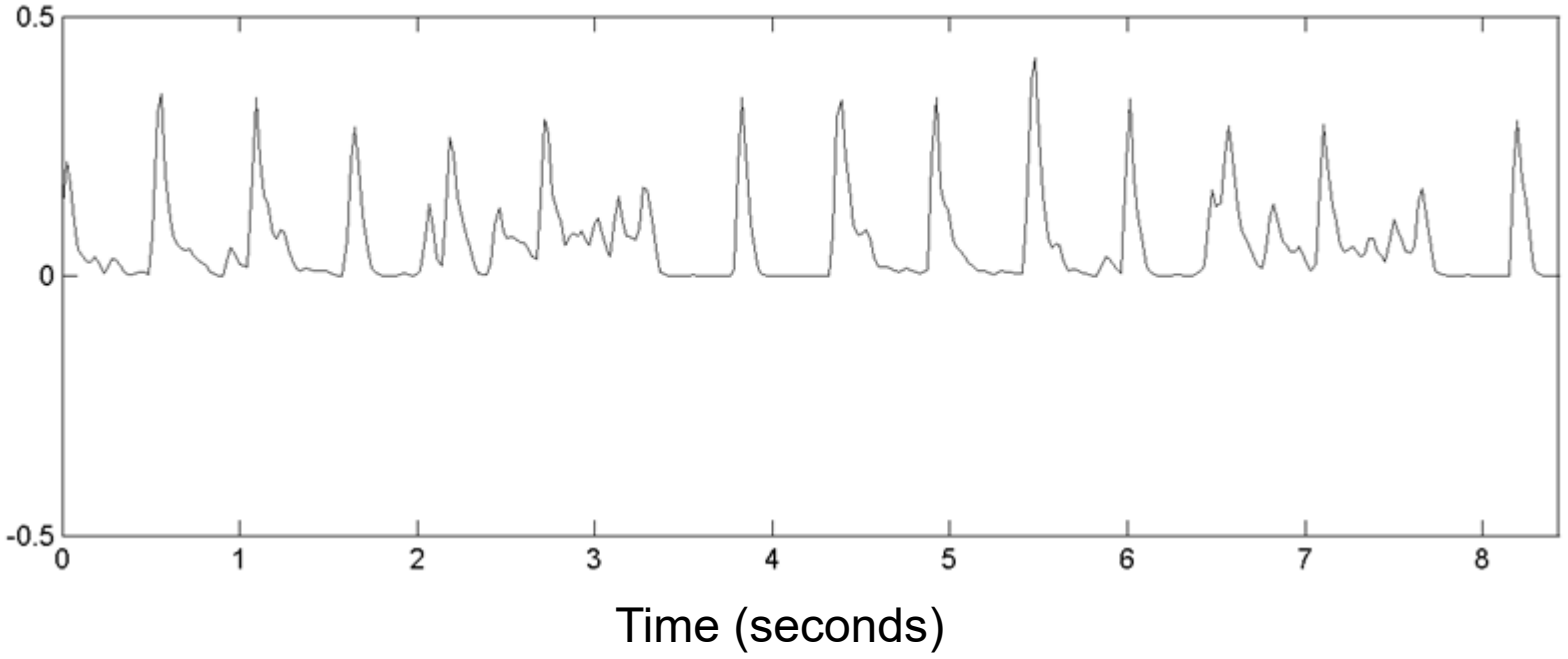


Onset Detection (Energy-Based)

Steps

1. Amplitude squaring
2. Windowing

Energy envelope



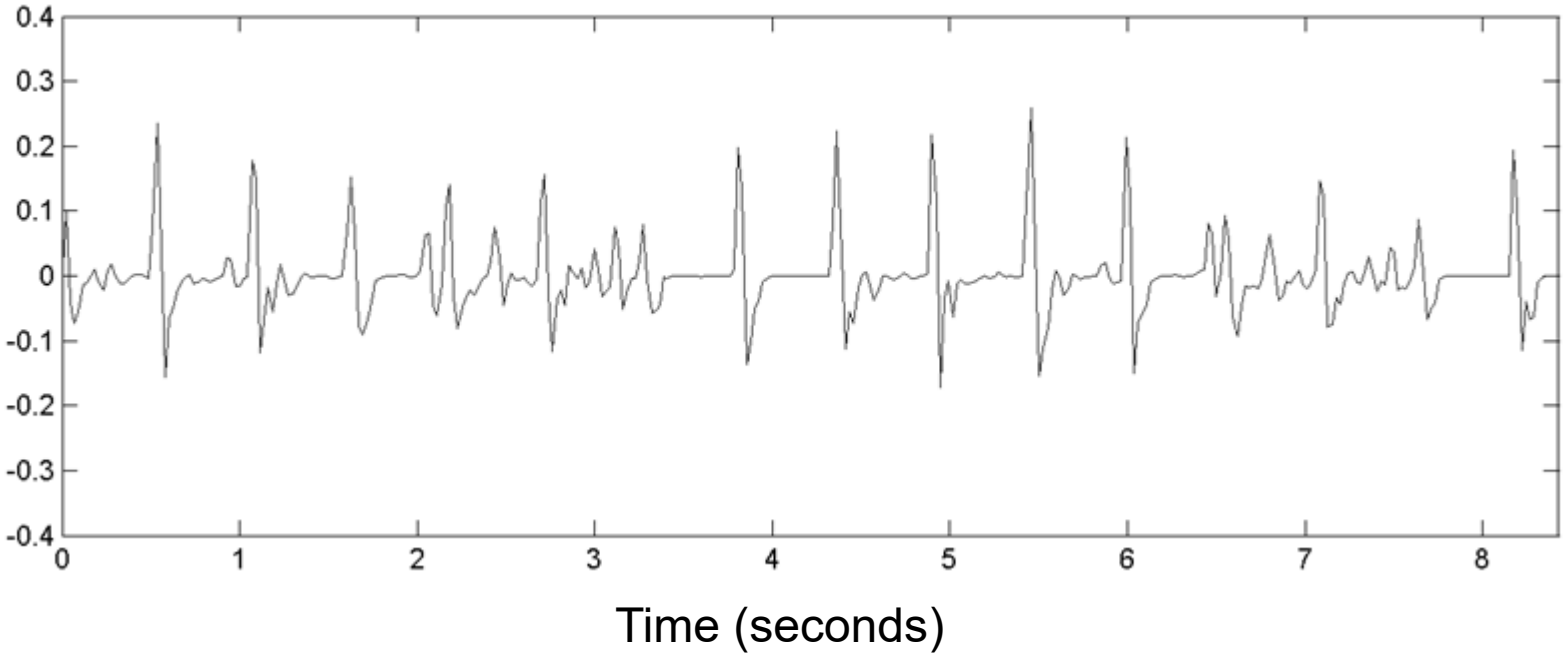
Onset Detection (Energy-Based)

Steps

1. Amplitude squaring
2. Windowing
3. Differentiation

Capturing energy changes

Differentiated energy envelope



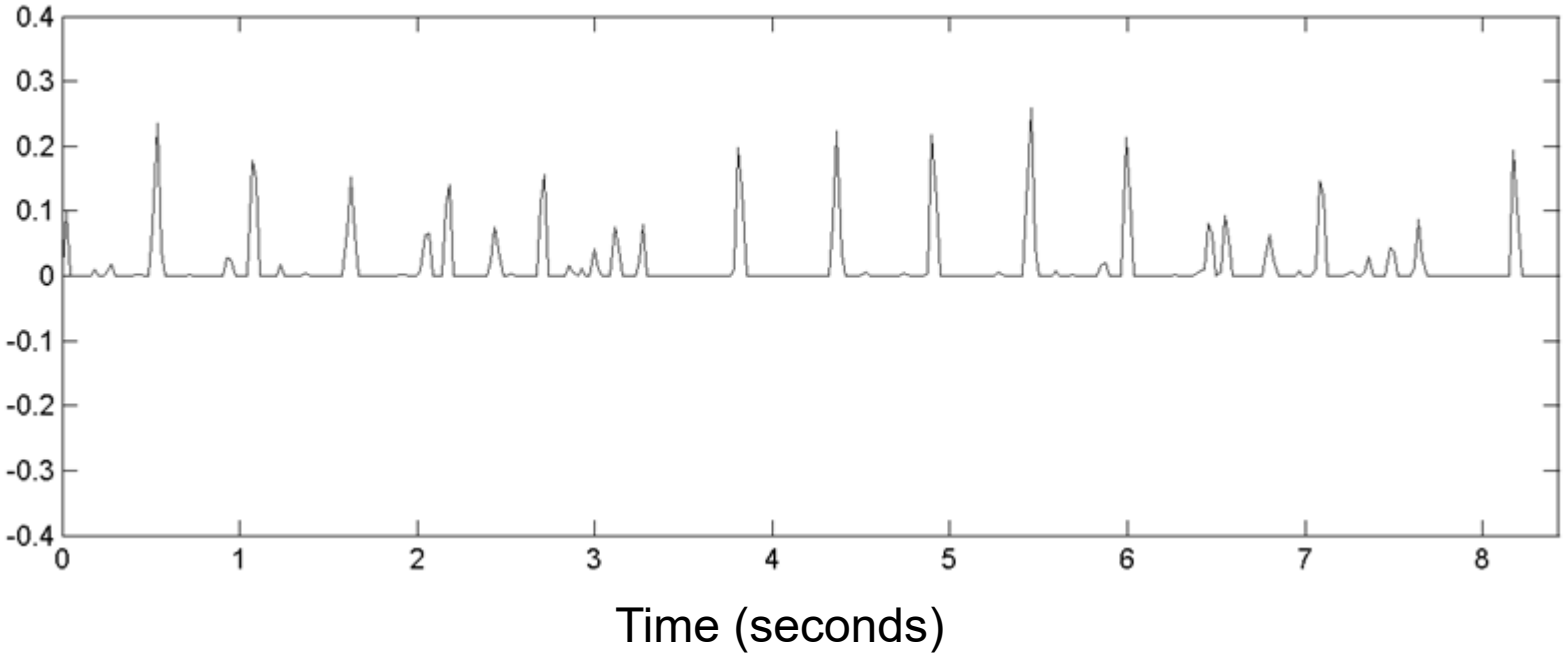
Onset Detection (Energy-Based)

Steps

1. Amplitude squaring
2. Windowing
3. Differentiation
4. Half wave rectification

Only energy increases are relevant for note onsets

Novelty curve

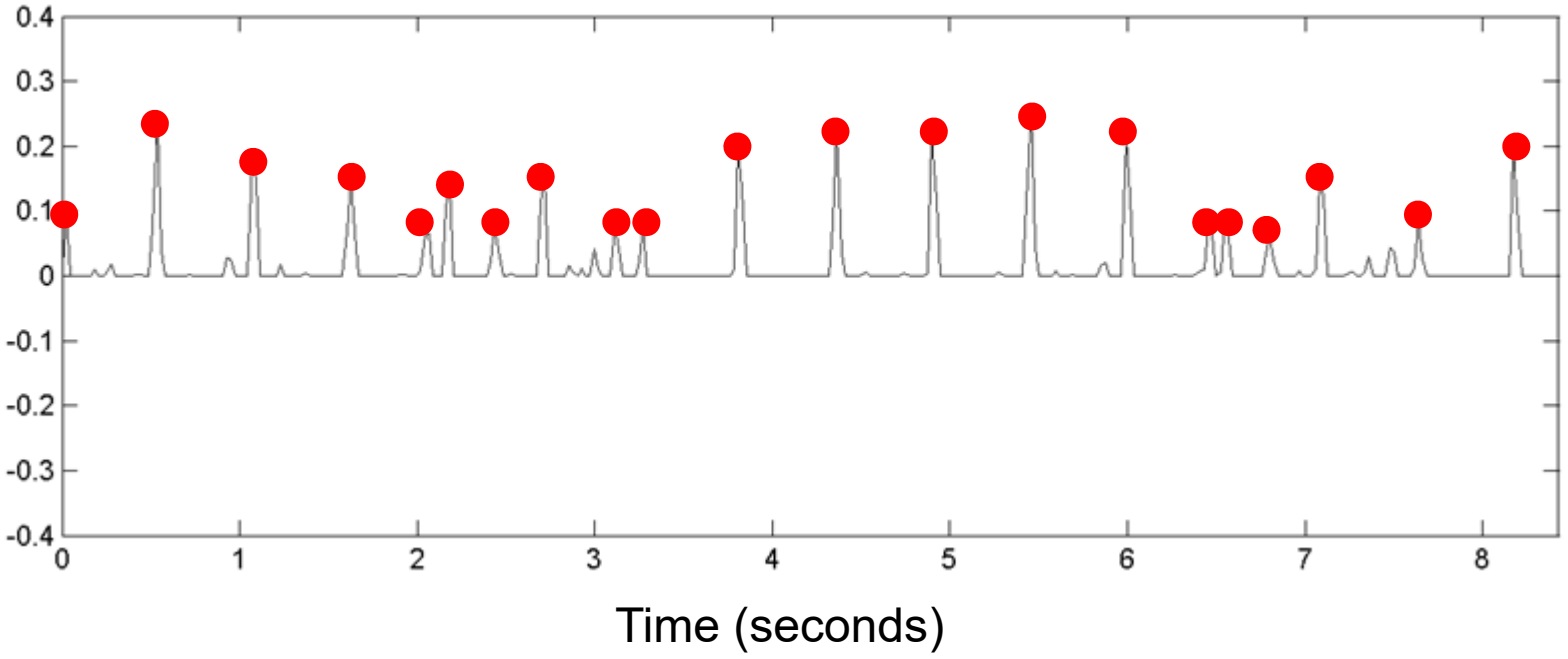


Onset Detection (Energy-Based)

Steps

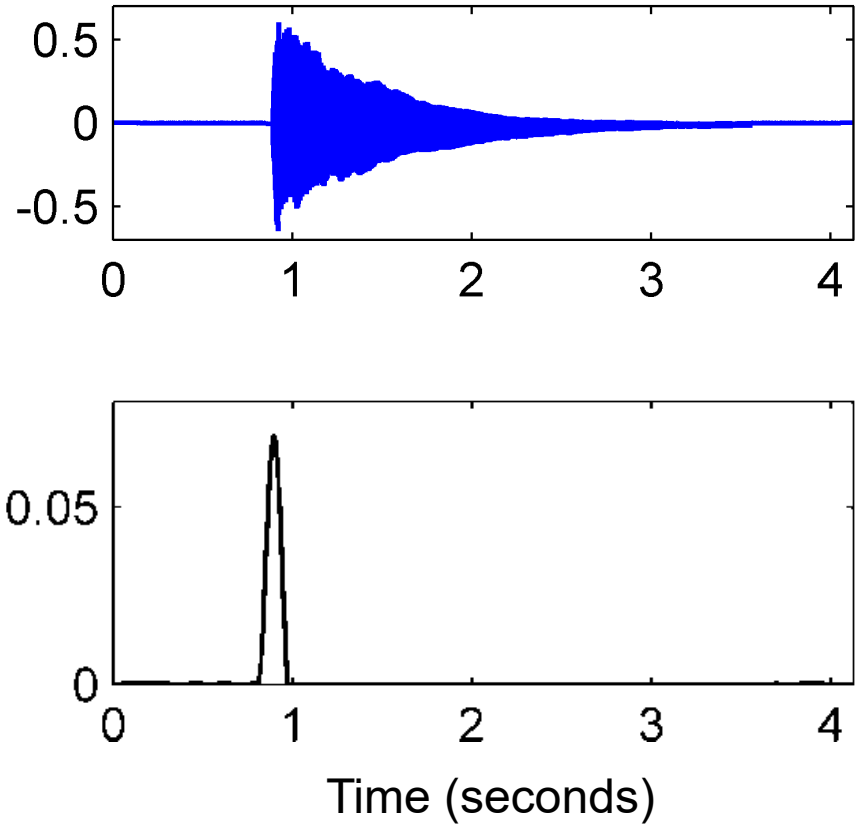
1. Amplitude squaring
2. Windowing
3. Differentiation
4. Half wave rectification
5. Peak picking

Peak positions indicate note onset candidates



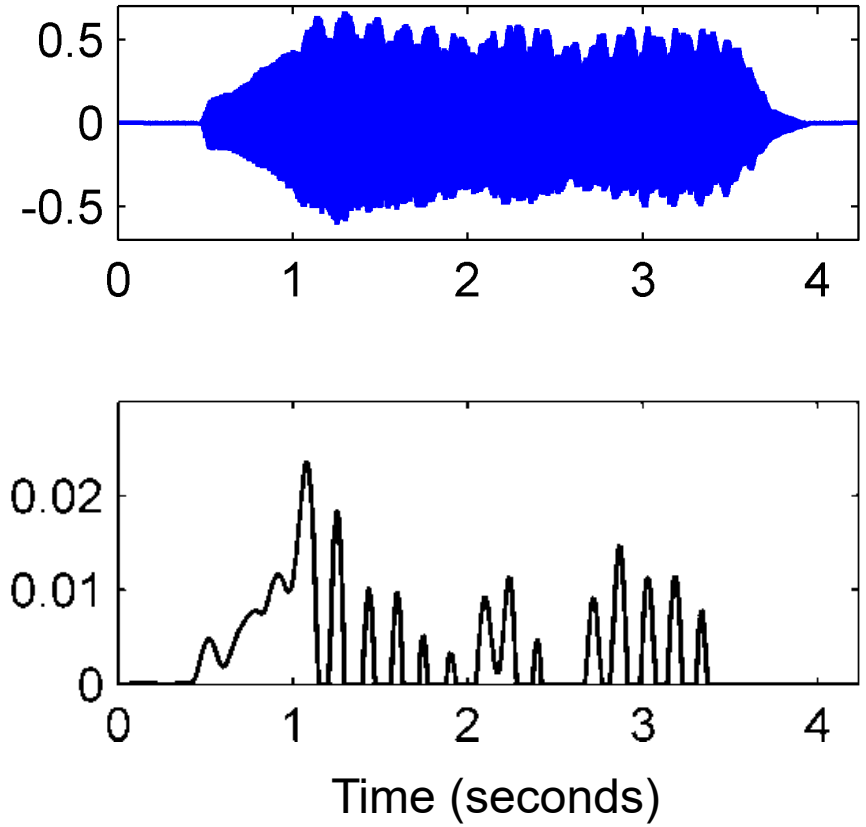
Onset Detection (Energy-Based)

Example: C4 played by piano



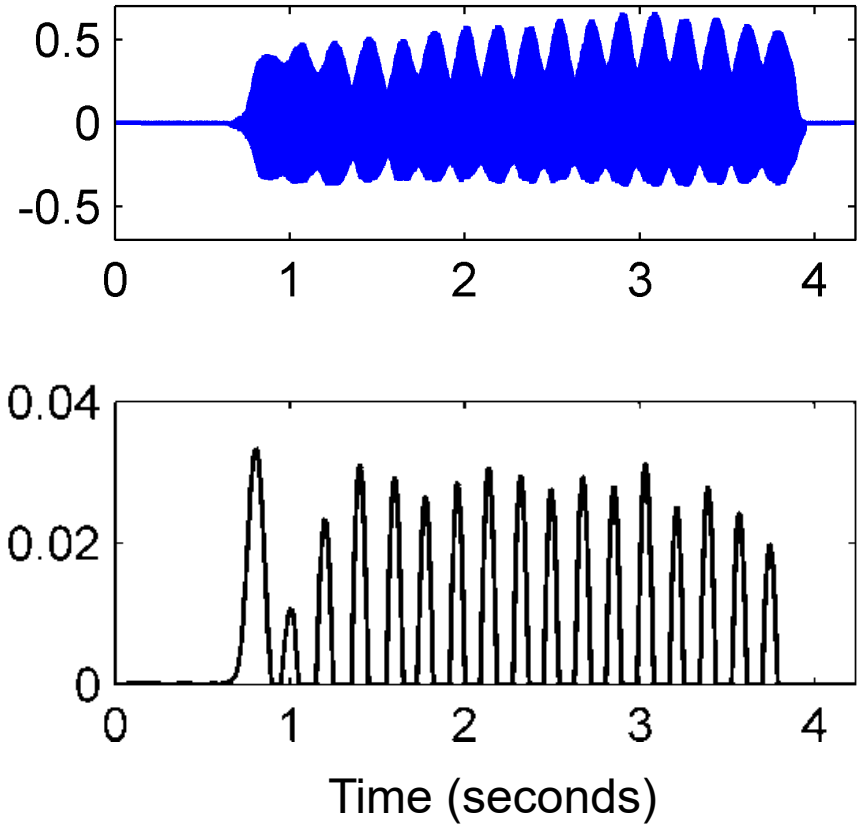
Onset Detection (Energy-Based)

Example: C4 played by violin



Onset Detection (Energy-Based)

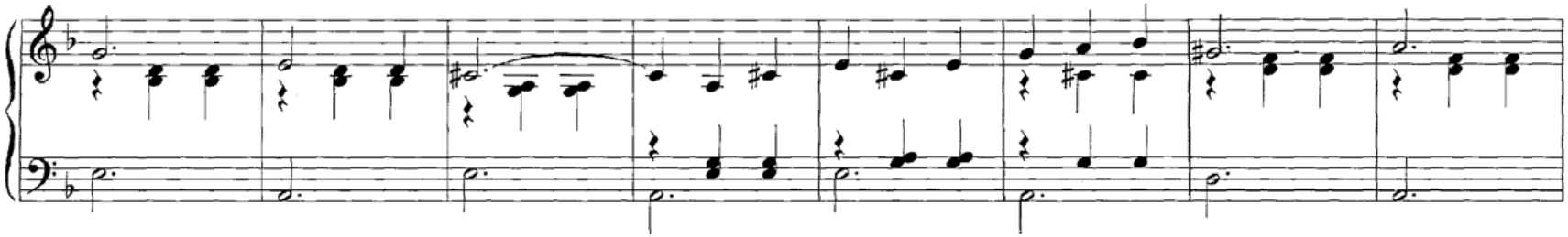
Example: C4 played by flute



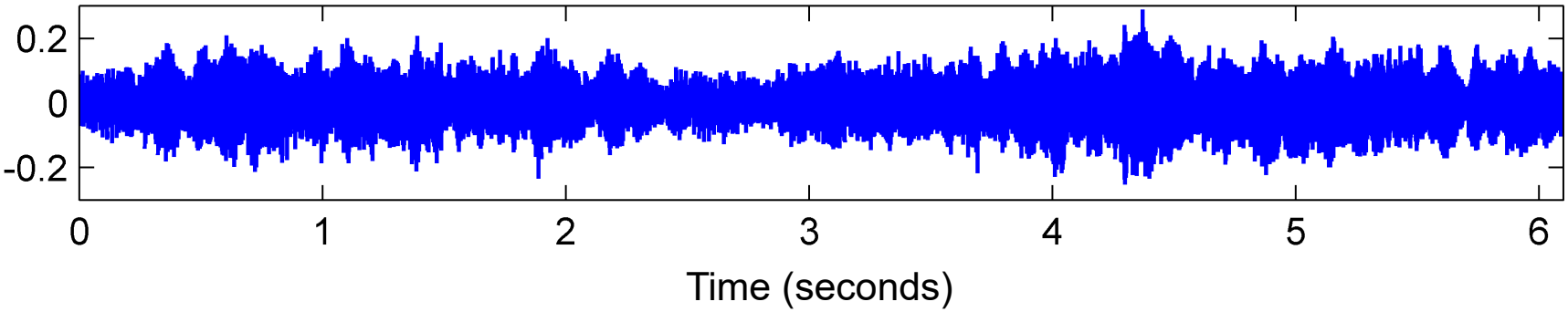
Onset Detection

- Energy curves often only work for percussive music
- Many instruments such as strings have weak note onsets
- No energy increase may be observable in complex sound mixtures
- More refined methods needed that capture
  - changes of spectral content
  - changes of pitch
  - changes of harmony

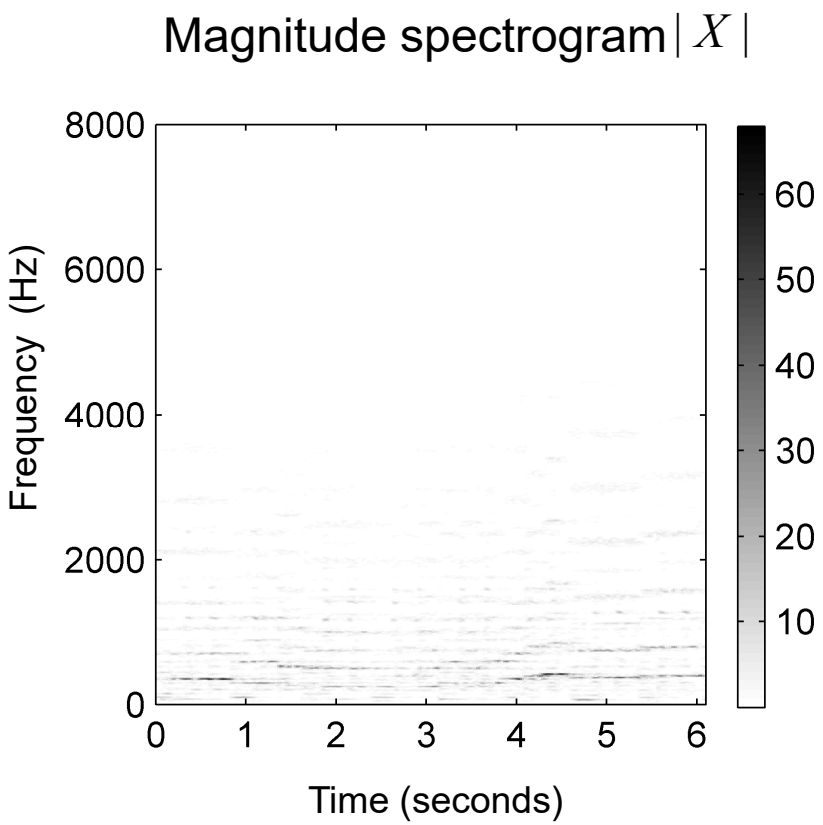
Onset Detection (Spectral-Based)



Audio recording



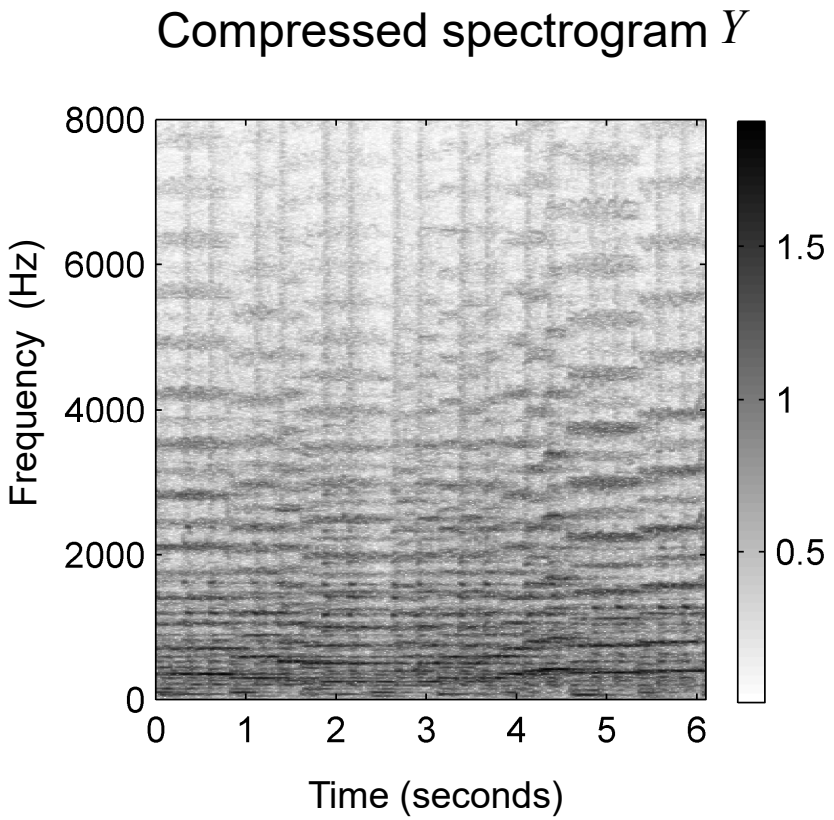
Onset Detection (Spectral-Based)



Steps:

1. Spectrogram

Onset Detection (Spectral-Based)

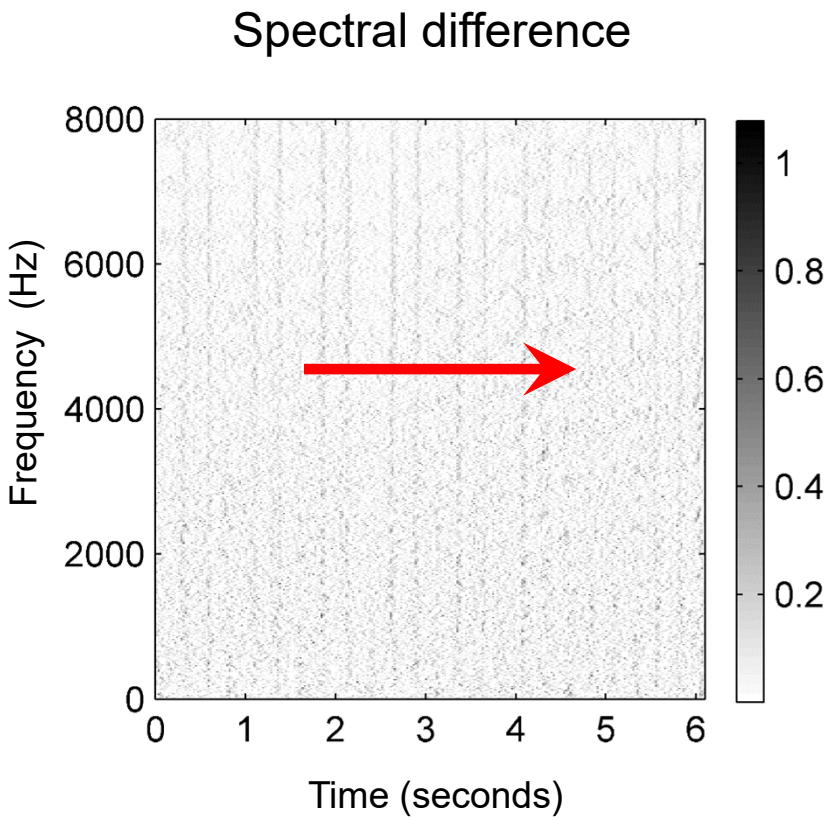


Steps:

1. Spectrogram
2. Logarithmic compression

$$Y = \log(1 + C \cdot |X|)$$

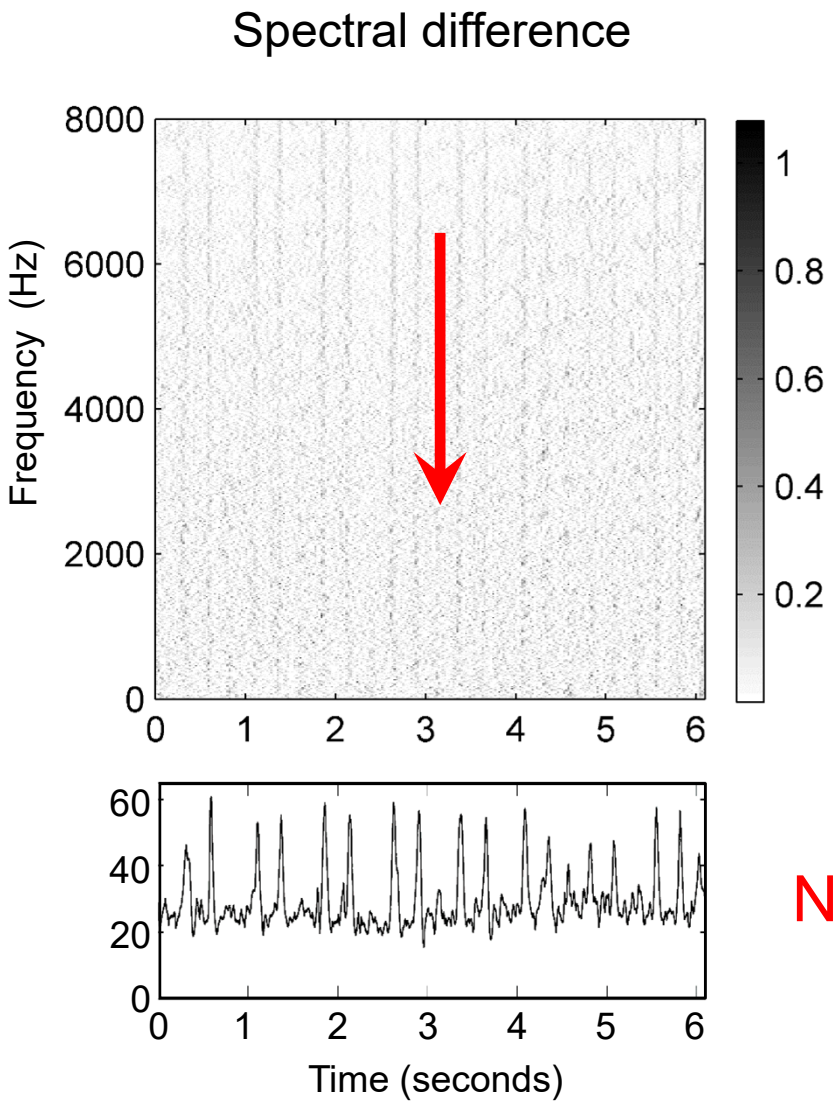
Onset Detection (Spectral-Based)



Steps:

1. Spectrogram
2. Logarithmic compression
3. Differentiation & half wave rectification

Onset Detection (Spectral-Based)



Steps:

1. Spectrogram
2. Logarithmic compression
3. Differentiation & half wave rectification
4. Accumulation

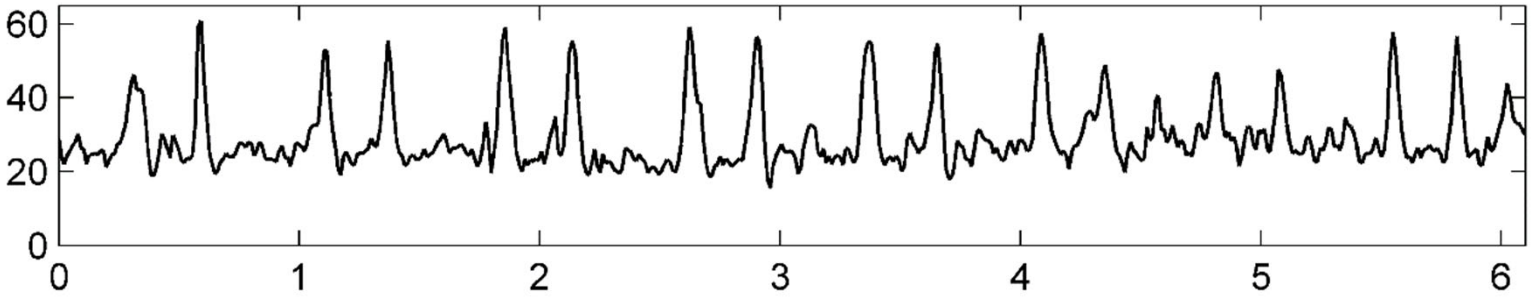
Novelty curve

Onset Detection (Spectral-Based)

Steps:

1. Spectrogram
2. Logarithmic compression
3. Differentiation & half wave rectification
4. Accumulation

Novelty curve



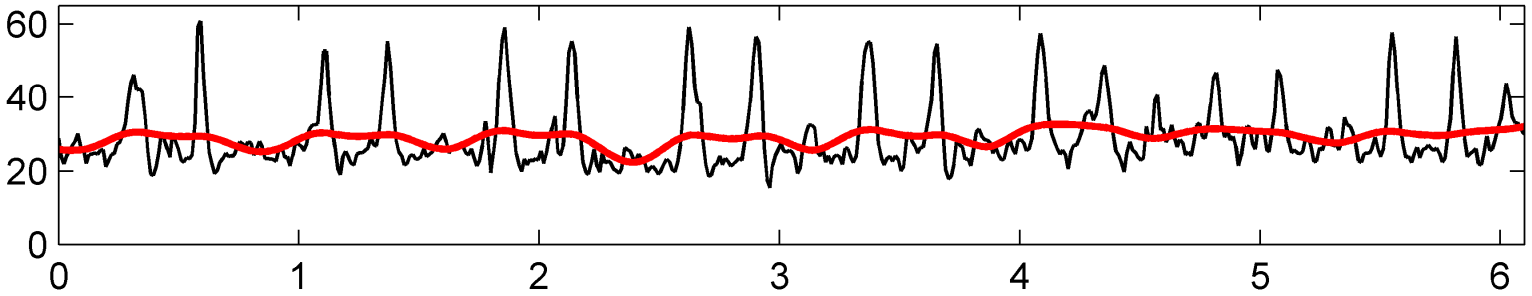
Onset Detection (Spectral-Based)

Steps:

1. Spectrogram
2. Logarithmic compression
3. Differentiation & half wave rectification
4. Accumulation
5. Normalization

Novelty curve

Substraction of local average

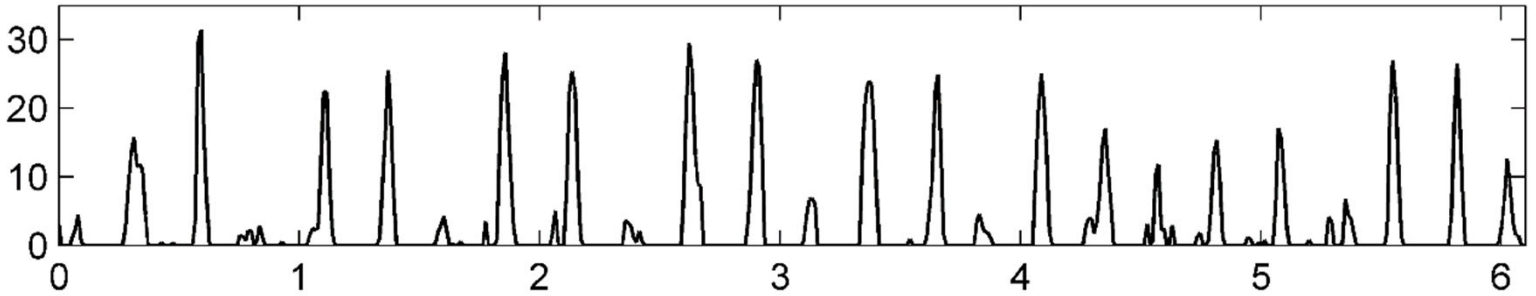


Onset Detection (Spectral-Based)

Steps:

1. Spectrogram
2. Logarithmic compression
3. Differentiation & half wave rectification
4. Accumulation
5. Normalization

Normalized novelty curve



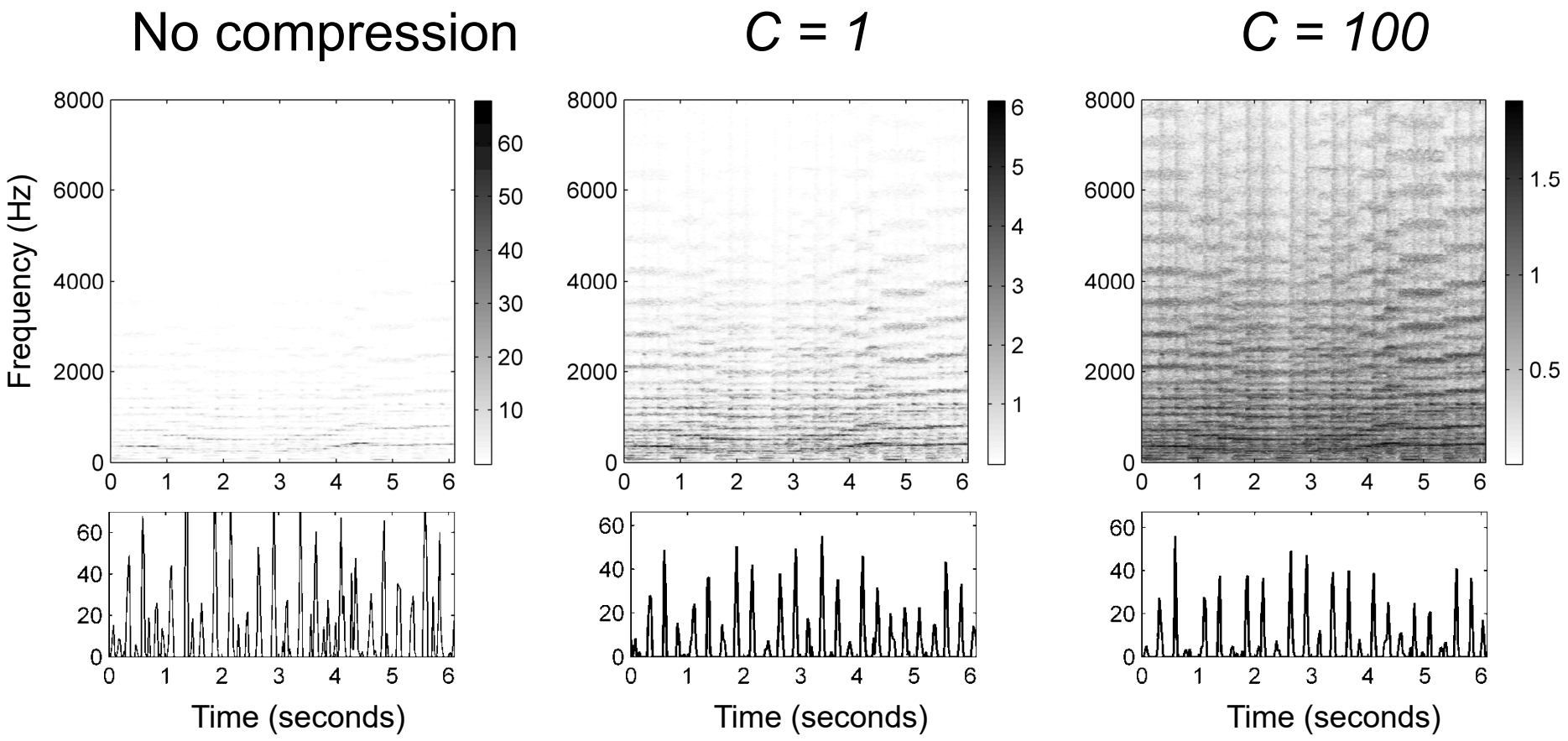
Onset Detection (Spectral-Based)

- Spectrogram $X = (X(t,k))_{t,k}$ $t \in [1:T]$ $k \in [1:K]$
- Compressed Spectrogram $Y := \log(1 + C \cdot |X|)$ $C > 1$
- Novelty curve $\Delta : [1:T-1] \to \mathbb{R}$

$$\Delta(t) := \sum_{k=1}^{K} |Y(t+1,k) - Y(t,k)|_{\geq 0}$$

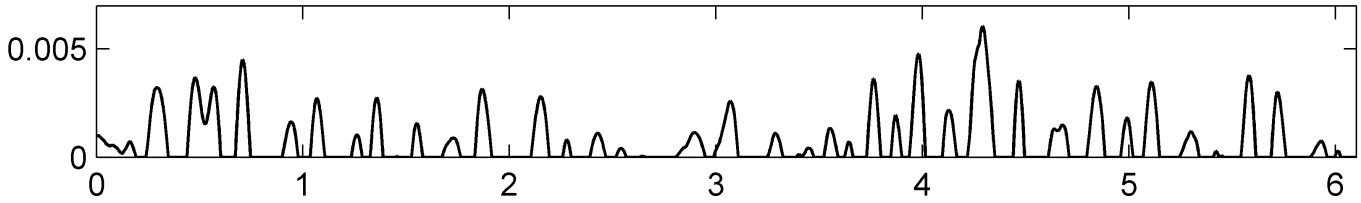
Logarithmic Compression

$$Y = \log(1 + C \cdot |X|)$$

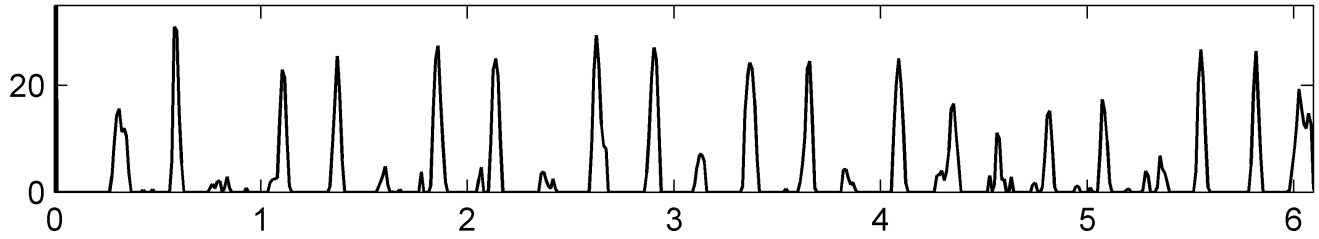


Onset Detection

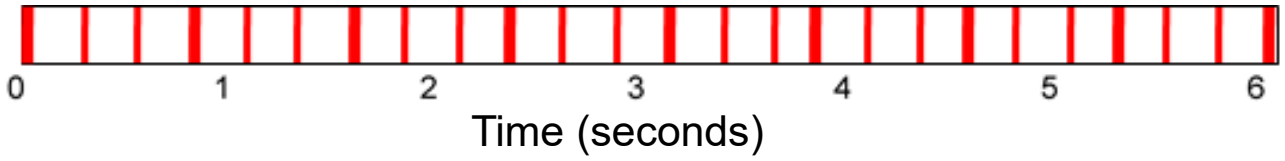
Energy-based novelty curve



Spectral-based novelty curve

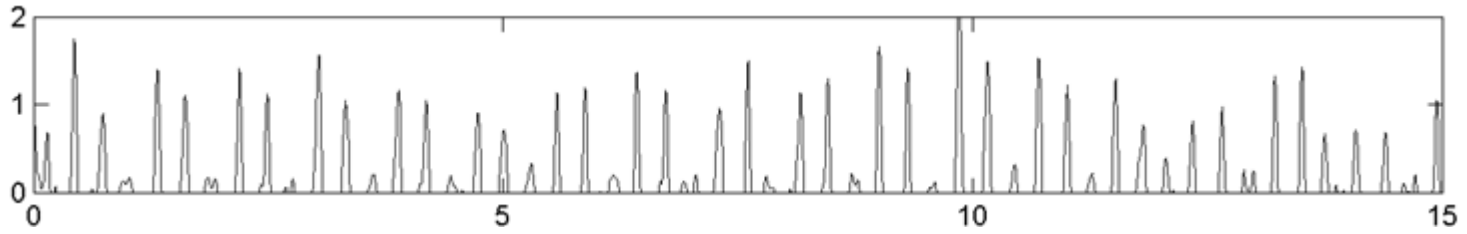


Manual onset annotations

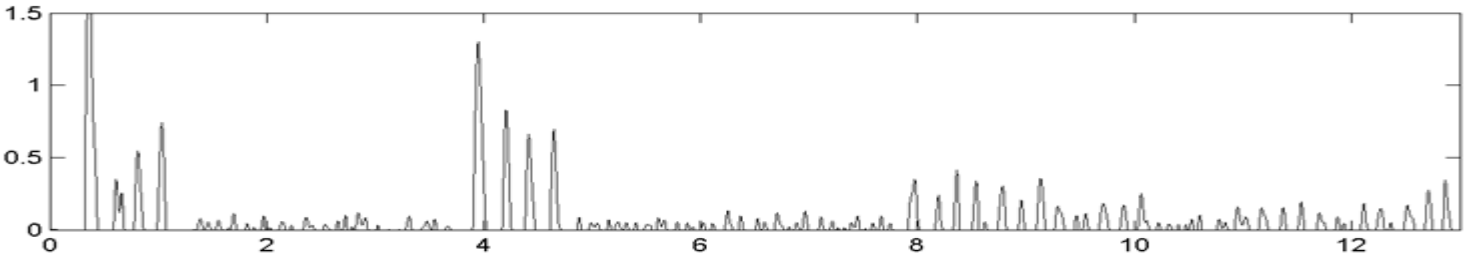


Onset Detection

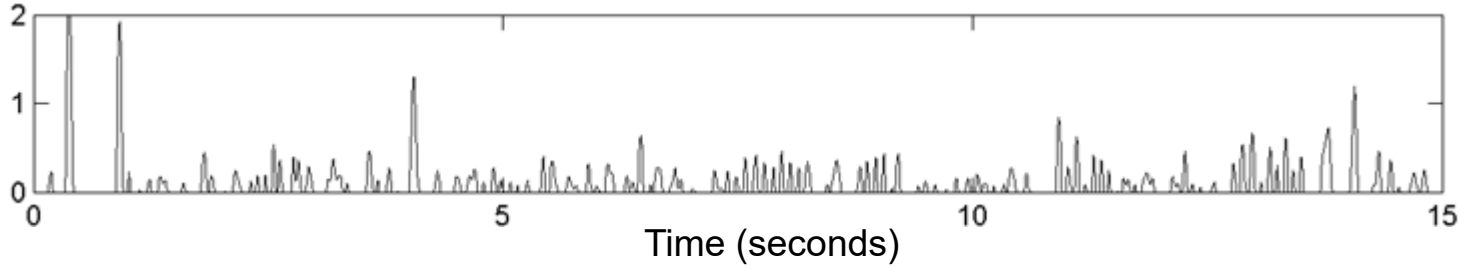
Shostakovich – 2nd Waltz



Beethoven – Fifth Symphony



Borodin – String Quartet No. 2



Onset Detection

Drumbeat 

Going Home 

Lyphard melodie 

Por una cabeza 

Donau 

Beat and Tempo

What is a beat?

- Steady pulse that drives music forward and provides the temporal framework of a piece of music
- Sequence of perceived pulses that are equally spaced in time
- The pulse a human taps along when listening to the music

[Parncutt 1994]

[Sethares 2007]

[Large/Palmer 2002]

[Lerdahl/ Jackendoff 1983]

[Fitch/ Rosenfeld 2007]

The term tempo then refers to the speed of the pulse.

Beat and Tempo

Strategy

- Analyze the novelty curve with respect to reoccurring or quasi-periodic patterns
- Avoid the explicit determination of note onsets (no peak picking)

Beat and Tempo

Strategy

- Analyze the novelty curve with respect to reoccurring or quasi-periodic patterns
- Avoid the explicit determination of note onsets (no peak picking)

[Scheirer, JASA 1998]

Methods

- Comb-filter methods
- Autocorrelation
- Fourier transfrom

[Ellis, JNMR 2007]

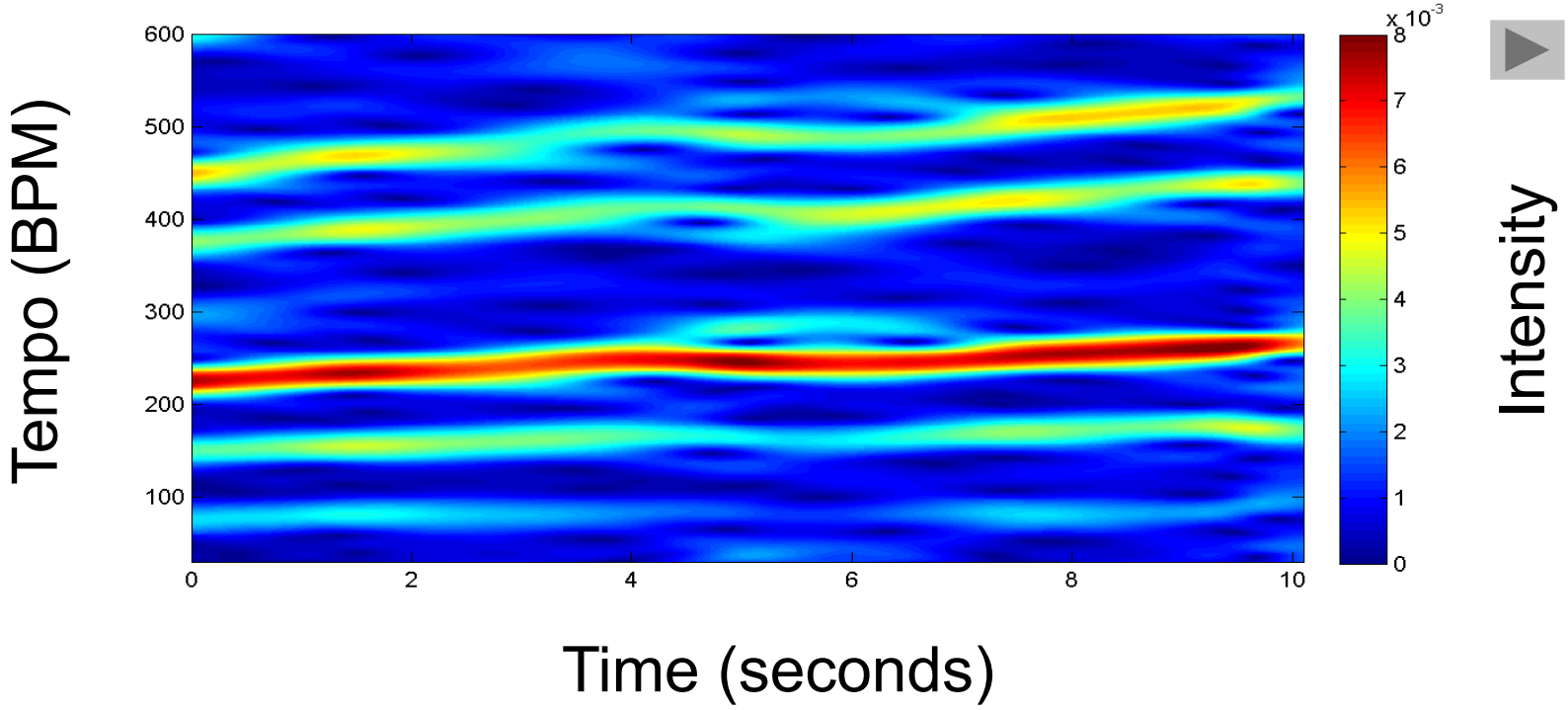
[Davies/Plumbley, IEEE-TASLP 2007]

[Peeters, JASP 2007]

[Grosche/Müller, ISMIR 2009]
[Grosche/Müller, IEEE-TASLP 2011]

Tempogram

Definition: A tempogram is a time-tempo representation that encodes the local tempo of a music signal over time.



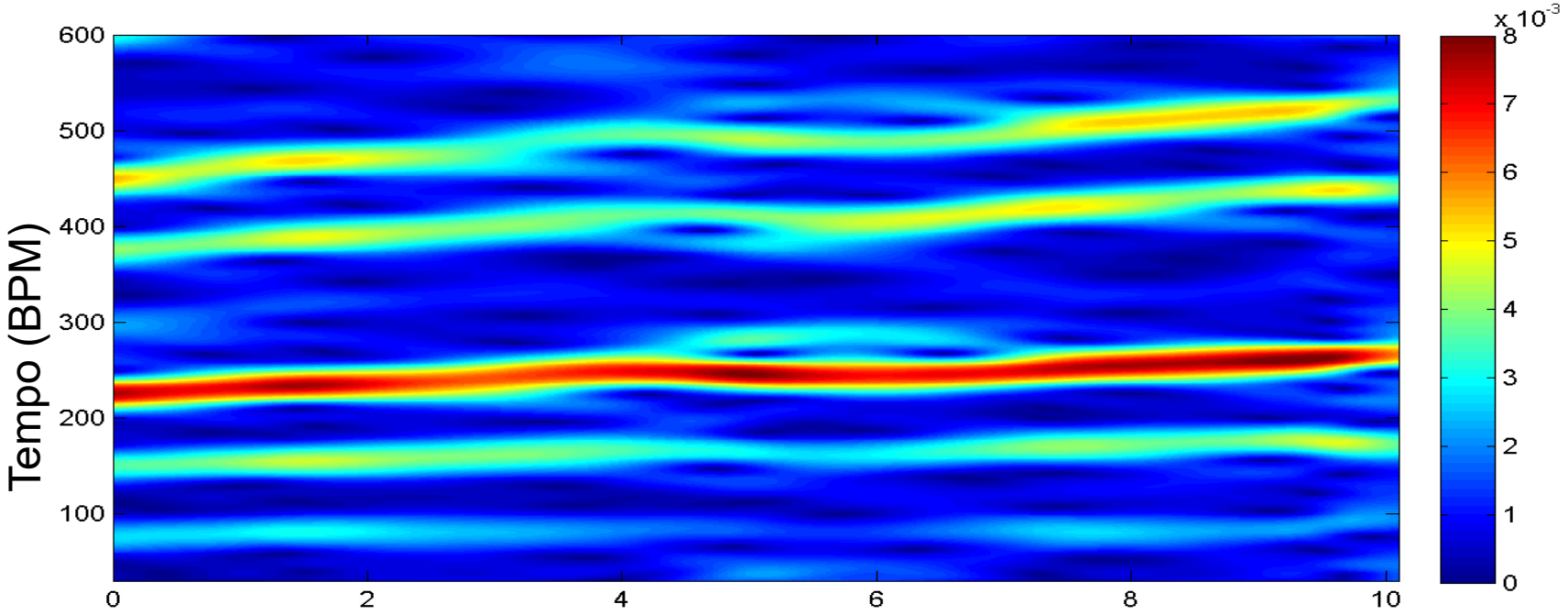
Tempogram (Fourier)

Definition: A tempogram is a time-tempo represenation that encodes the local tempo of a music signal over time.

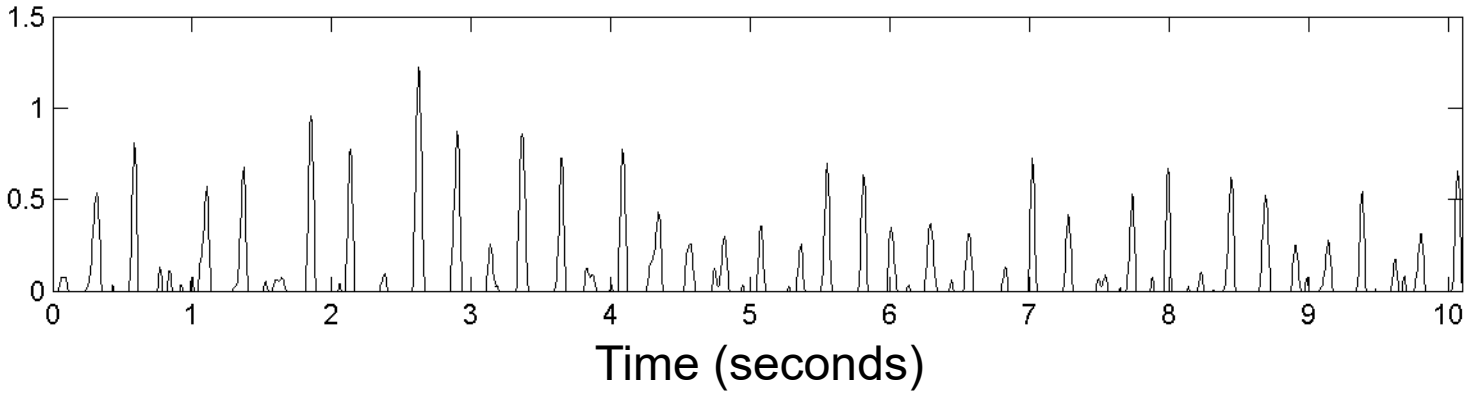
Fourier-based method

- Compute a spectrogram (STFT) of the novelty curve
- Convert frequency axis (given in Hertz) into tempo axis (given in BPM)
- Magnitude spectrogram indicates local tempo

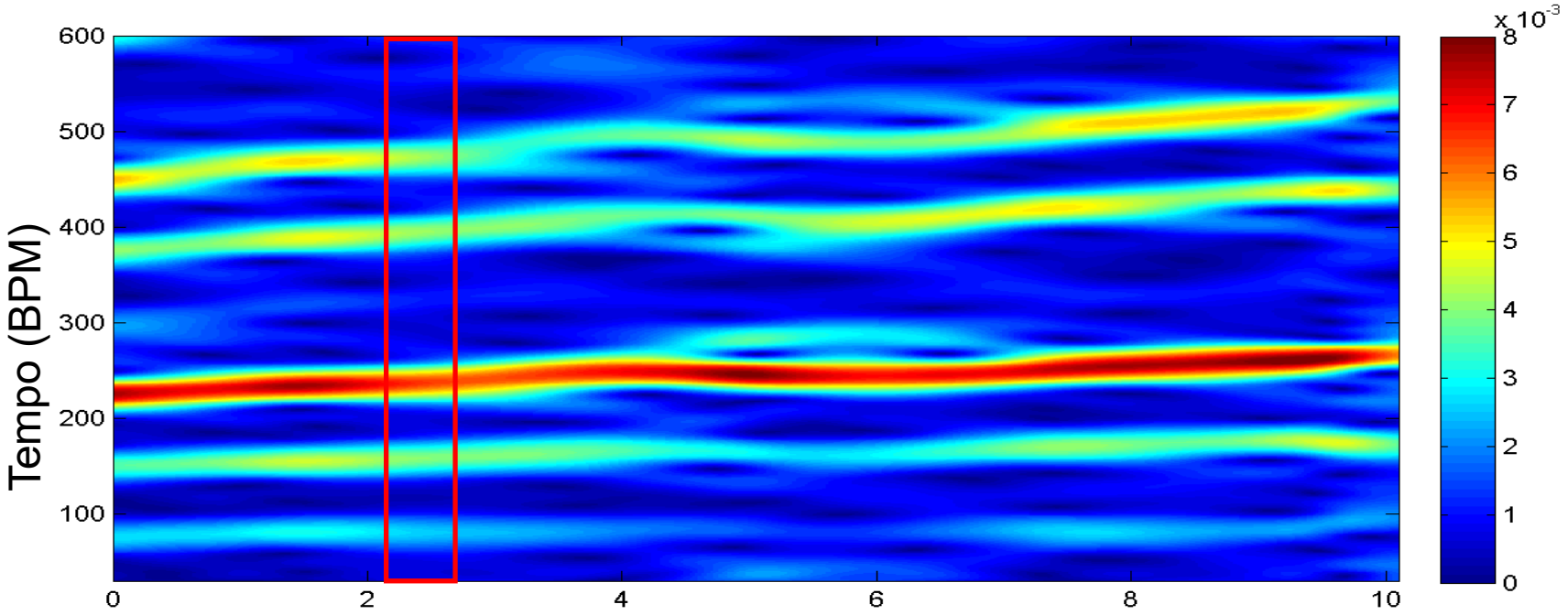
Tempogram (Fourier)



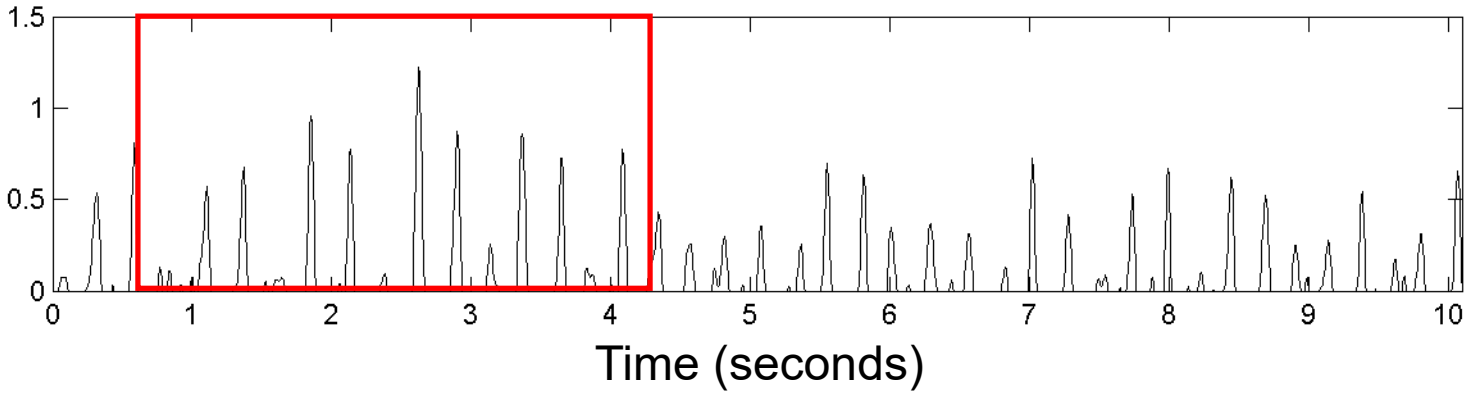
Novelty curve



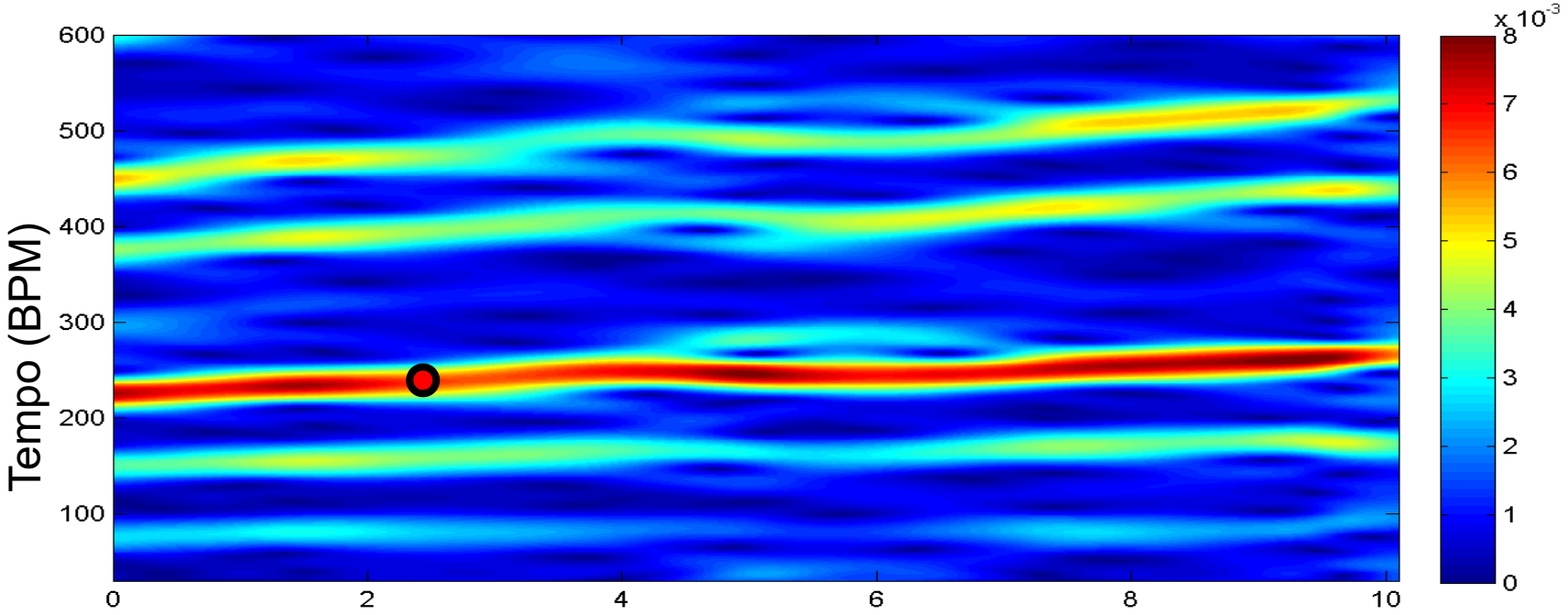
Tempogram (Fourier)



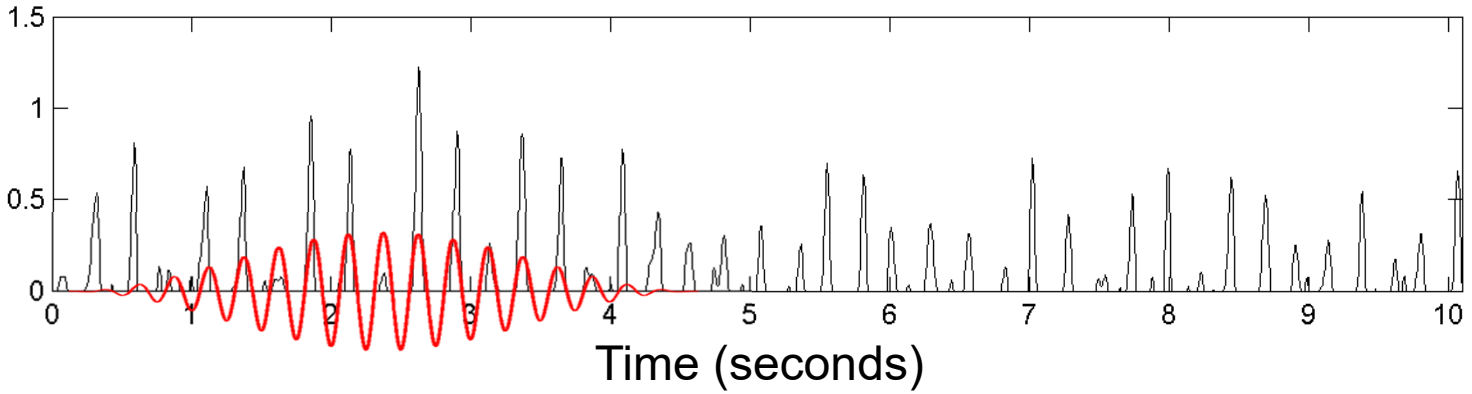
Novelty curve (local section)



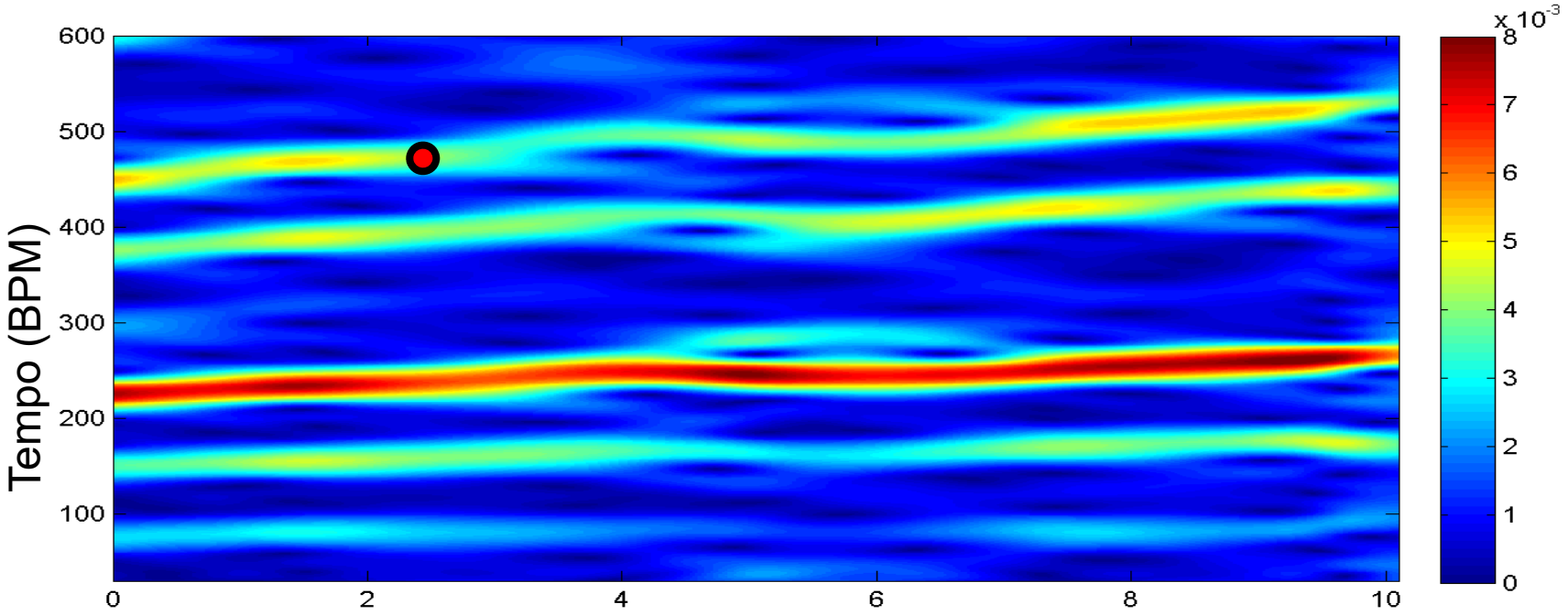
Tempogram (Fourier)



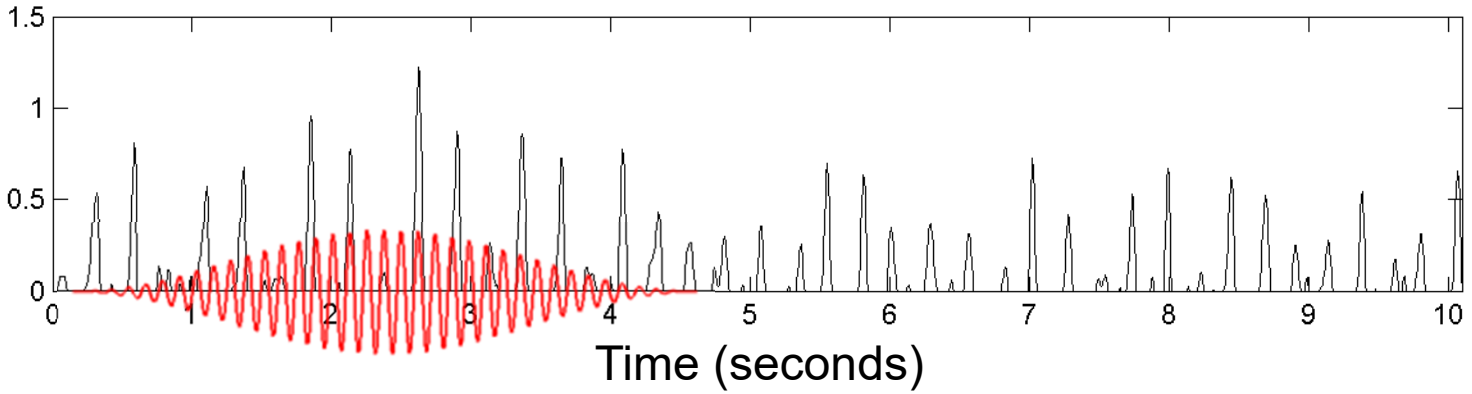
Windowed sinusoidal



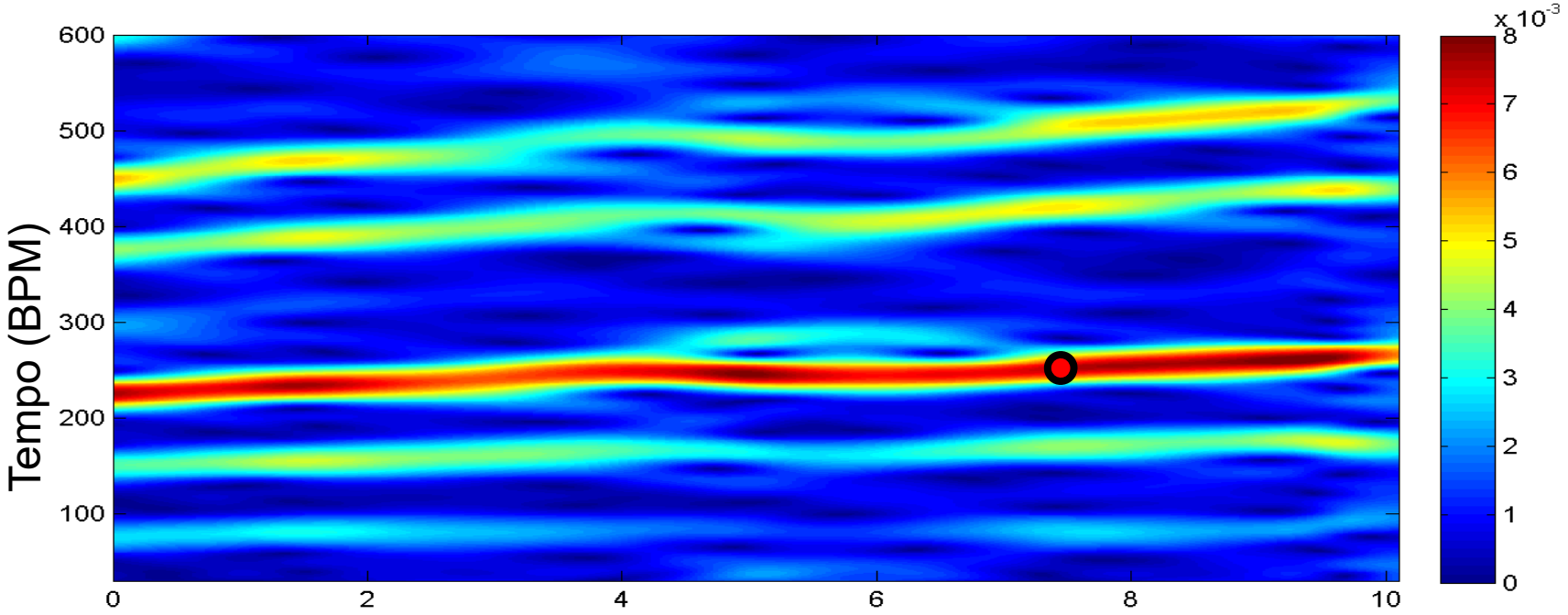
Tempogram (Fourier)



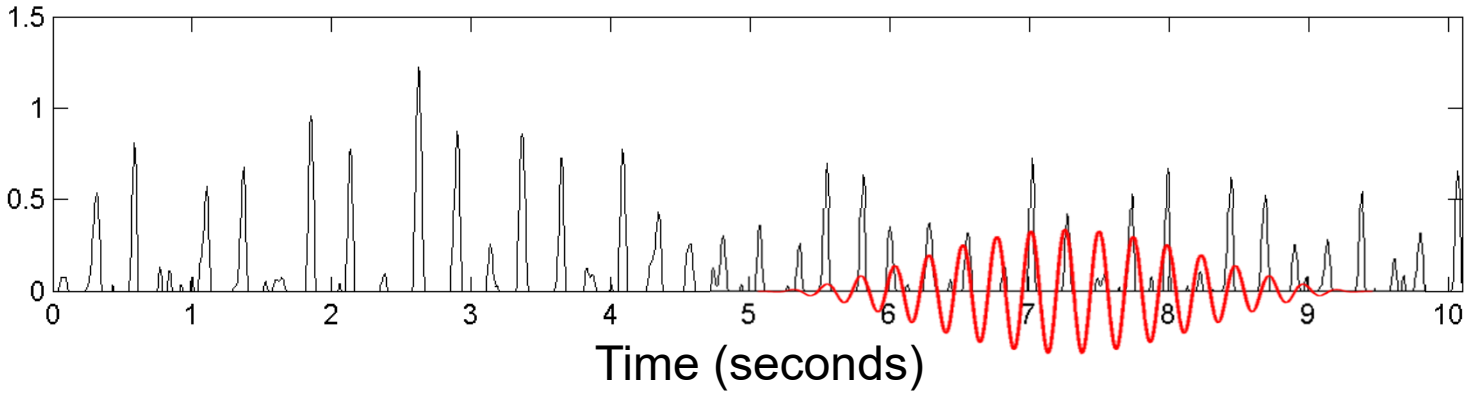
Windowed sinusoidal



Tempogram (Fourier)



Windowed sinusoidal



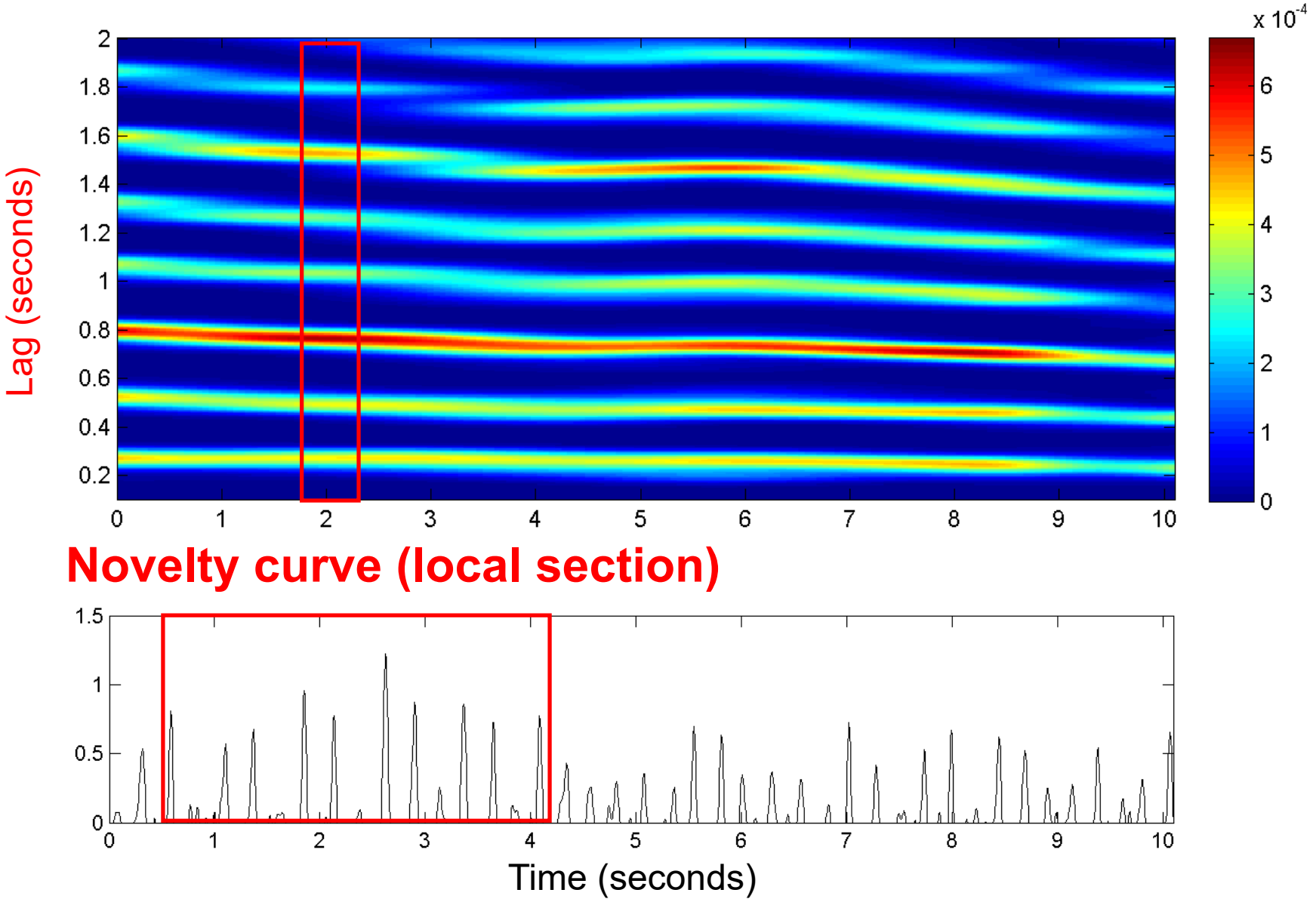
Tempogram (Autocorrelation)

Definition: A tempogram is a time-tempo represenation that encodes the local tempo of a music signal over time.

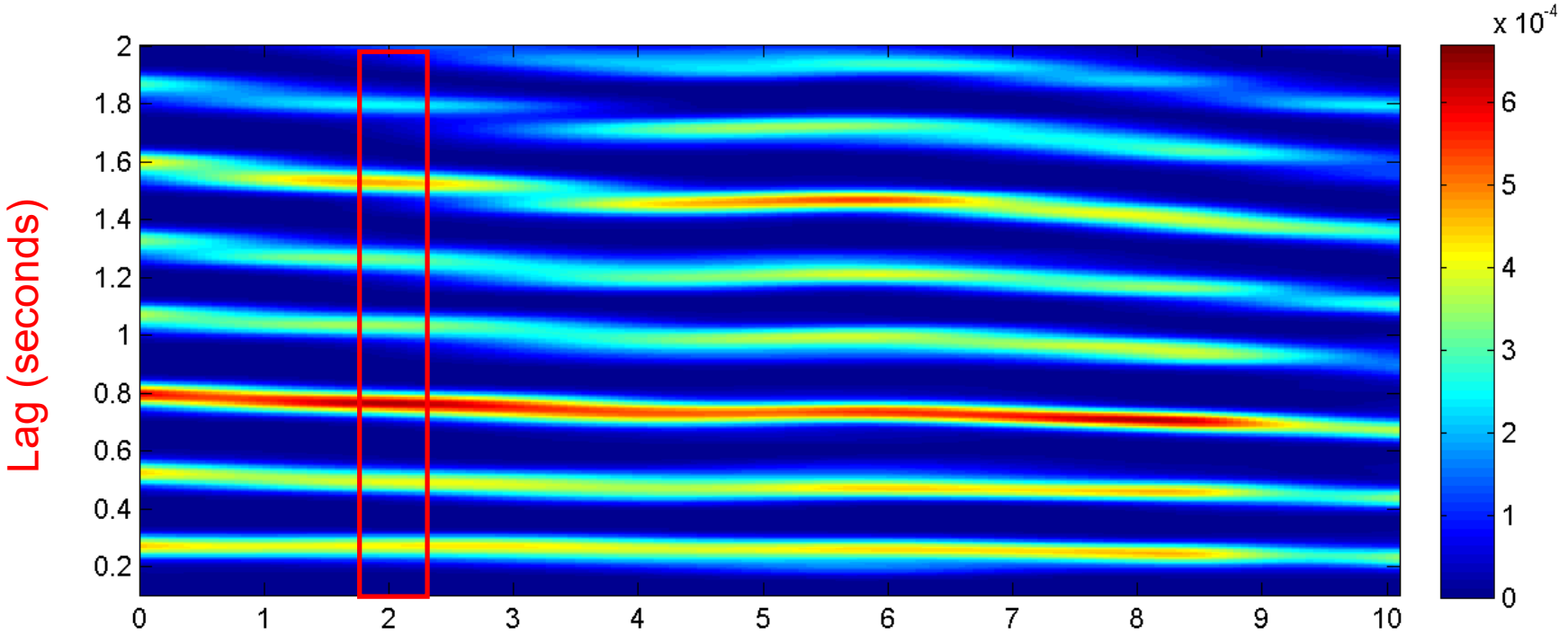
Autocorrelation-based method

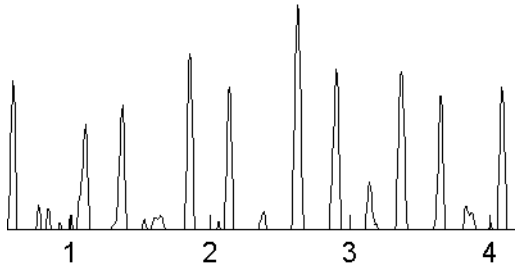
- Compare novelty curve with time-lagged local sections of itself
- Convert lag-axis (given in seconds) into tempo axis (given in BPM)
- Autocorrelogram indicates local tempo

Tempogram (Autocorrelation)

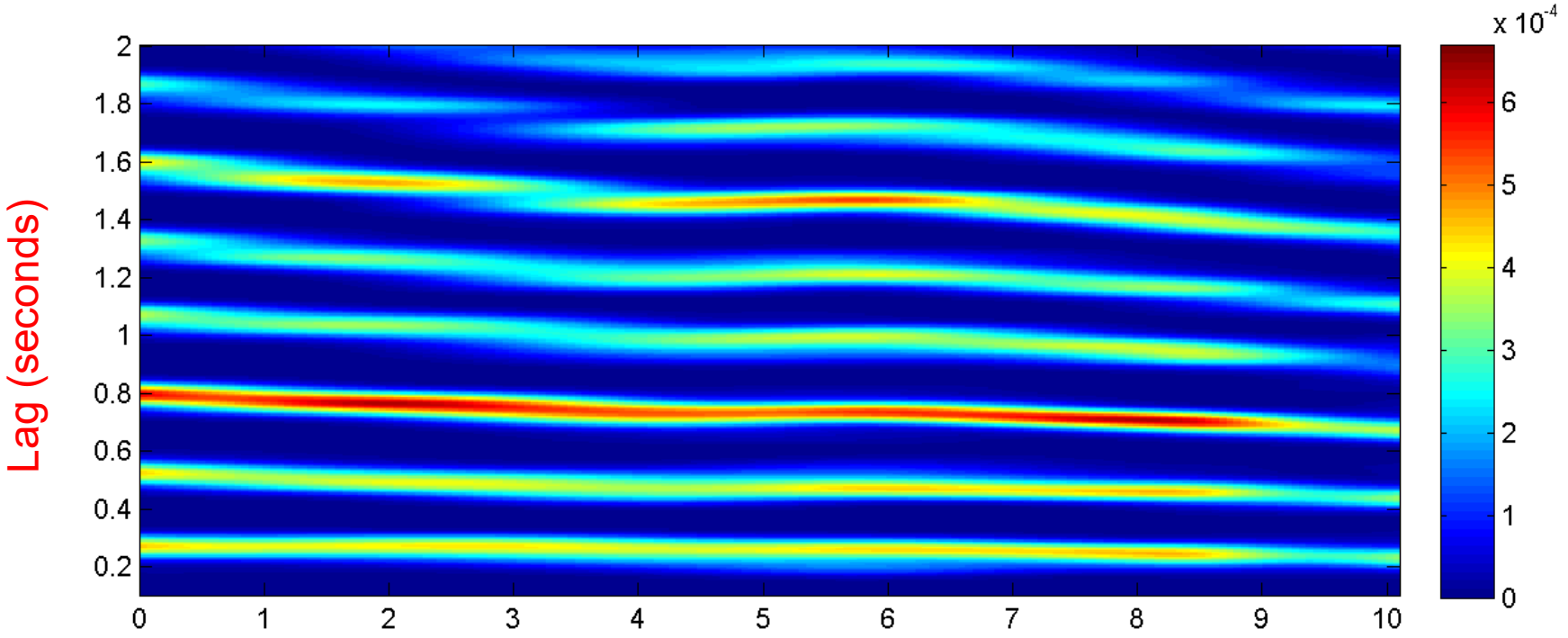


Tempogram (Autocorrelation)

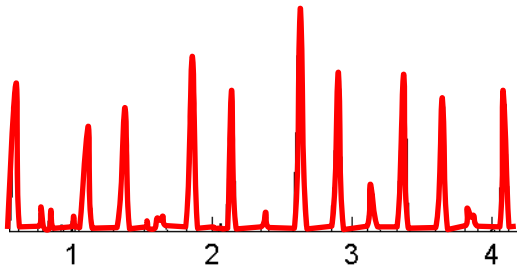




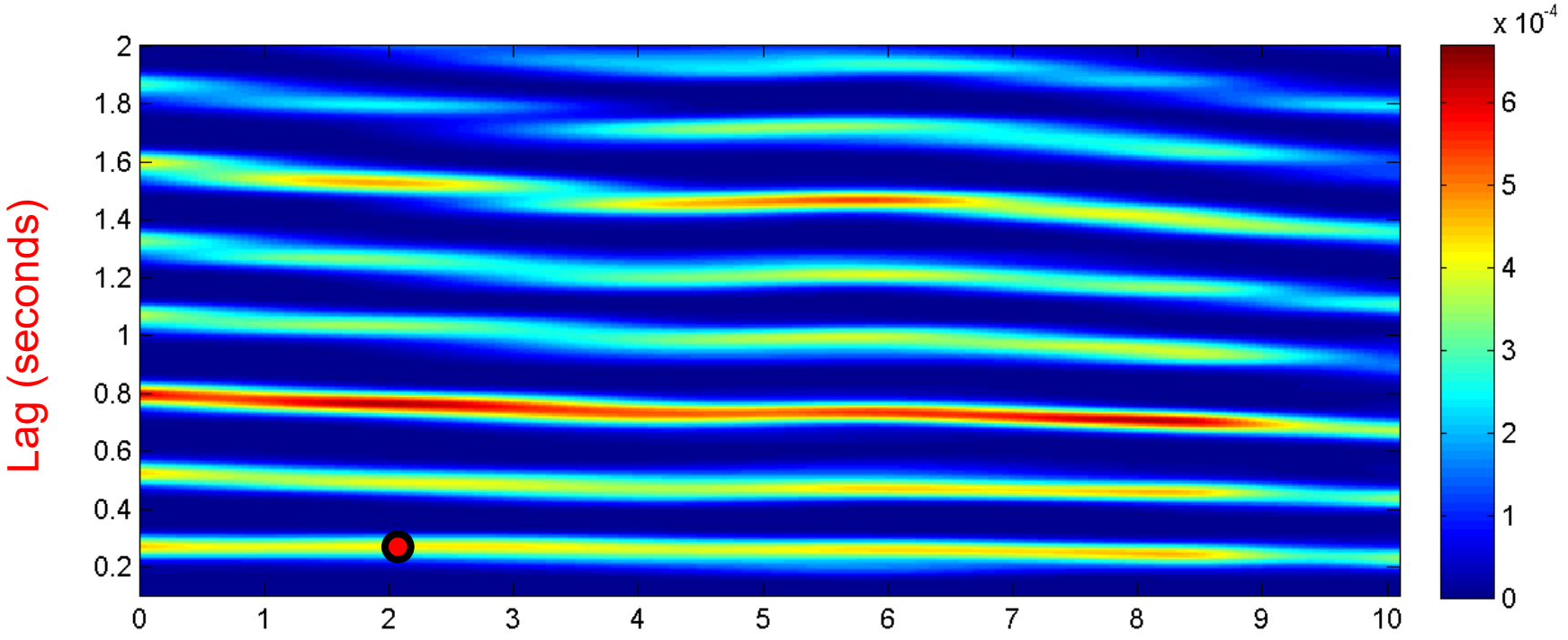
Tempogram (Autocorrelation)



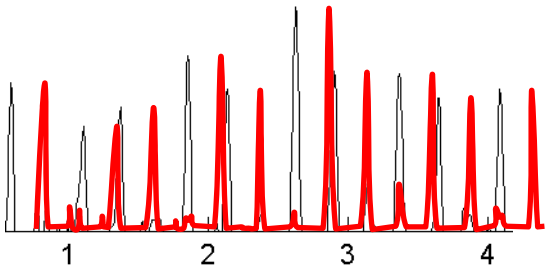
Lag = 0 (seconds)



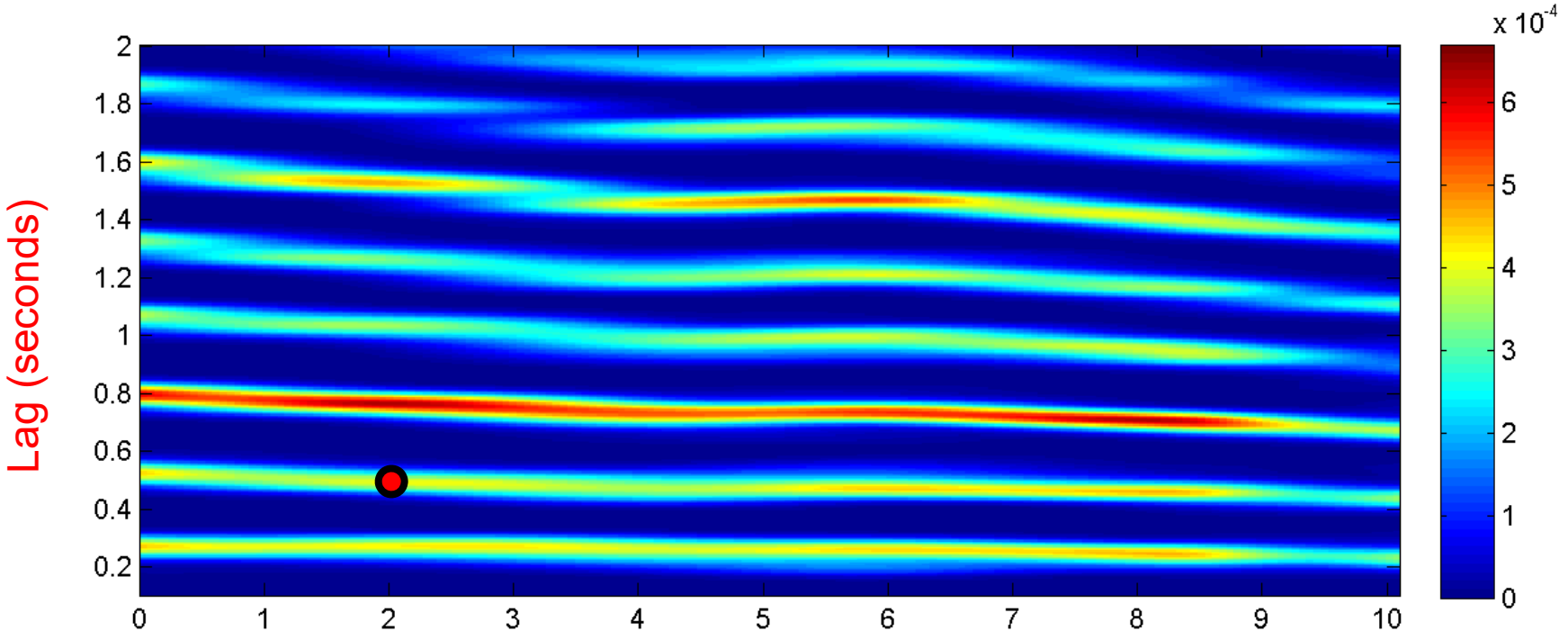
Tempogram (Autocorrelation)



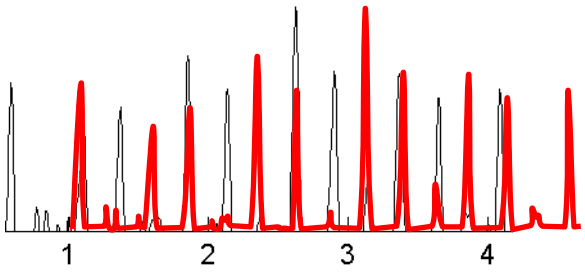
Lag = 0.26 (seconds)



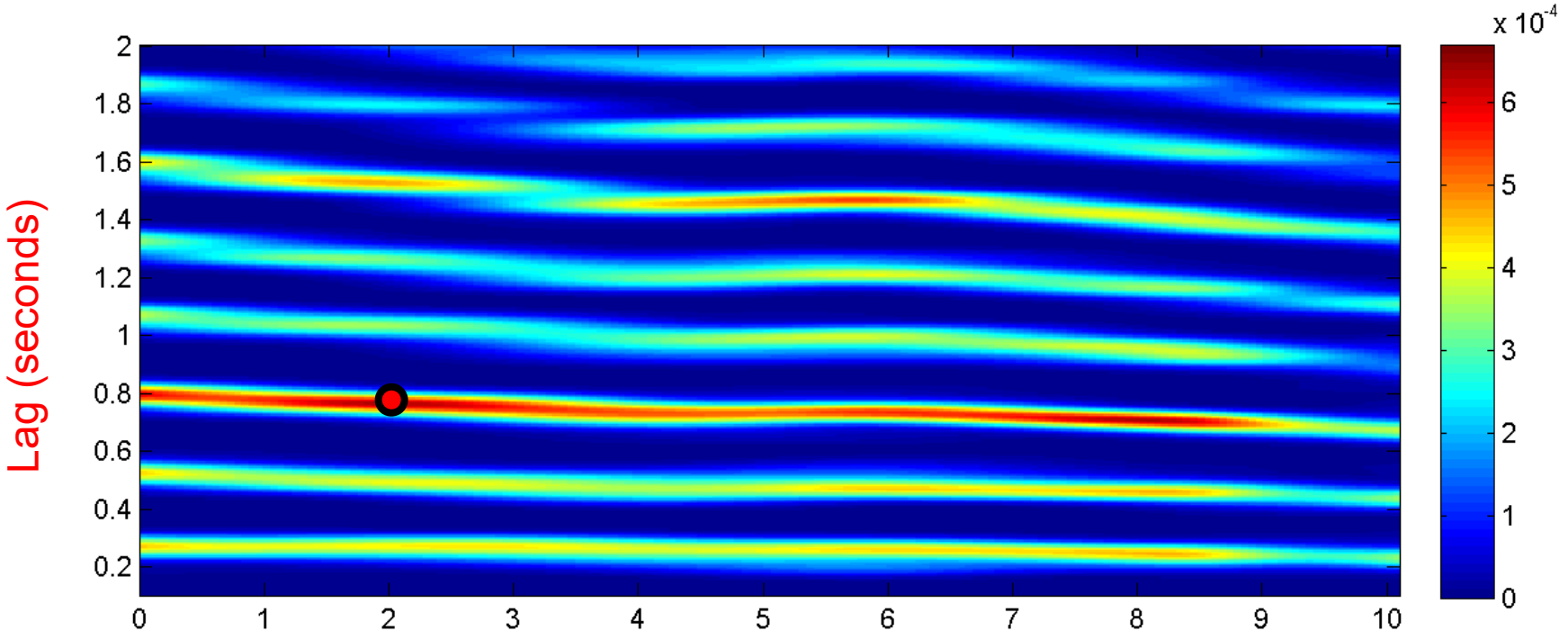
Tempogram (Autocorrelation)



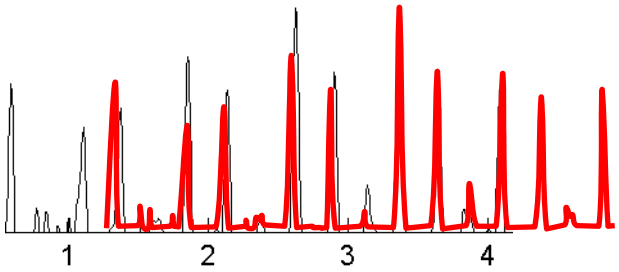
Lag = 0.52 (seconds)



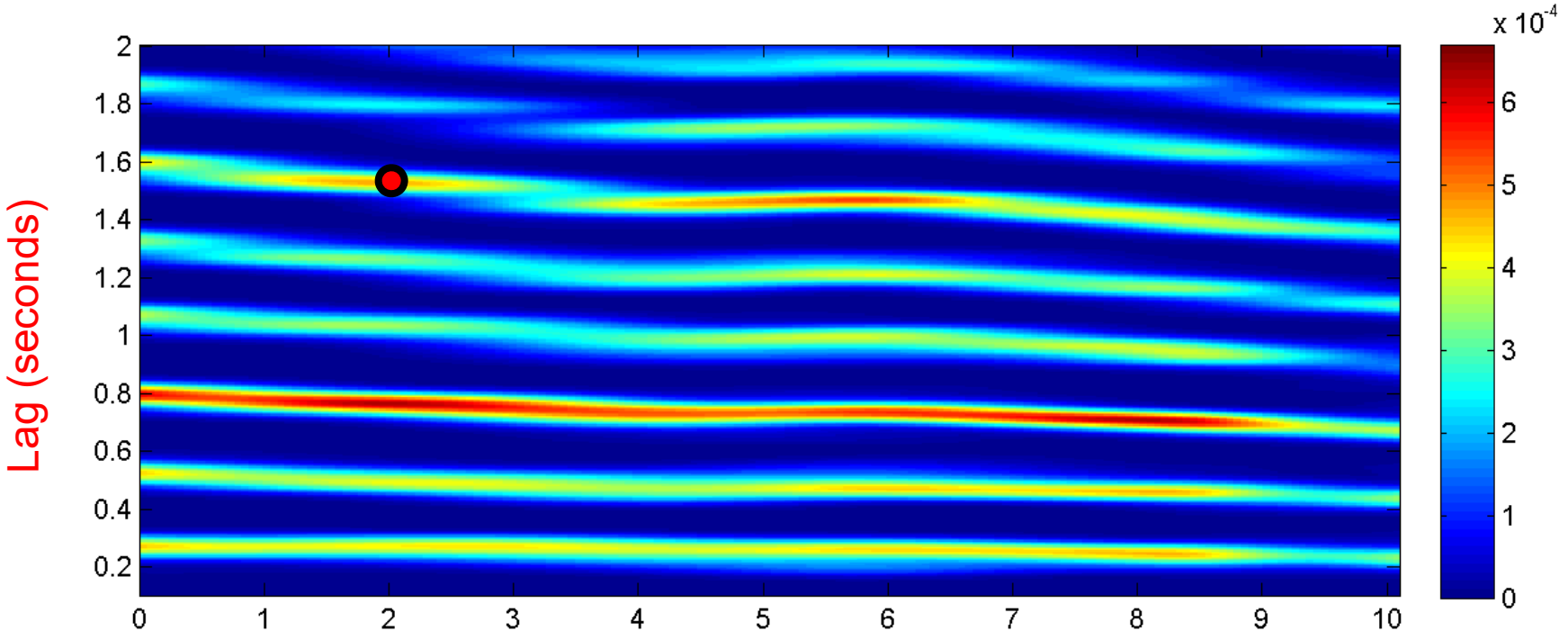
Tempogram (Autocorrelation)



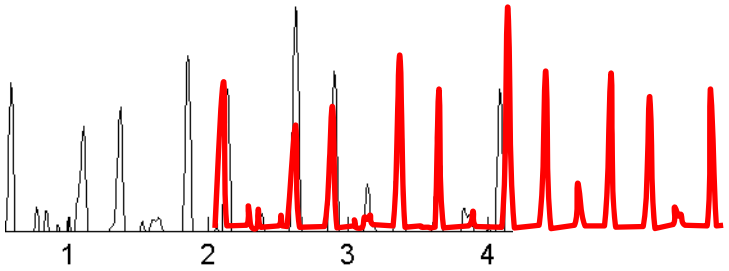
Lag = 0.78 (seconds)



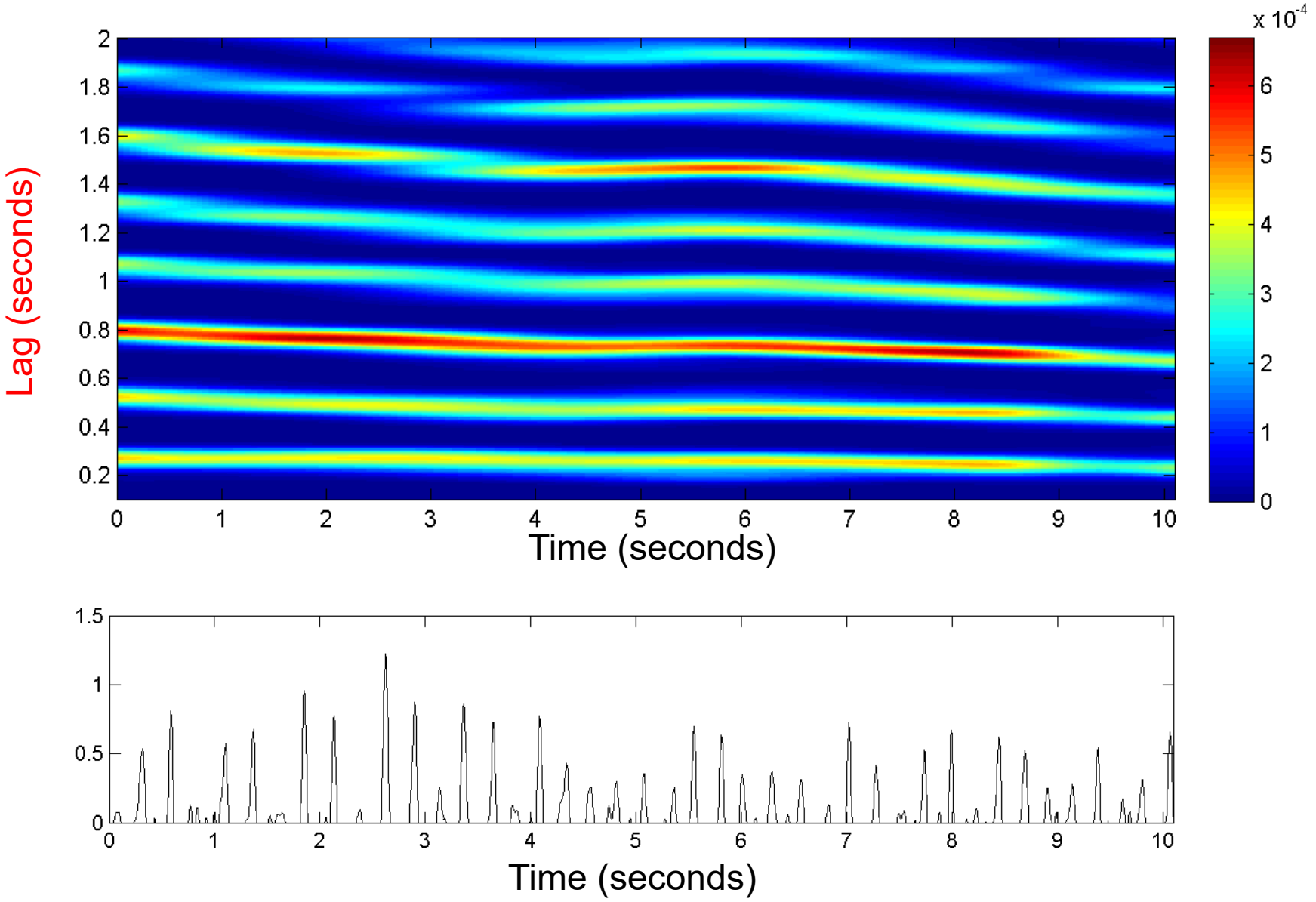
Tempogram (Autocorrelation)



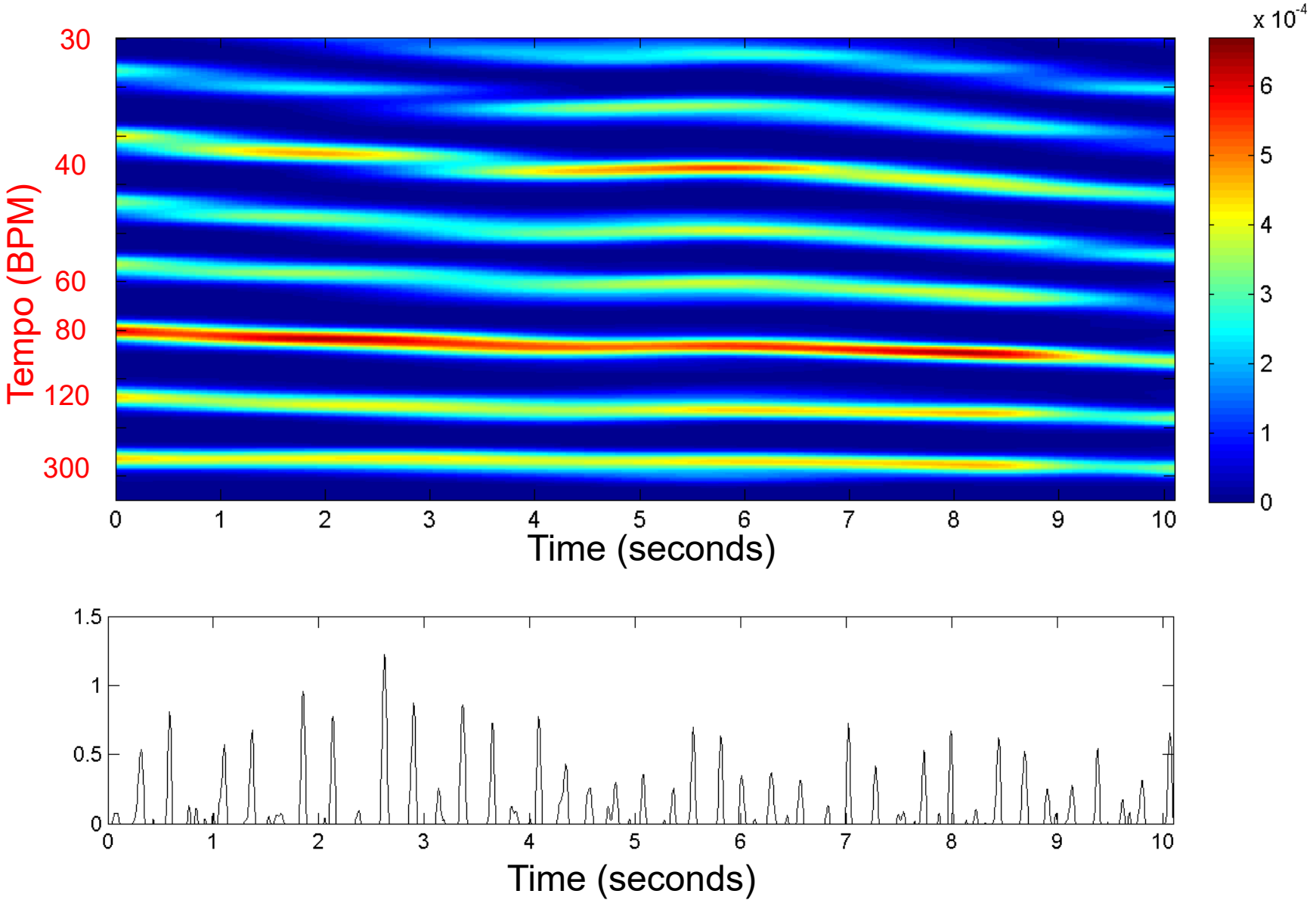
Lag = 1.56 (seconds)



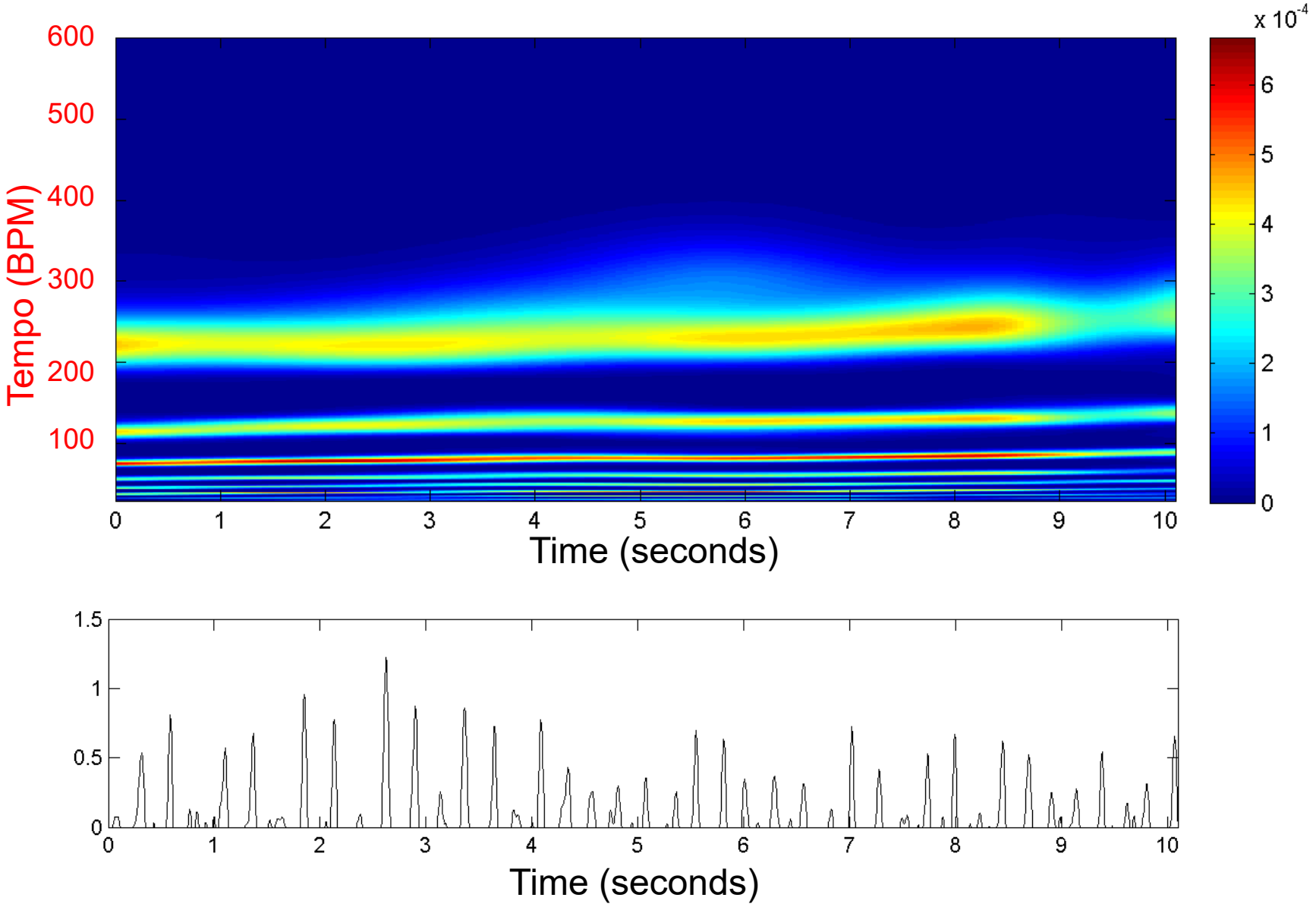
Tempogram (Autocorrelation)



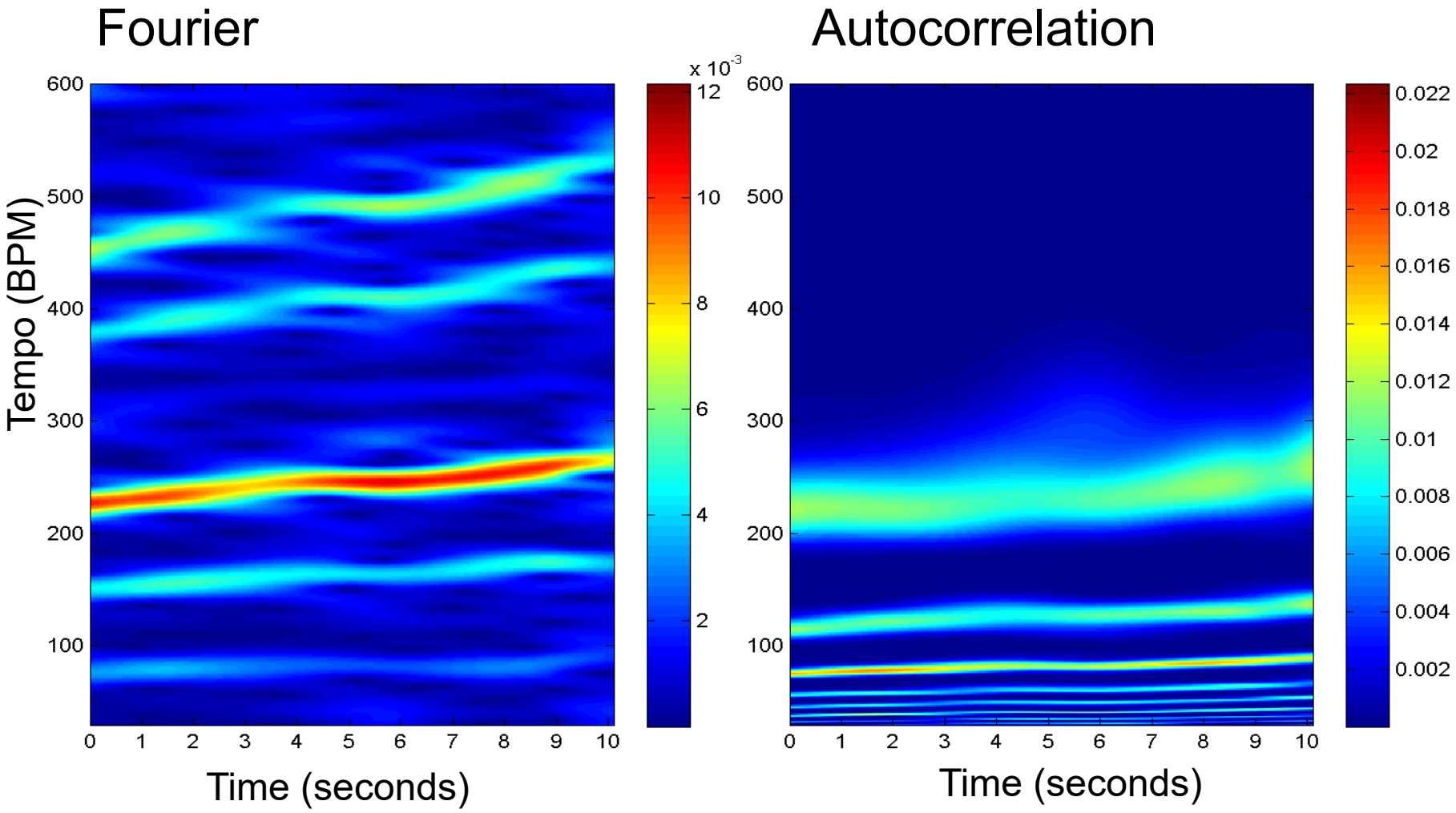
Tempogram (Autocorrelation)



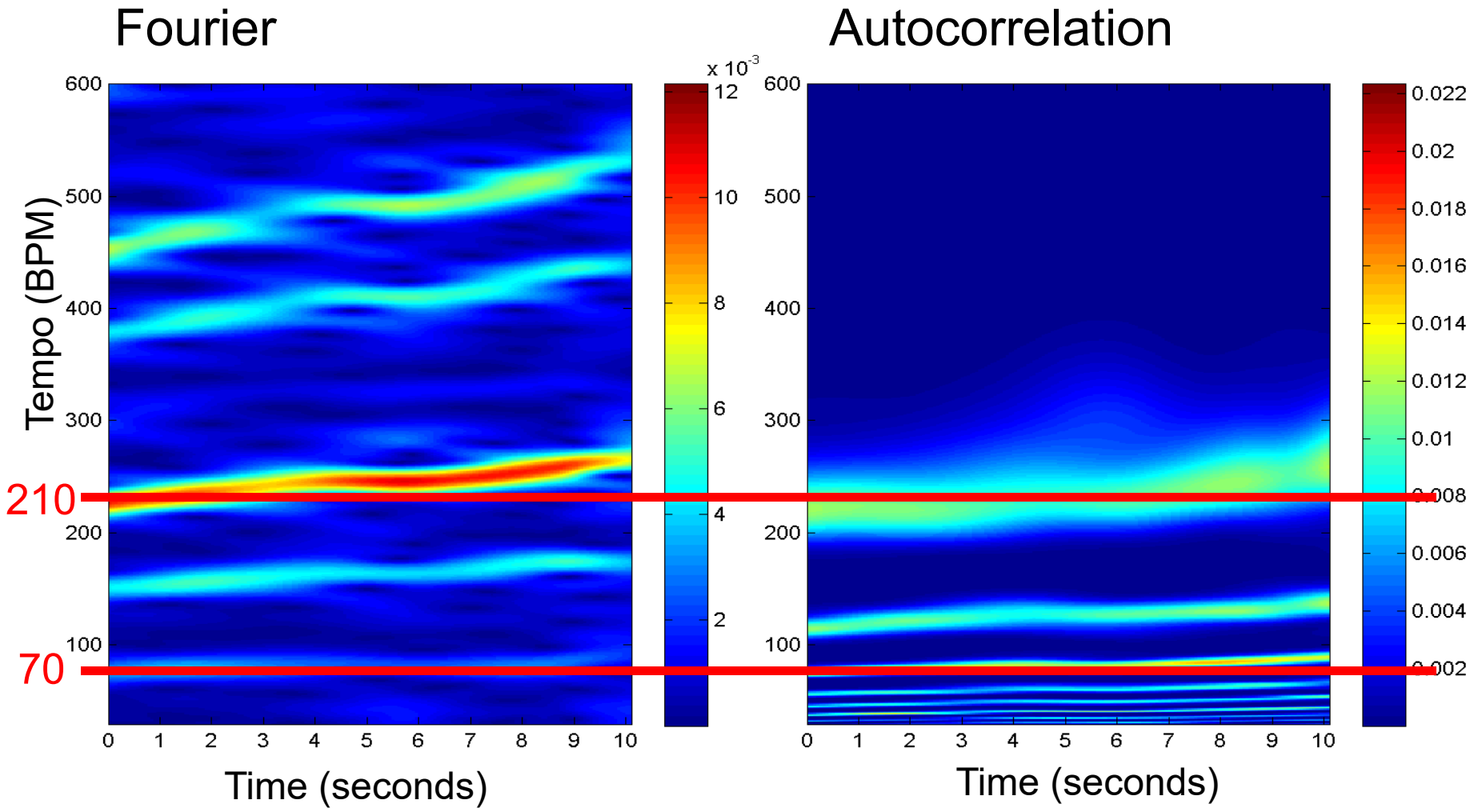
Tempogram (Autocorrelation)



Tempogram


Fourier
Autocorrelation
Tempo (BPM)
Time (seconds)
Time (seconds)
x 10^-3
600
500
400
300
200
100
0 1 2 3 4 5 6 7 8 9 10
12
10
8
6
4
2
0.022
0.02
0.018
0.016
0.014
0.012
0.01
0.008
0.006
0.004
0.002

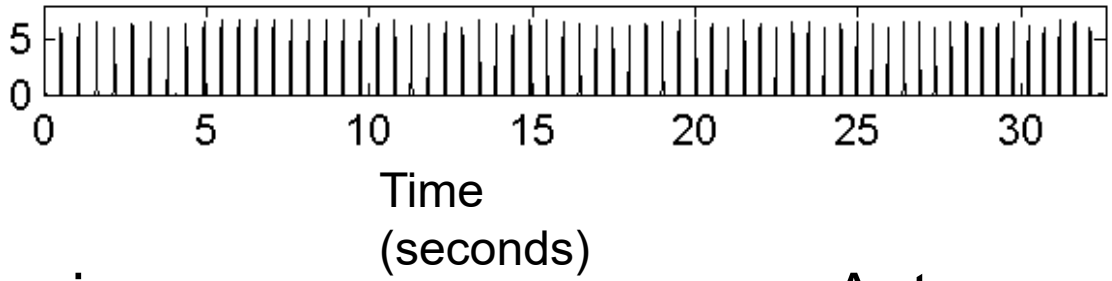
Tempogram



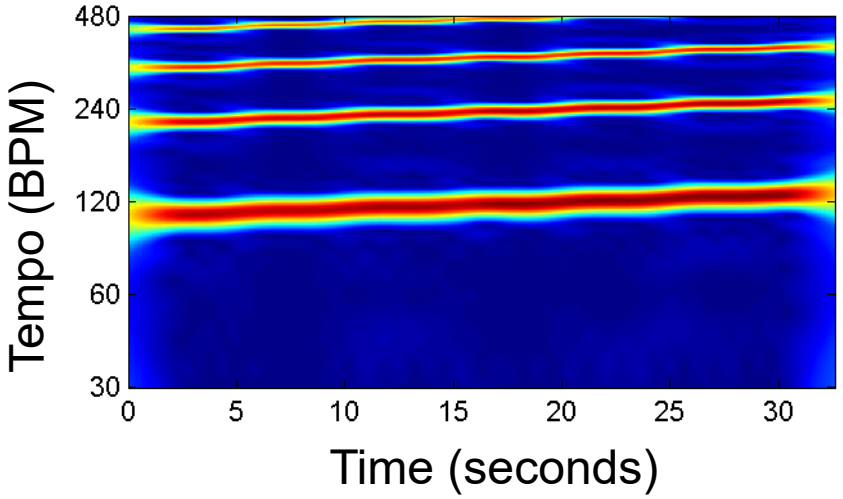
Tempo@Tatum = 210 BPM

Tempo@Measure = 70 BPM

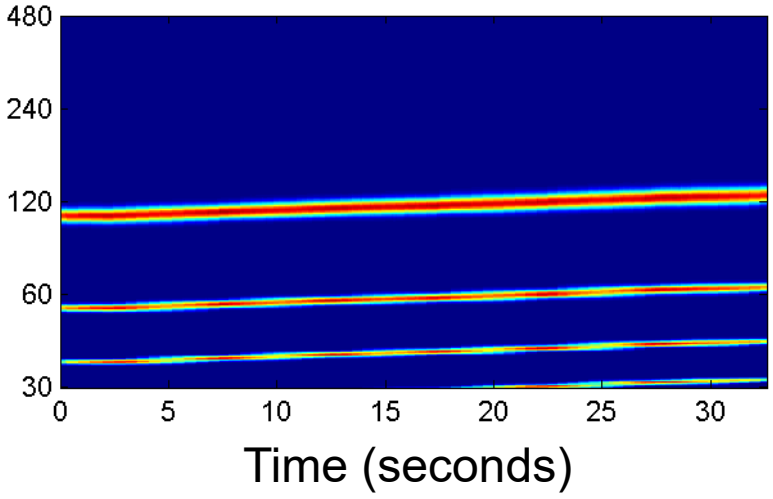
Tempogram



Fourier



Autocorrelation



Emphasis of tempo harmonics (integer multiples)

Emphasis of tempo subharmonics (integer fractions)

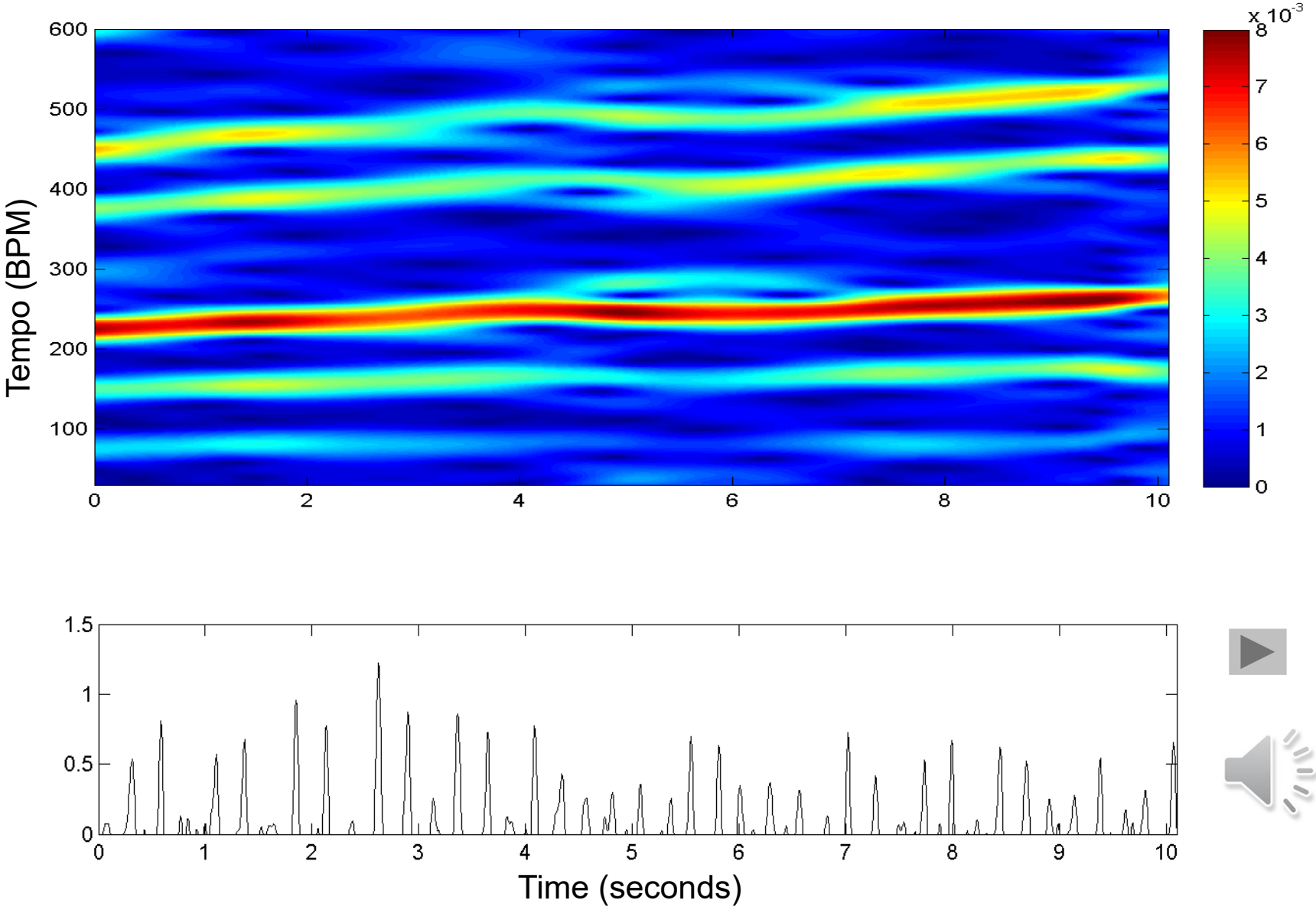
Tempogram (Summary)

Fourier	Autocorrelation
Novelty curve is compared with sinusoidal kernels each representing a specific tempo	Novelty curve is compared with time-lagged local (windowed) sections of itself
Convert frequency (Hertz) into tempo (BPM)	Convert time-lag (seconds) into tempo (BPM)
Reveals novelty periodicities	Reveals novelty self-similarities
Emphasizes harmonics	Emphasizes subharmonics
Suitable to analyze tempo on tatum and tactus level	Suitable to analyze tempo on tactus and measure level

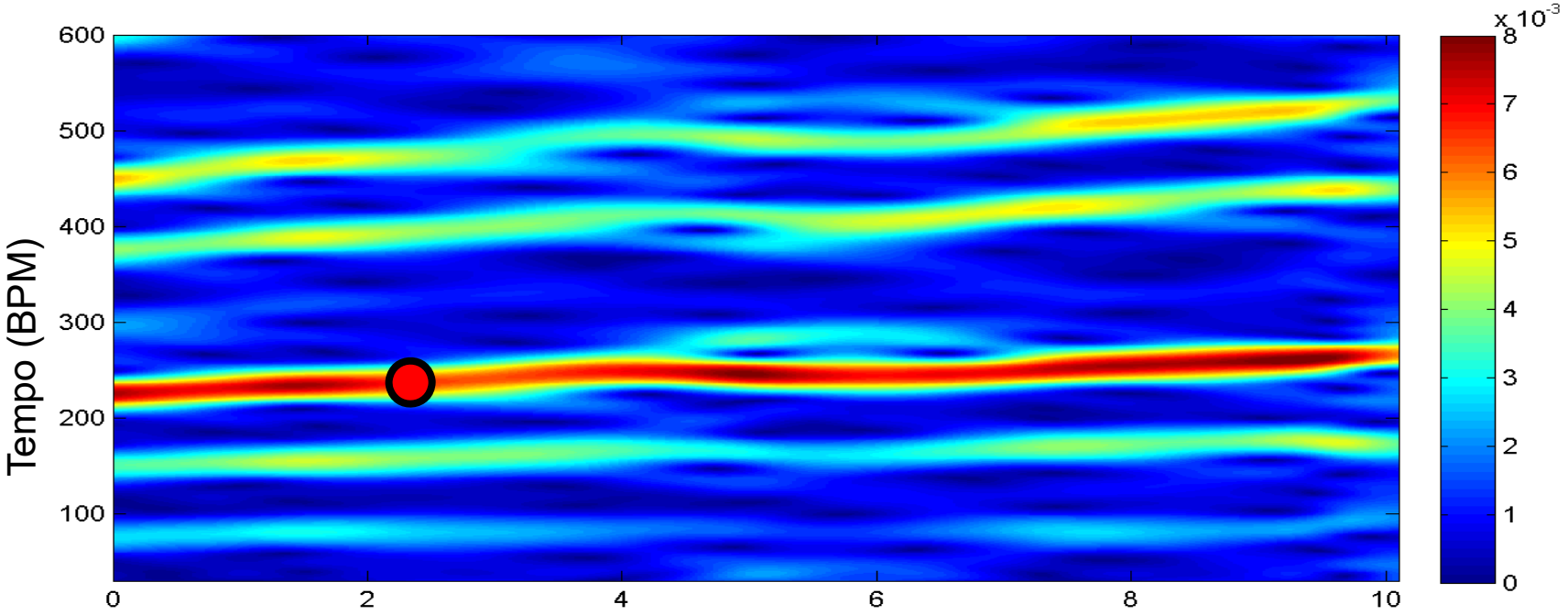
Beat Tracking

- Given the tempo, find the best sequence of beats
- Complex Fourier tempogram contains magnitude and phase information
- The magnitude encodes how well the novelty curve resonates with a sinusoidal kernel of a specific tempo
- The phase optimally aligns the sinusoidal kernel with the peaks of the novelty curve

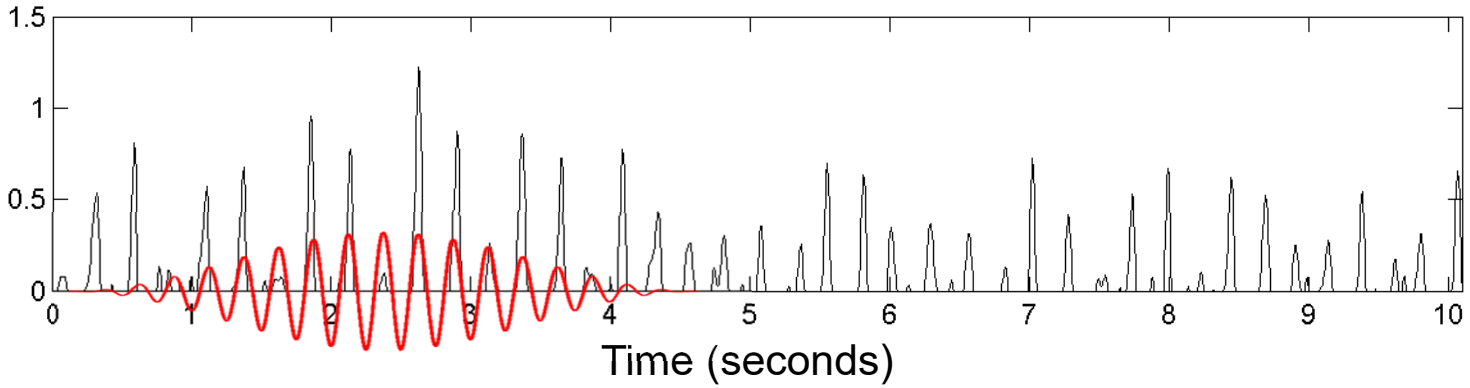
Local Pulse Tracking



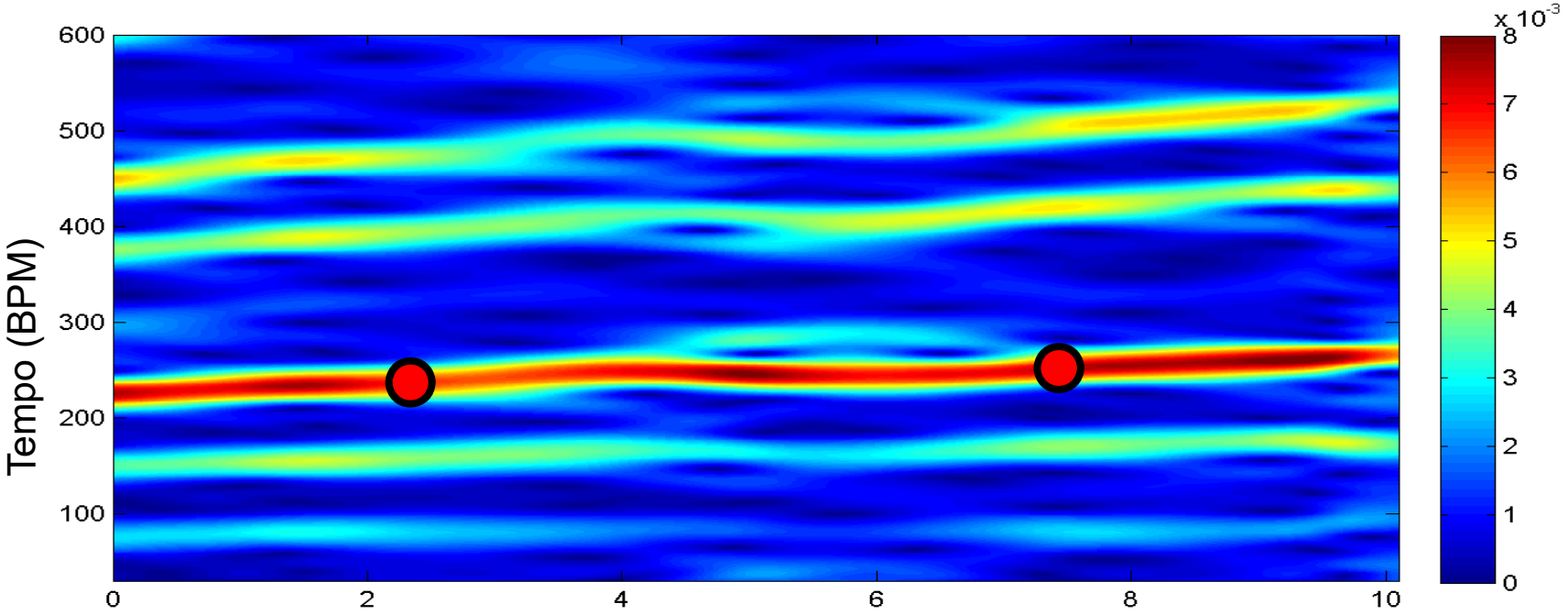
Local Pulse Tracking



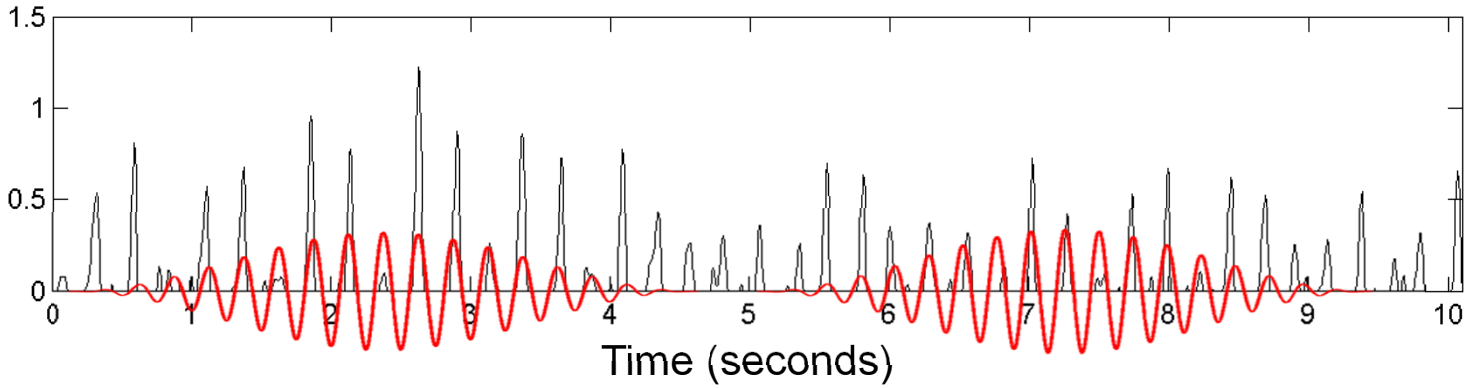
Optimizing local periodicity kernel



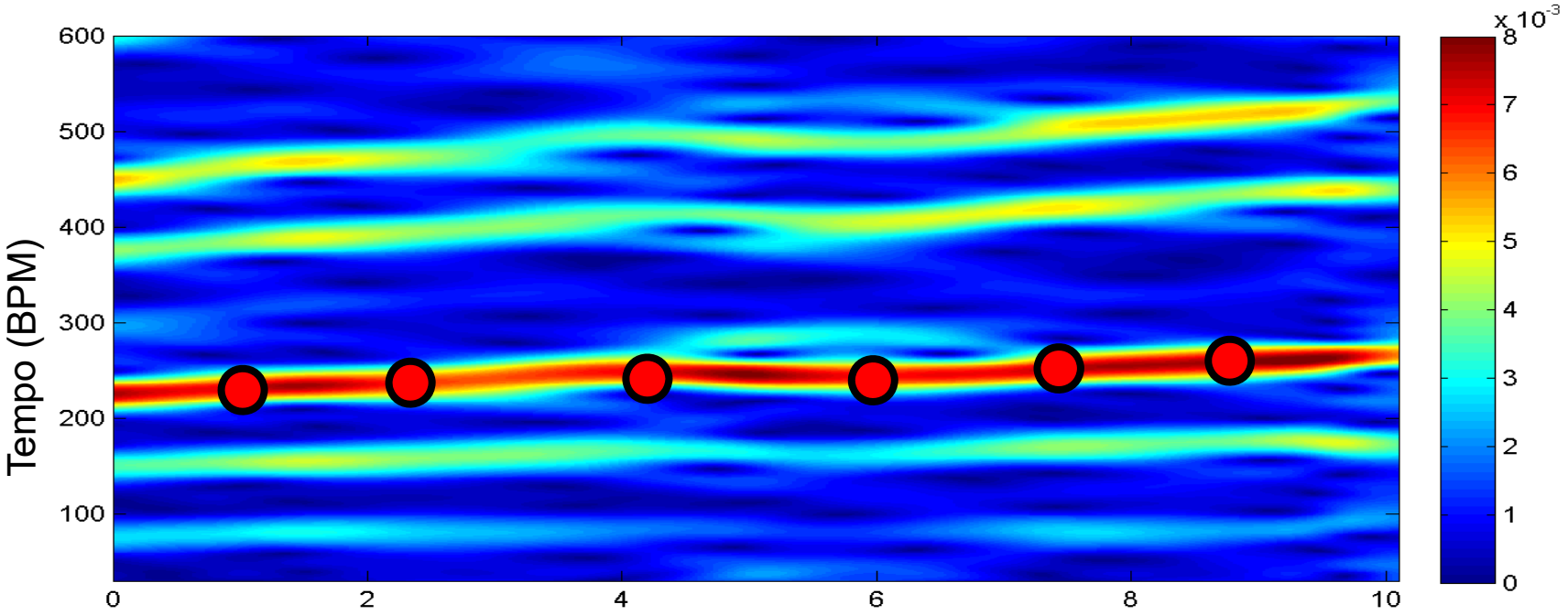
Local Pulse Tracking



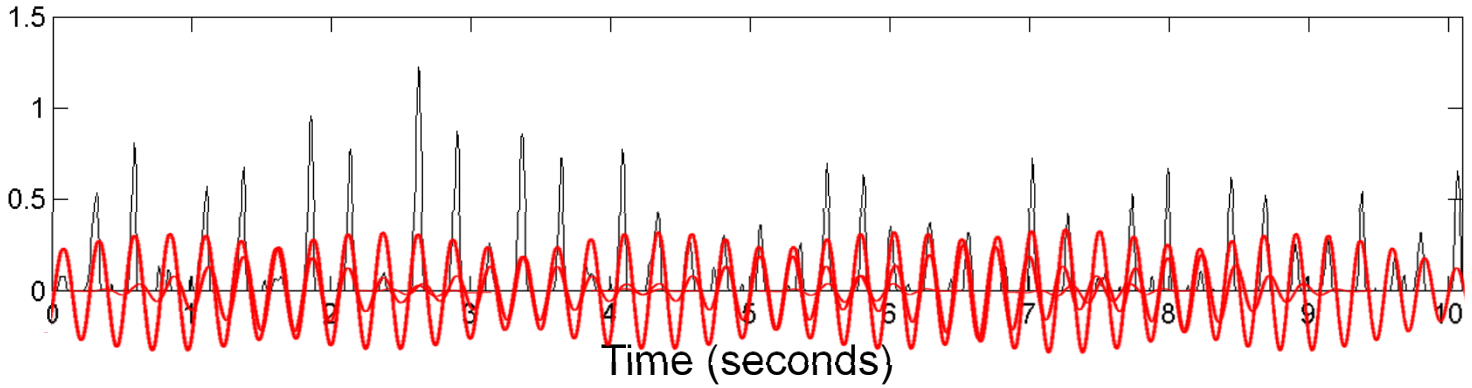
Optimizing local periodicity kernel



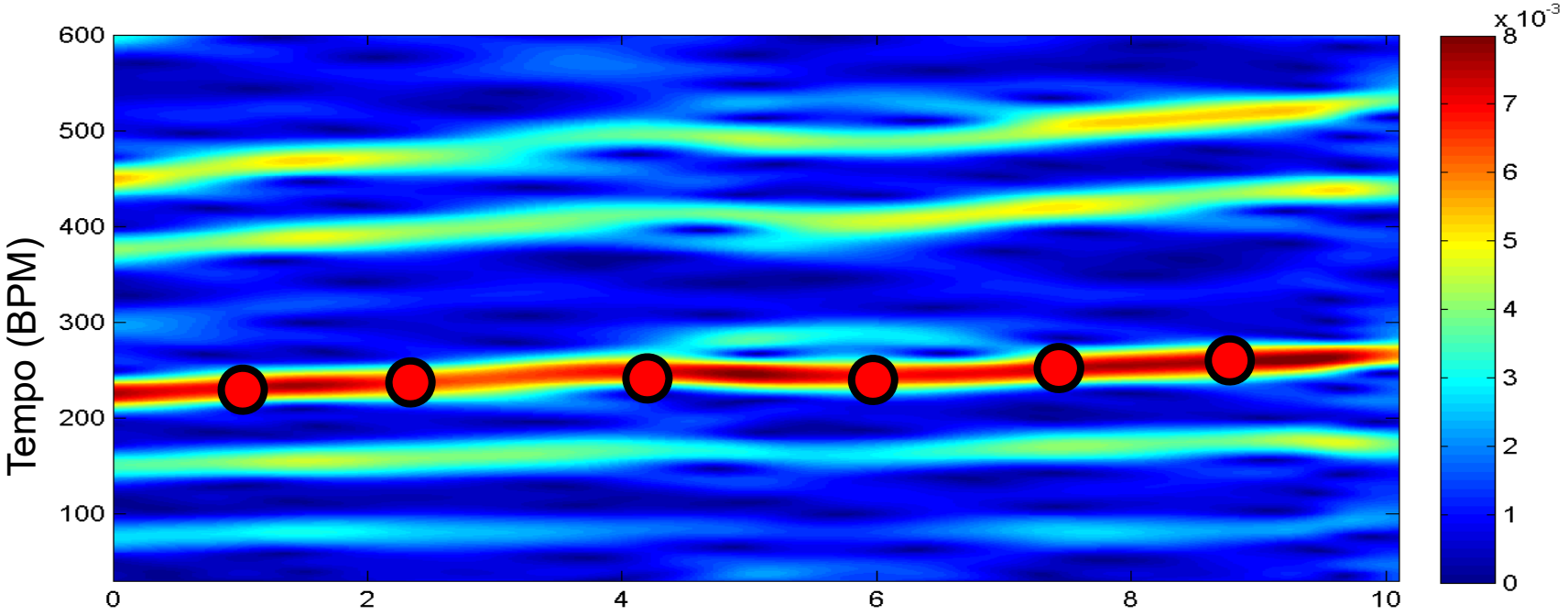
Local Pulse Tracking



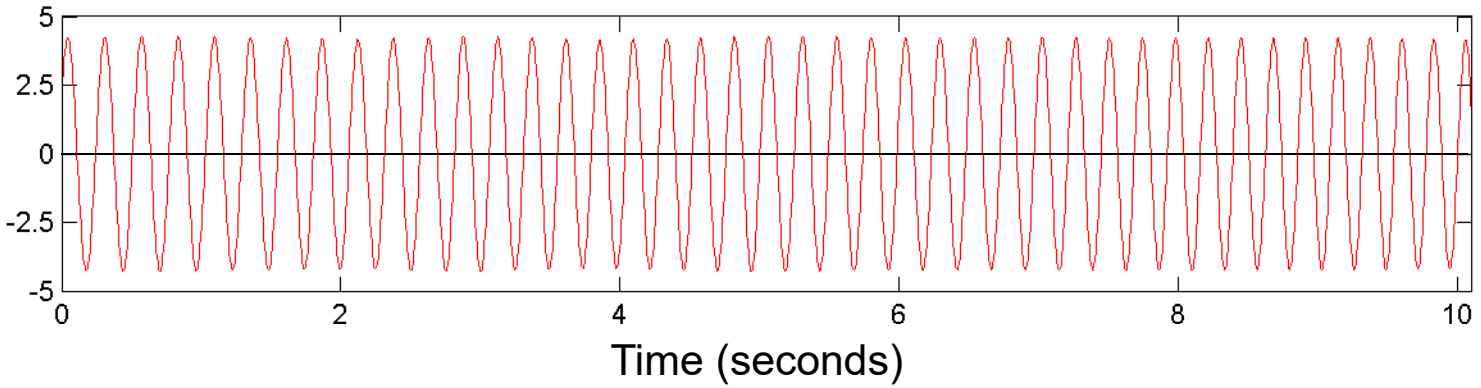
Optimizing local periodicity kernel



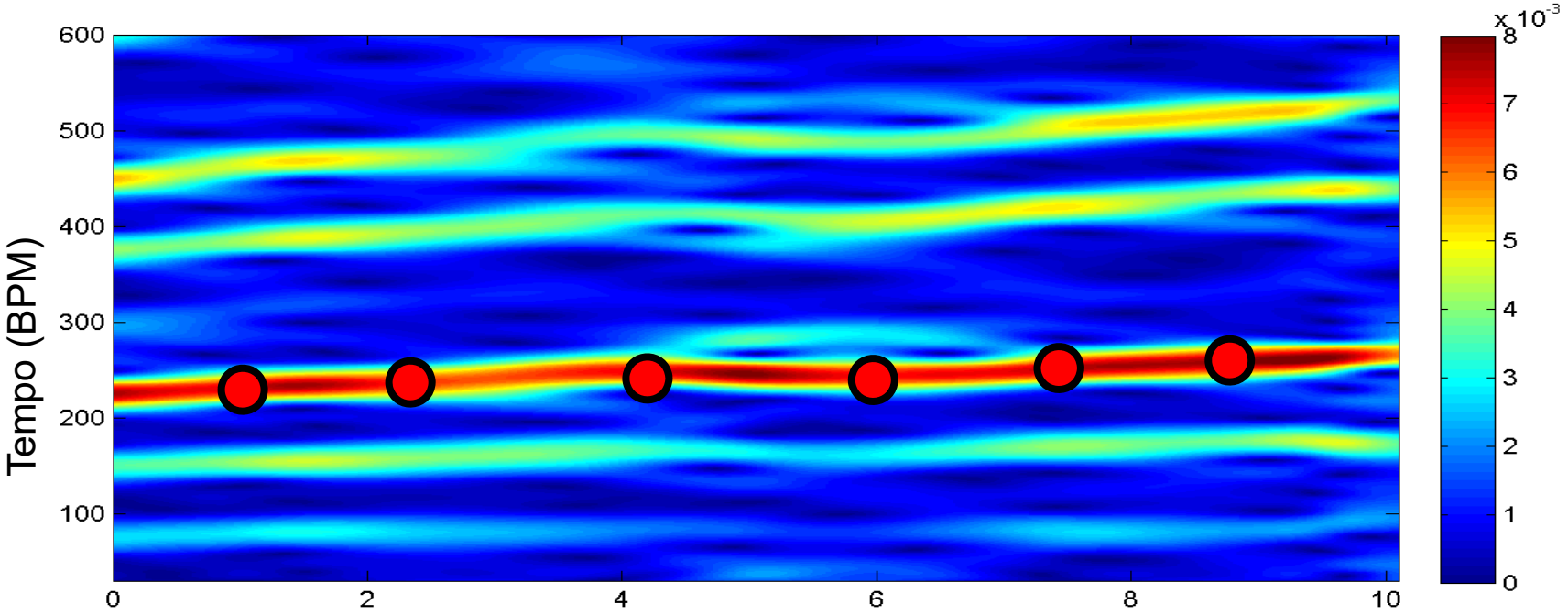
Local Pulse Tracking



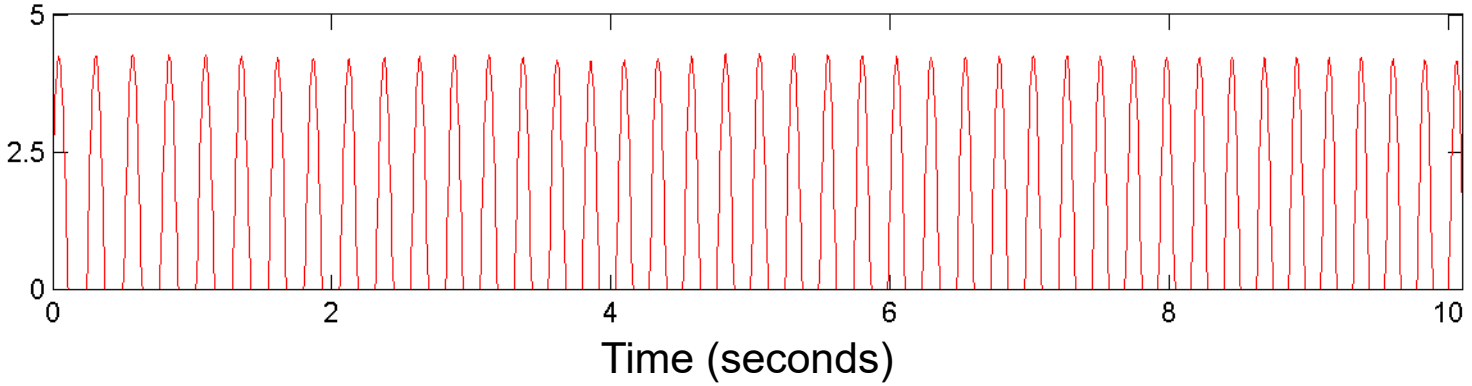
Accumulation of kernels



Local Pulse Tracking

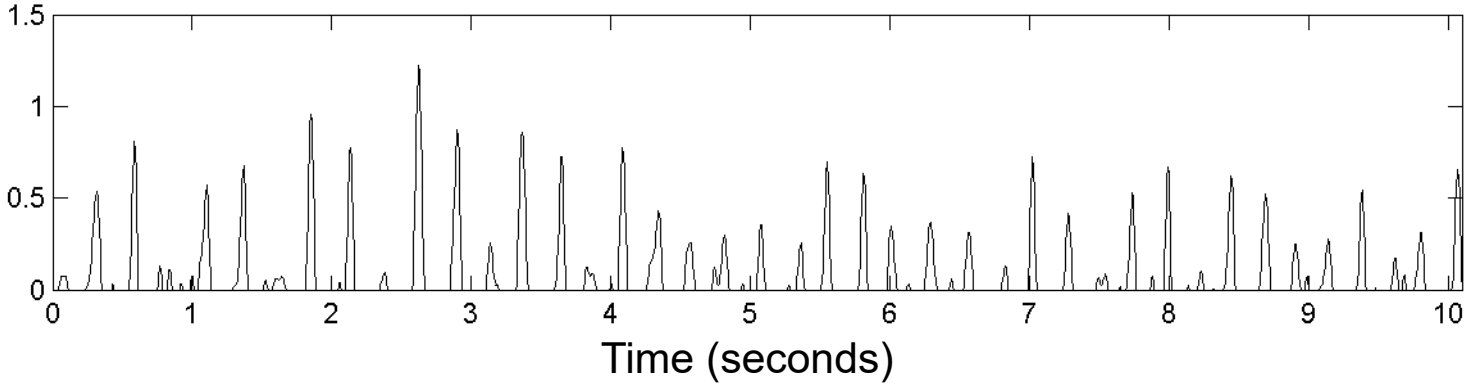


Halfwave rectification

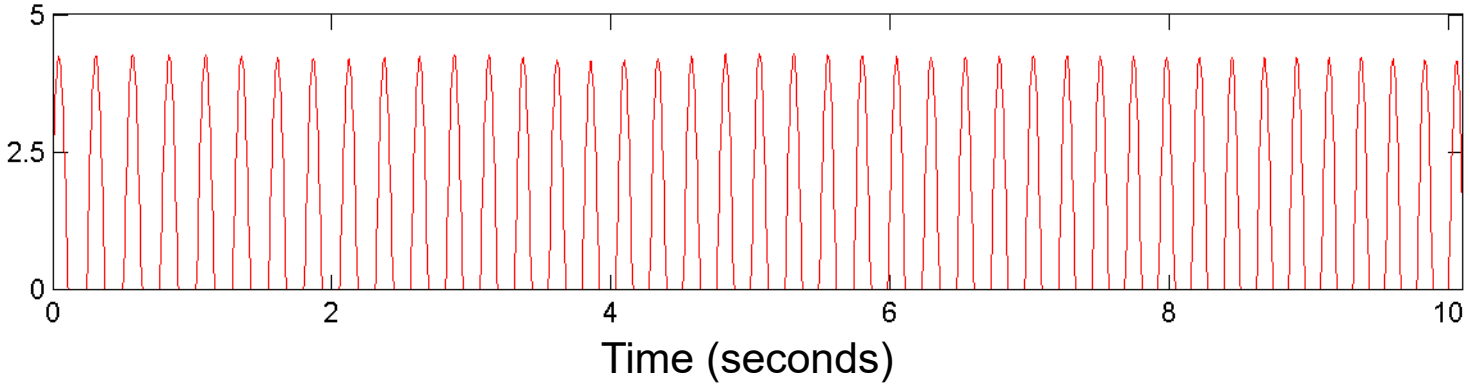


Local Pulse Tracking

Novelty Curve



Predominant Local Pulse (PLP)



Local Pulse Tracking

Novelty Curve

- Indicates note onset candidates
- Extraction errors in particular for soft onsets
- Simple peak-picking problematic

Predominant Local Pulse (PLP)

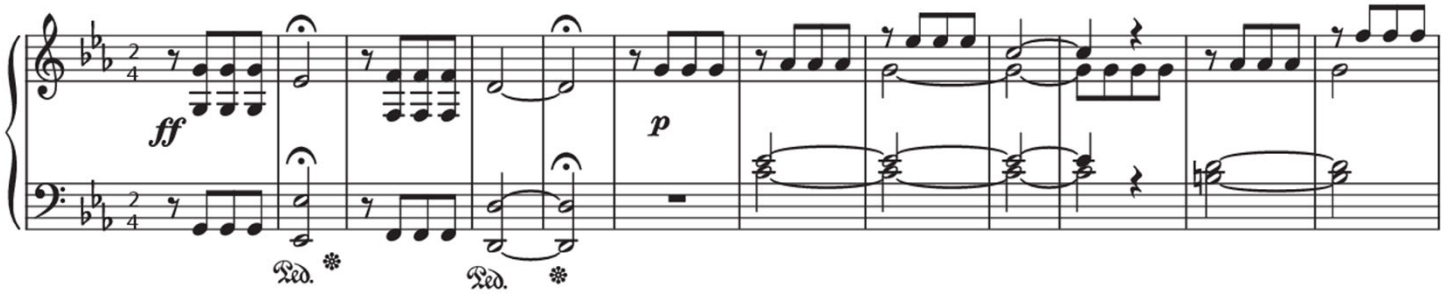
- Periodicity enhancement of novelty curve
- Accumulation introduces error robustness
- Locality of kernels handles tempo variations

Local Pulse Tracking

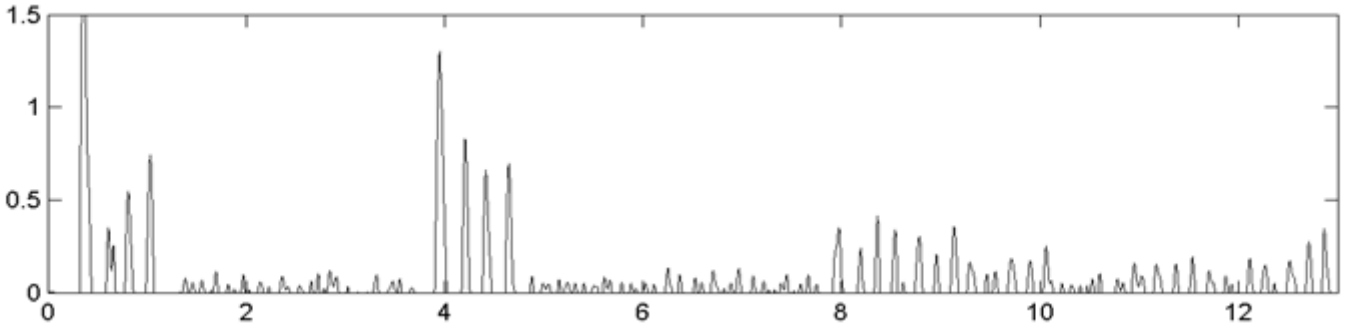
- Novelty function $\Delta : \mathbb{Z} \to \mathbb{R}$
- Fourier representation $\mathcal{F}(n,\omega) = \sum_{m\in\mathbb{Z}} \Delta(m)\overline{w}(m-n)\exp(-2\pi i\omega m)$
- Fourier tempogram $\mathcal{T}^{\mathrm{F}}(n,\tau) = |\mathcal{F}(n,\tau/60)|$
- Maximal tempo (per frame) $\tau_n := \underset{\tau\in\Theta}{\operatorname{argmax}} \mathcal{T}^{\mathrm{F}}(n,\tau)$

  Set of tempi, e.g., Θ = [30:300] BPM
- Phase $\varphi_n = -\frac{1}{2\pi}\operatorname{angle}\big(\mathcal{F}(n,\tau_n/60)\big)$
- Sinusoidal kernel $\kappa_n(m) := w(m-n)\cos\Big(2\pi\big((\tau_n/60)\cdot m - \varphi_n\big)\Big)$
- Periodicity curve (PLP) $\Gamma(m) = \big|\sum_{n\in\mathbb{Z}} \kappa_n(m)\big|_{\geq 0}$

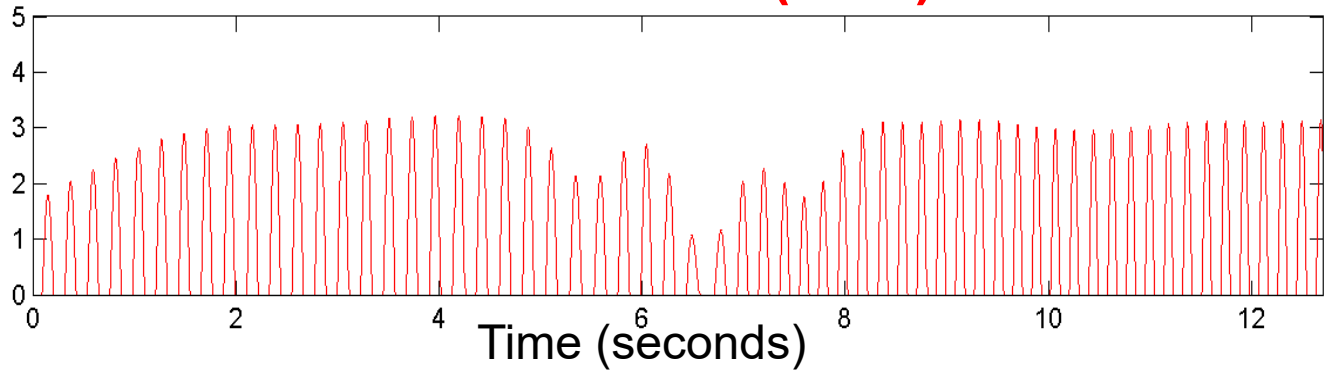
Local Pulse Tracking



Novelty Curve

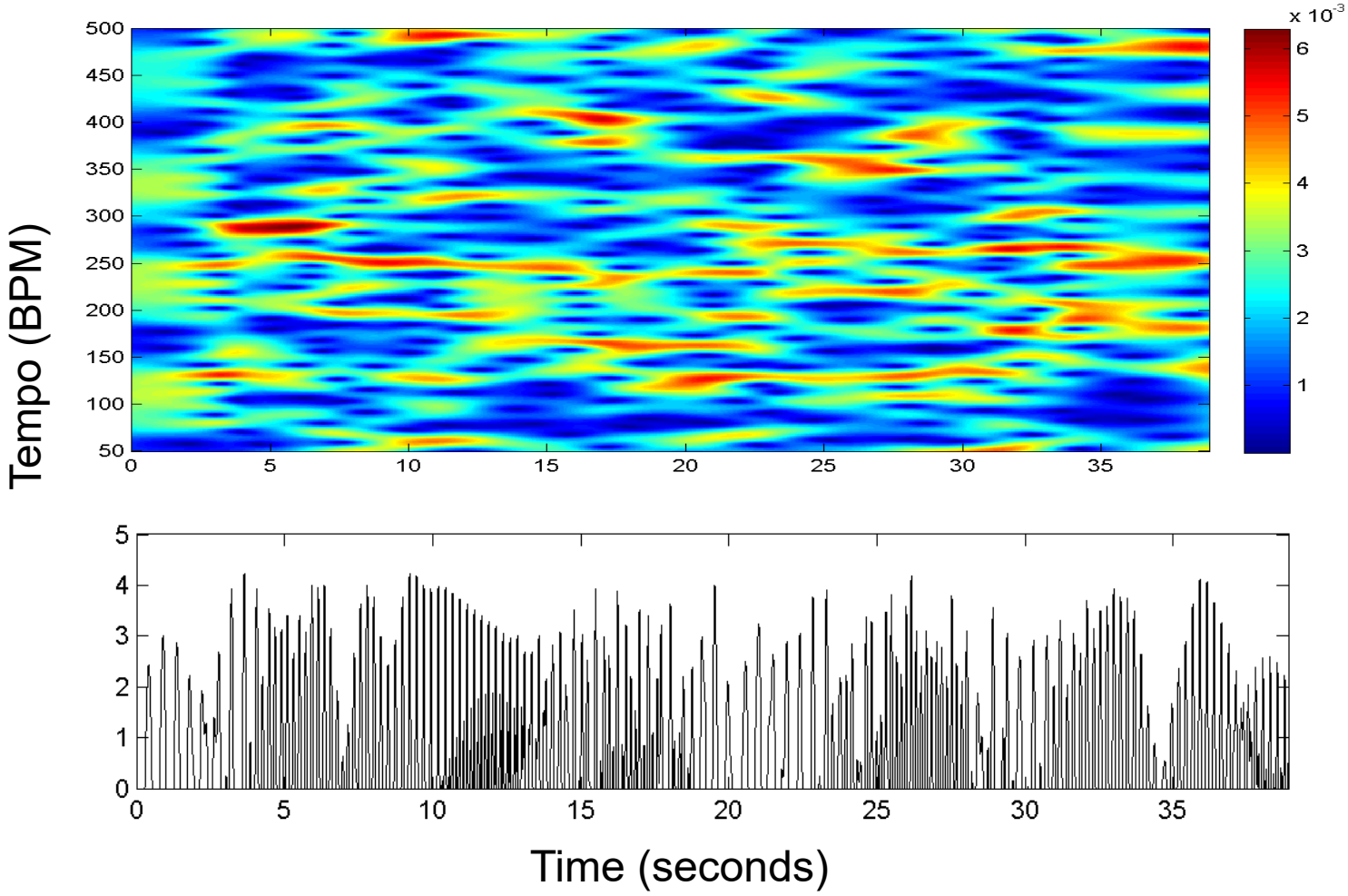


Predominant Local Pulse (PLP)



Local Pulse Tracking

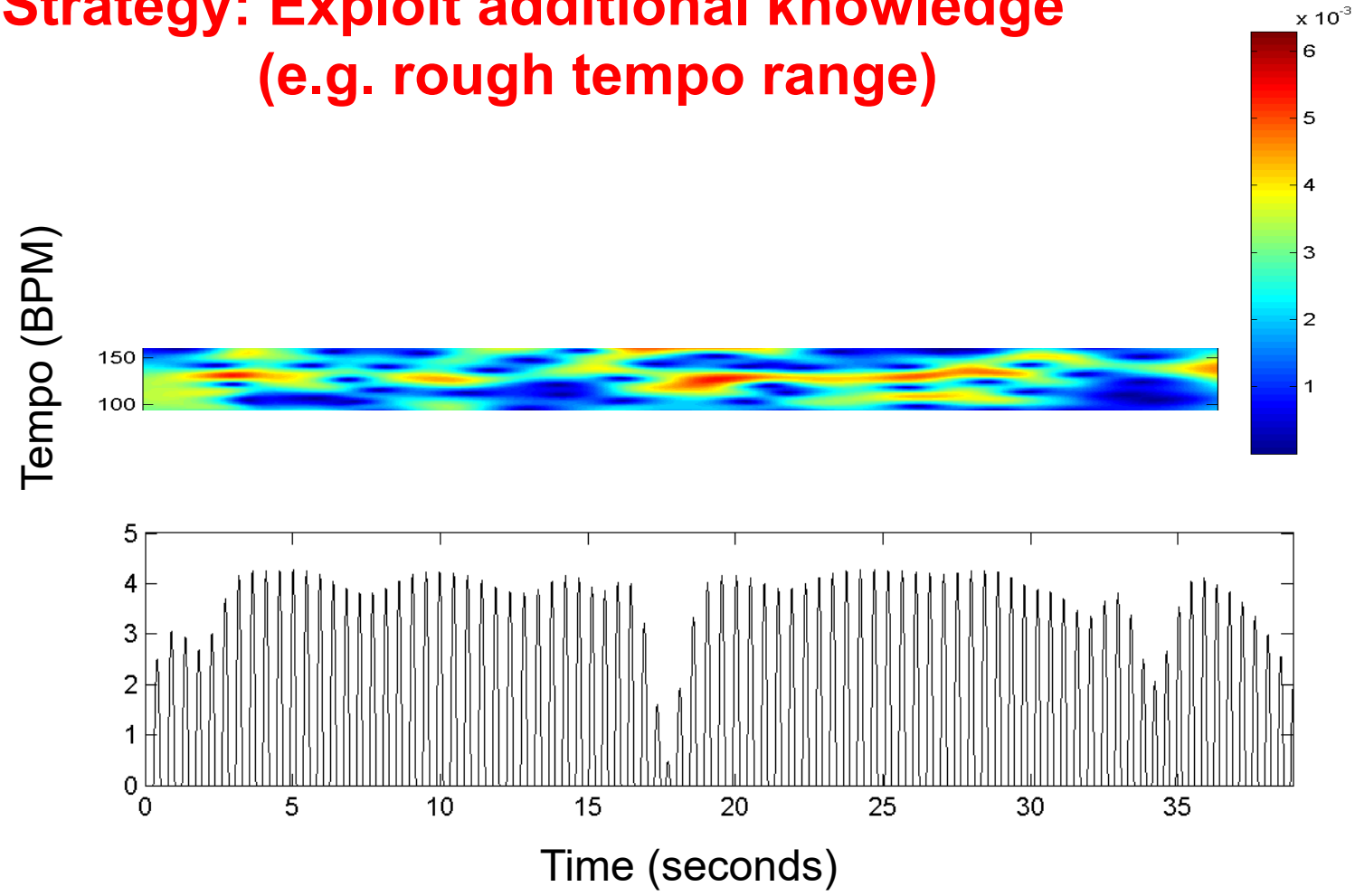
Borodin – String Quartet No. 2



Local Pulse Tracking

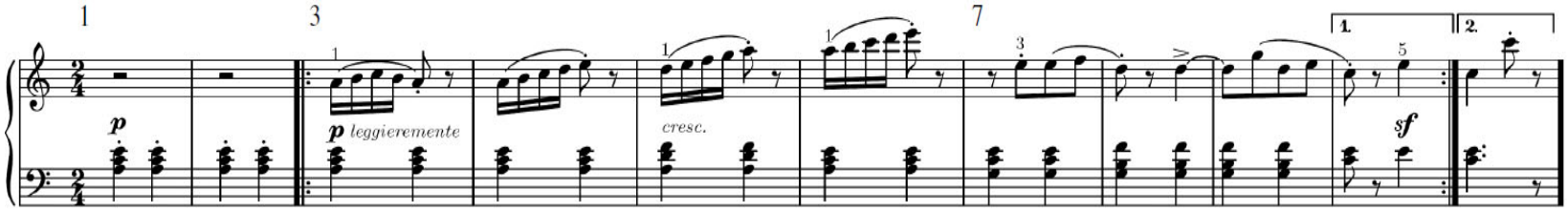
Borodin – String Quartet No. 2

Strategy: Exploit additional knowledge (e.g. rough tempo range)



Pulse Levels

Piano Etude Op. 100 No. 2 by Burgmüller



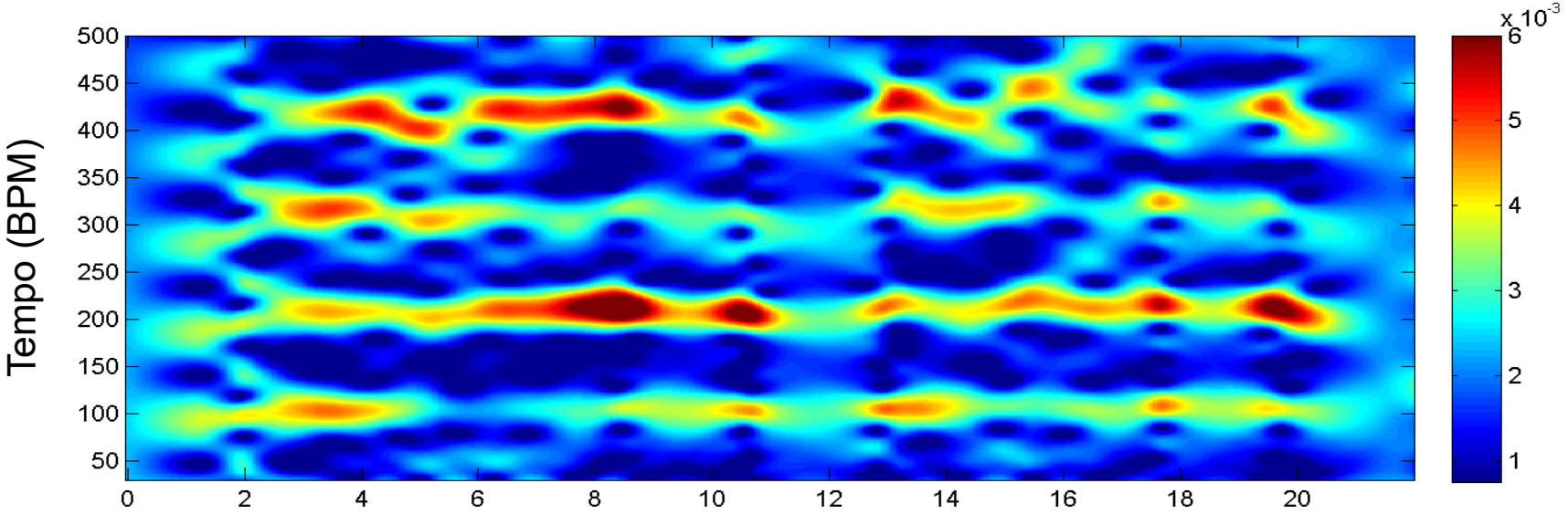
1/4 ● ● ● ●

1/8 • • • • • • • • • • • • • • • •

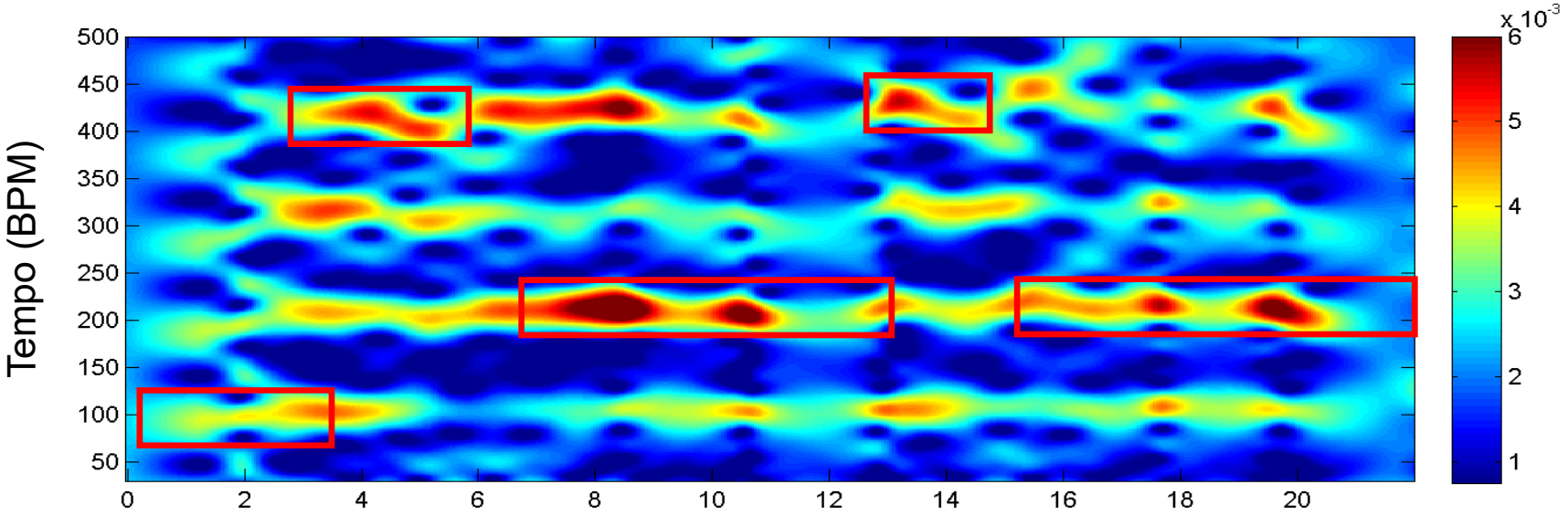
1/16 •••••••• •••••••• •••••••• ••••••••

What is the pulse level: Measure – Tactus – Tatum?

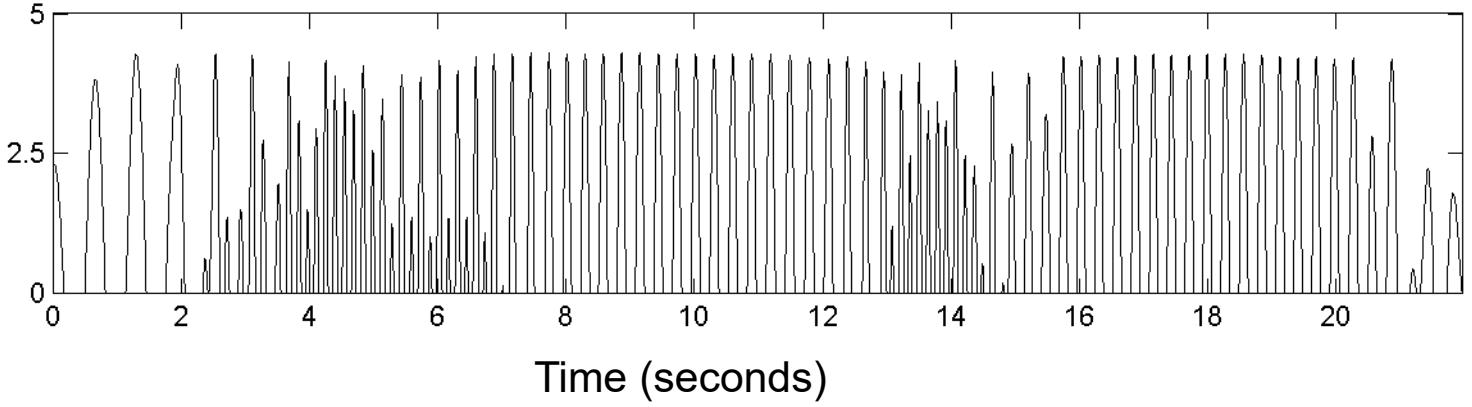
Pulse Levels



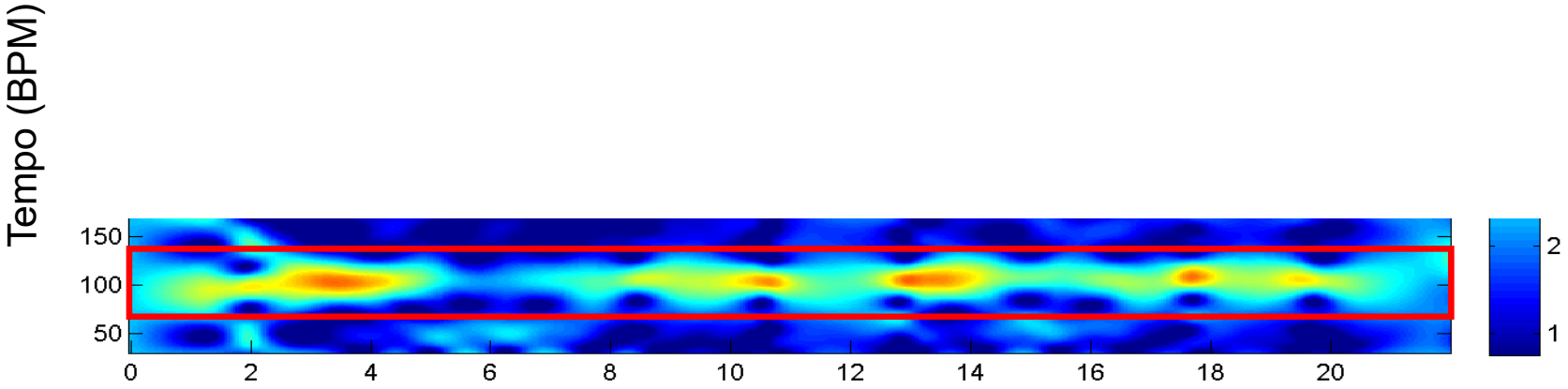
Pulse Levels



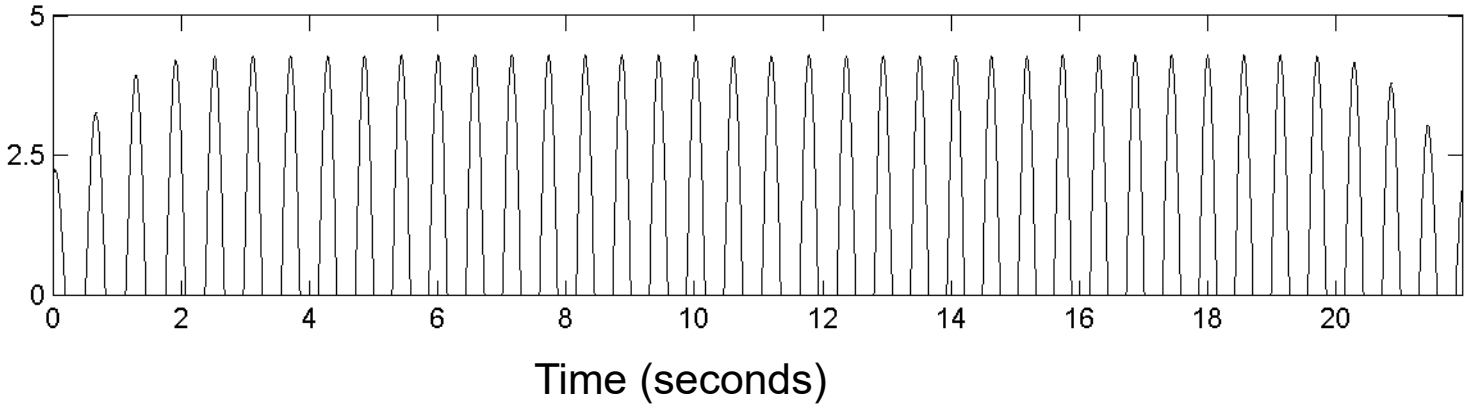
Switching of predominant pulse level



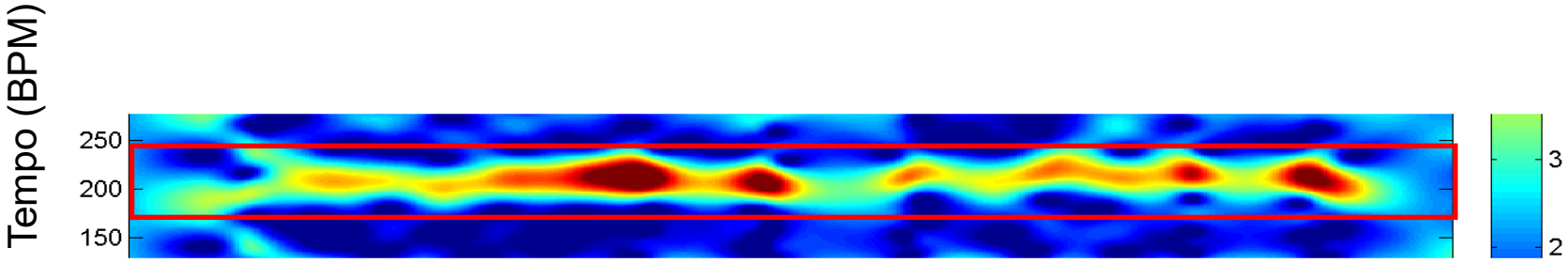
Pulse Levels



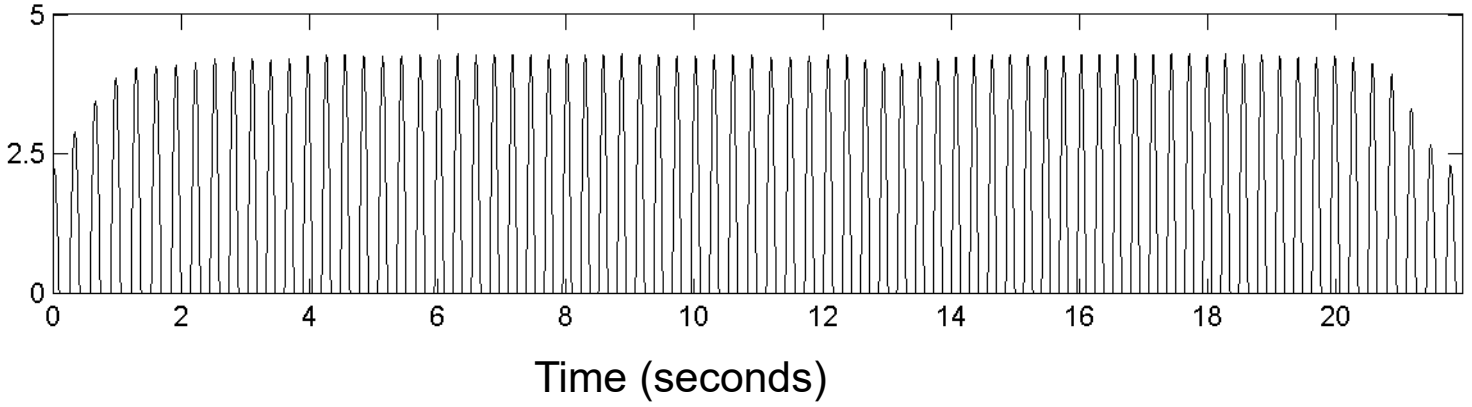
1/4 **note pulse level**



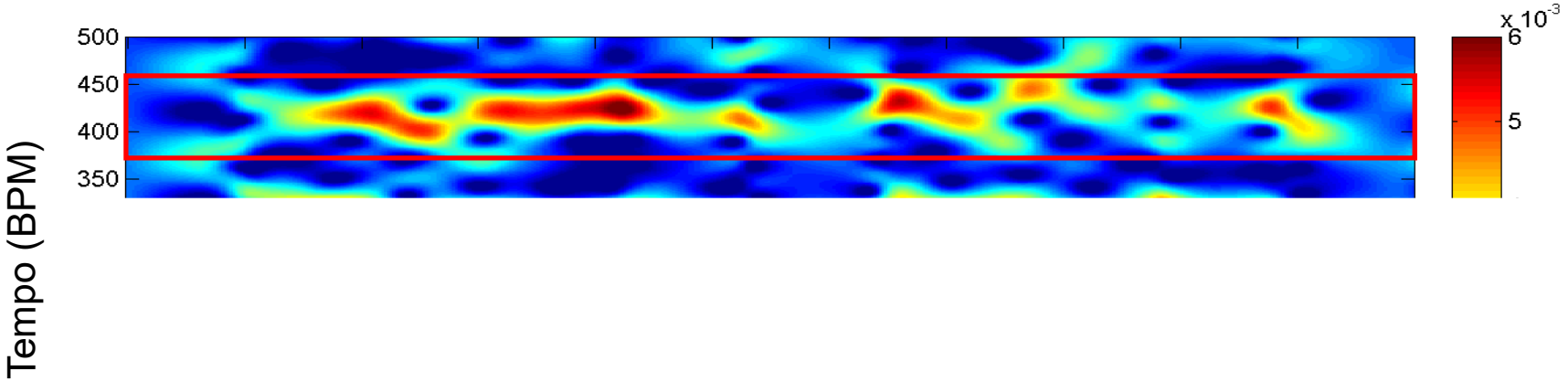
Pulse Levels



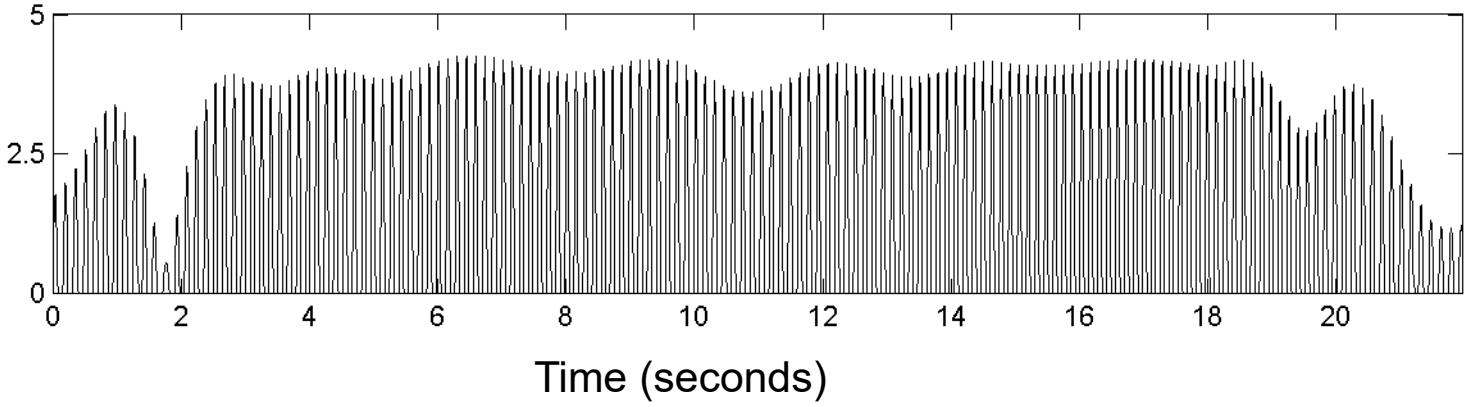
1/8 **note pulse level**



Pulse Levels

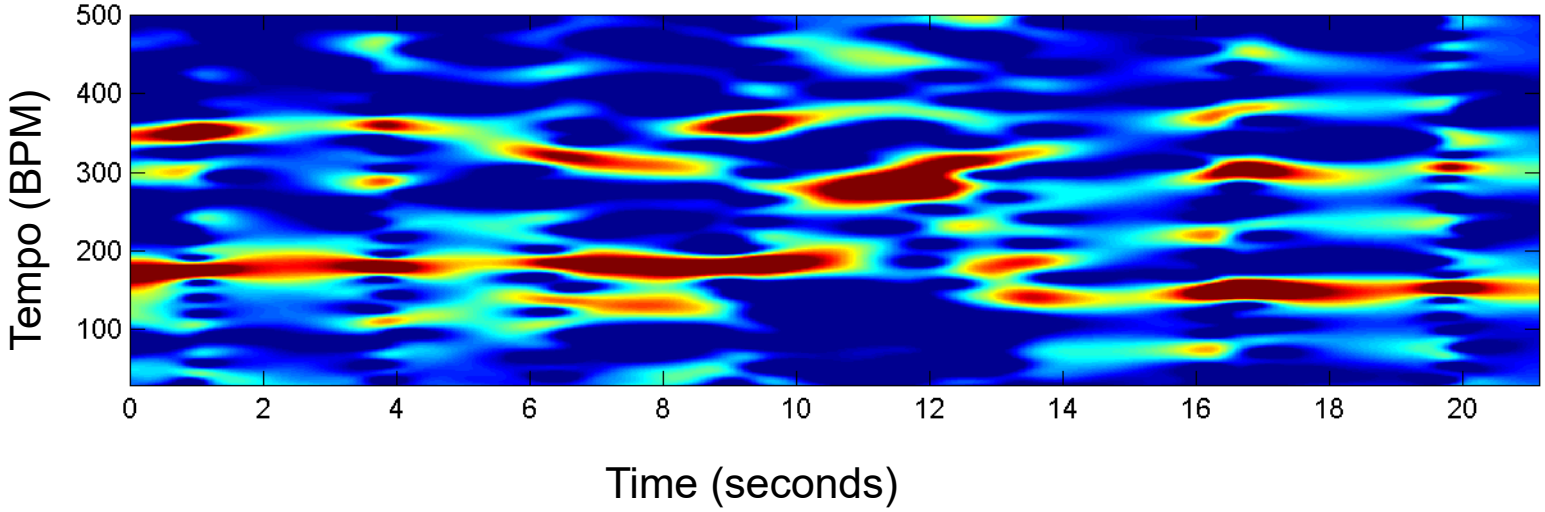


1/16 **note pulse level**



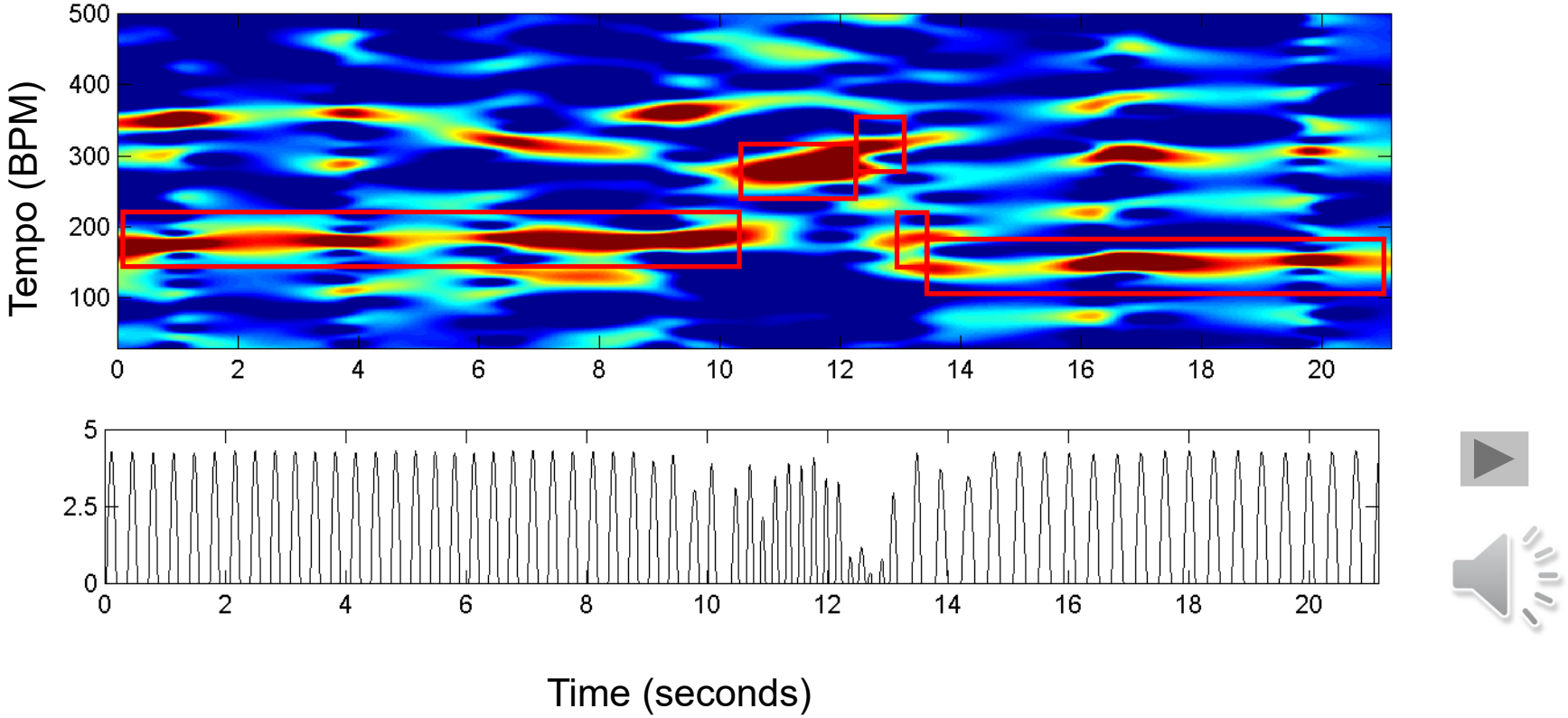
Local Pulse Tracking

Brahms Hungarian Dance No. 5



Local Pulse Tracking

Brahms Hungarian Dance No. 5

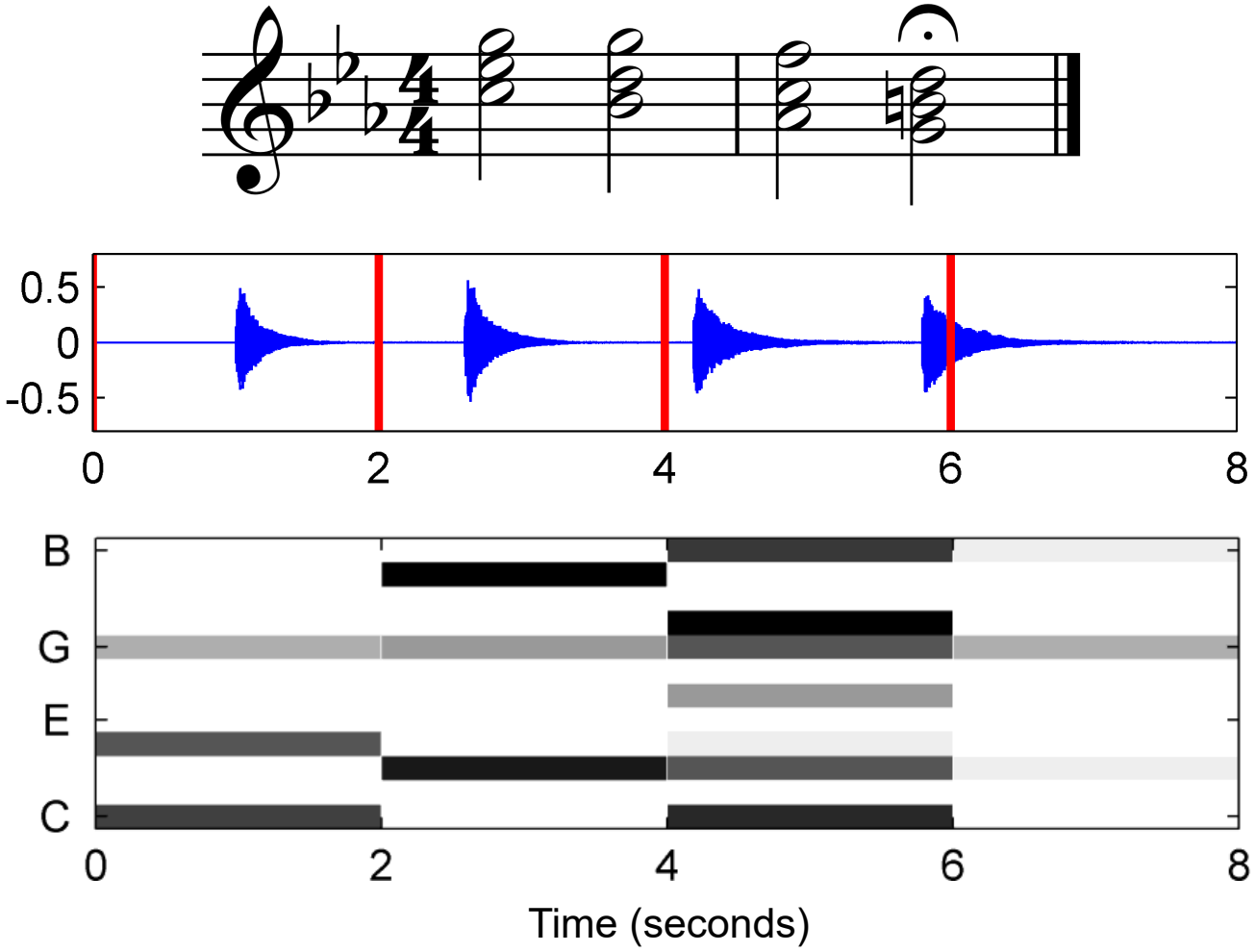


Applications

- Feature design
  (beat-synchronous features, adaptive windowing)
- Digital DJ / audio editing
  (mixing and blending of audio material)
- Music classification
- Music recommendation
- Performance analysis
  (extraction of tempo curves)

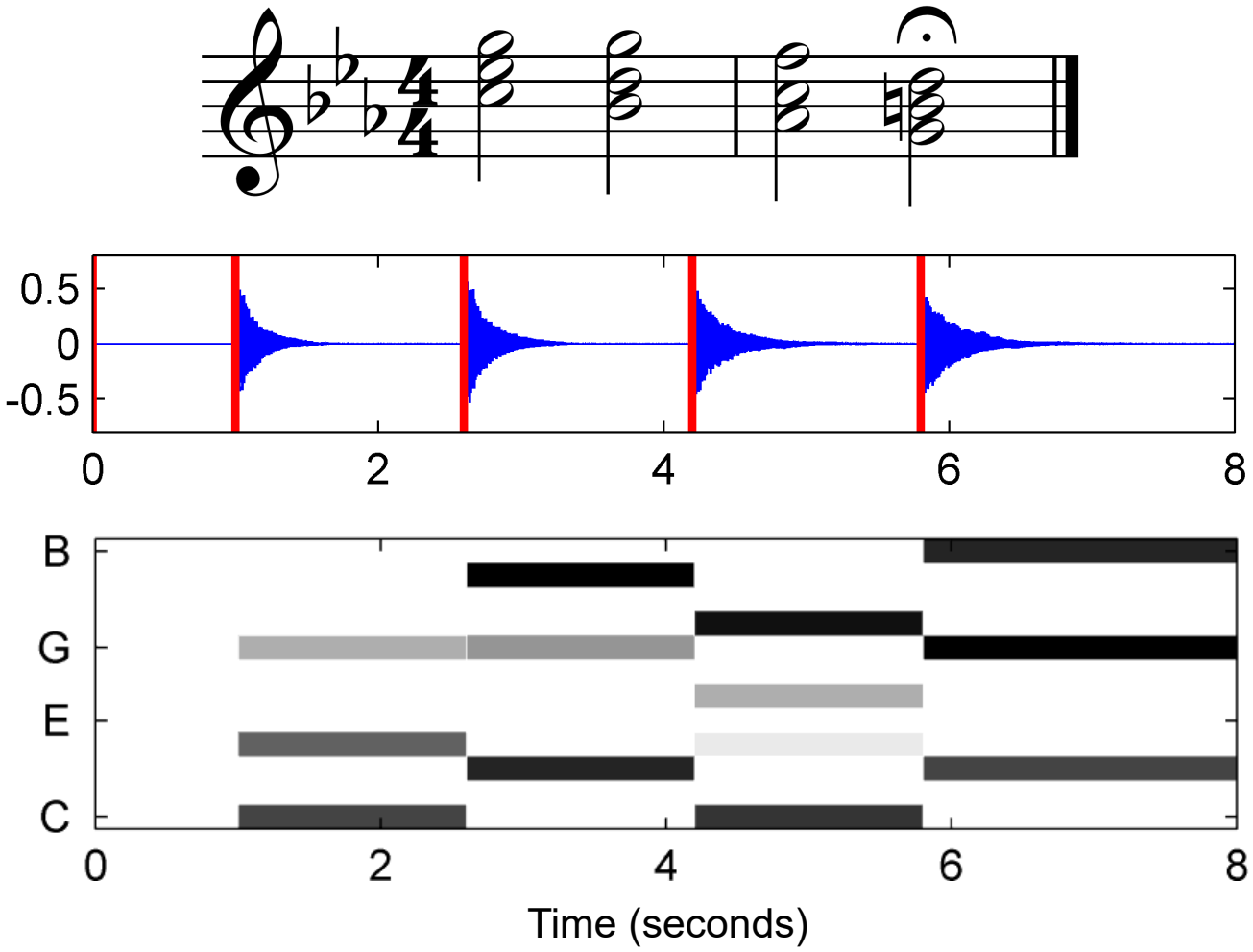
Application: Feature Design

Fixed window size



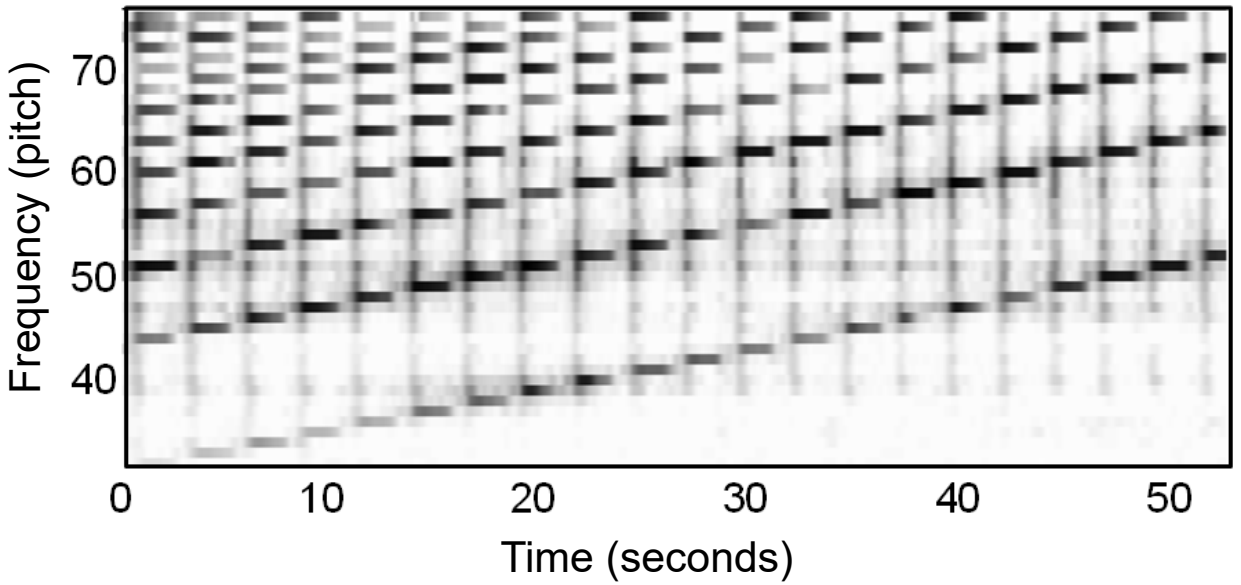
Application: Feature Design

Adaptive window size



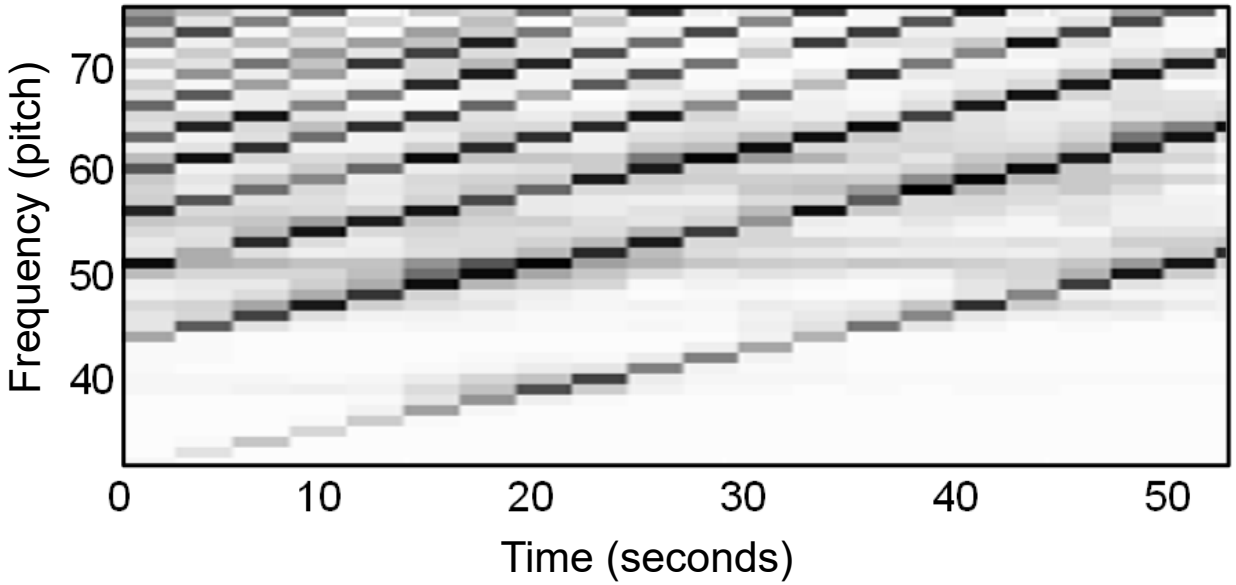
Application: Feature Design

Fixed window size



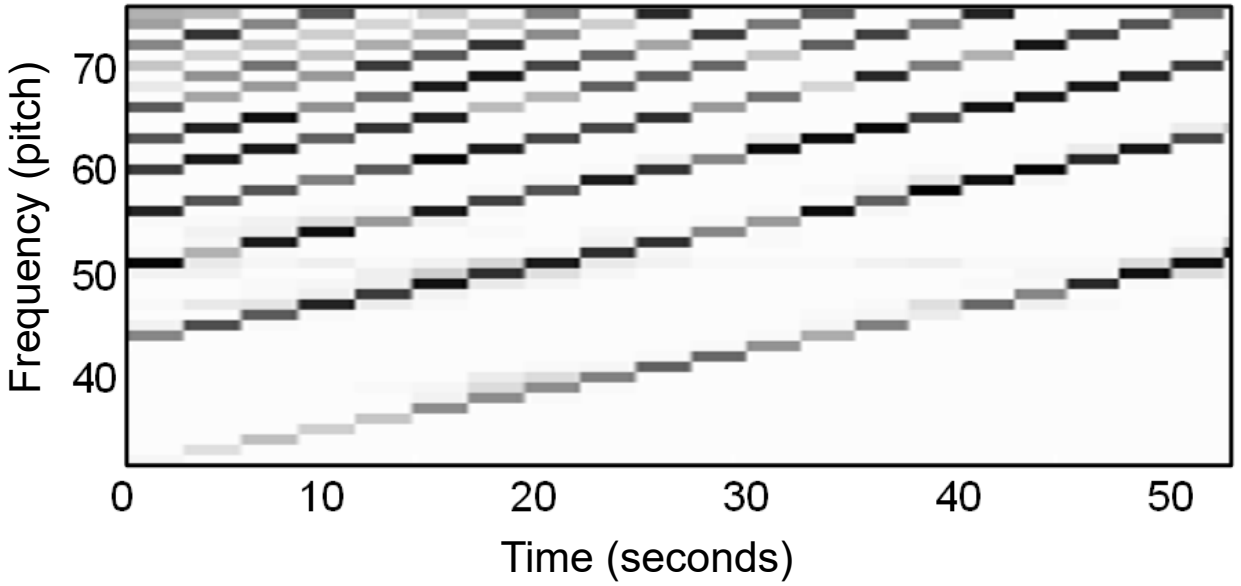
Application: Feature Design

Adaptive window size



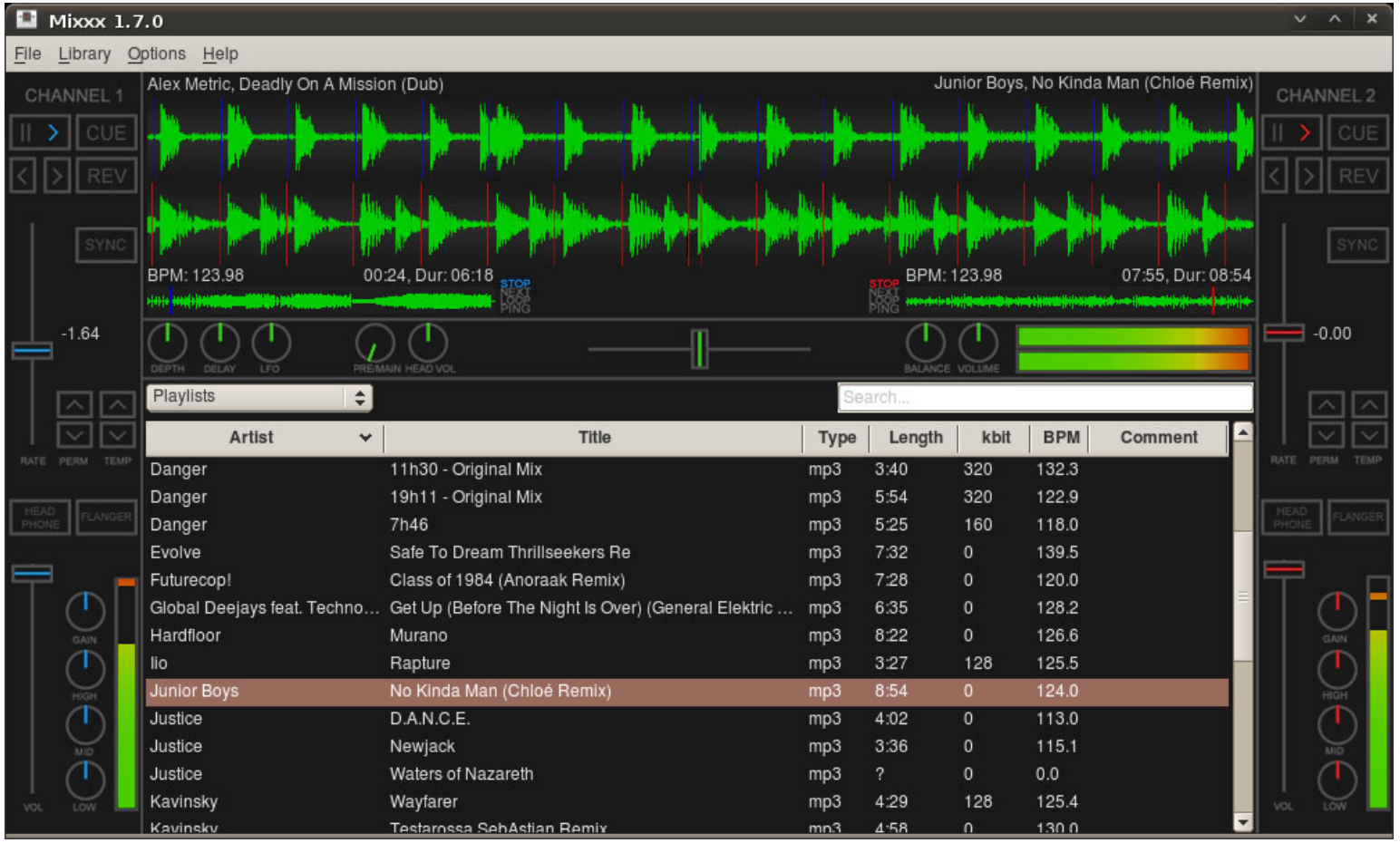
Application: Feature Design

Adaptive window size



Denoising by excluding boundary neighborhoods

Application: Audio Editing (Digital DJ)



http://www.mixxx.org/

Application: Beat-Synchronous Light Effects

Summary

1. Onset Detection
   - Novelty curve (*something is changing*)
   - Indicates note onset candidates
   - Hard task for non-percussive instruments (strings)

2. Tempo Estimation
   - Fourier tempogram
   - Autocorrelation tempogram
   - Musical knowledge (tempo range, continuity)

3. Beat tracking
   - Find most likely beat positions
   - Exploiting phase information from Fourier tempogram